



2018 Annual INCOSE  
Great Lakes Regional Conference  
**SYSTEMS AT THE CROSSROADS**  
17 - 20 October 2018 | Indianapolis, Indiana

# Simulation Modeling Workshop 19 October 2018

# Rainer Dronzek

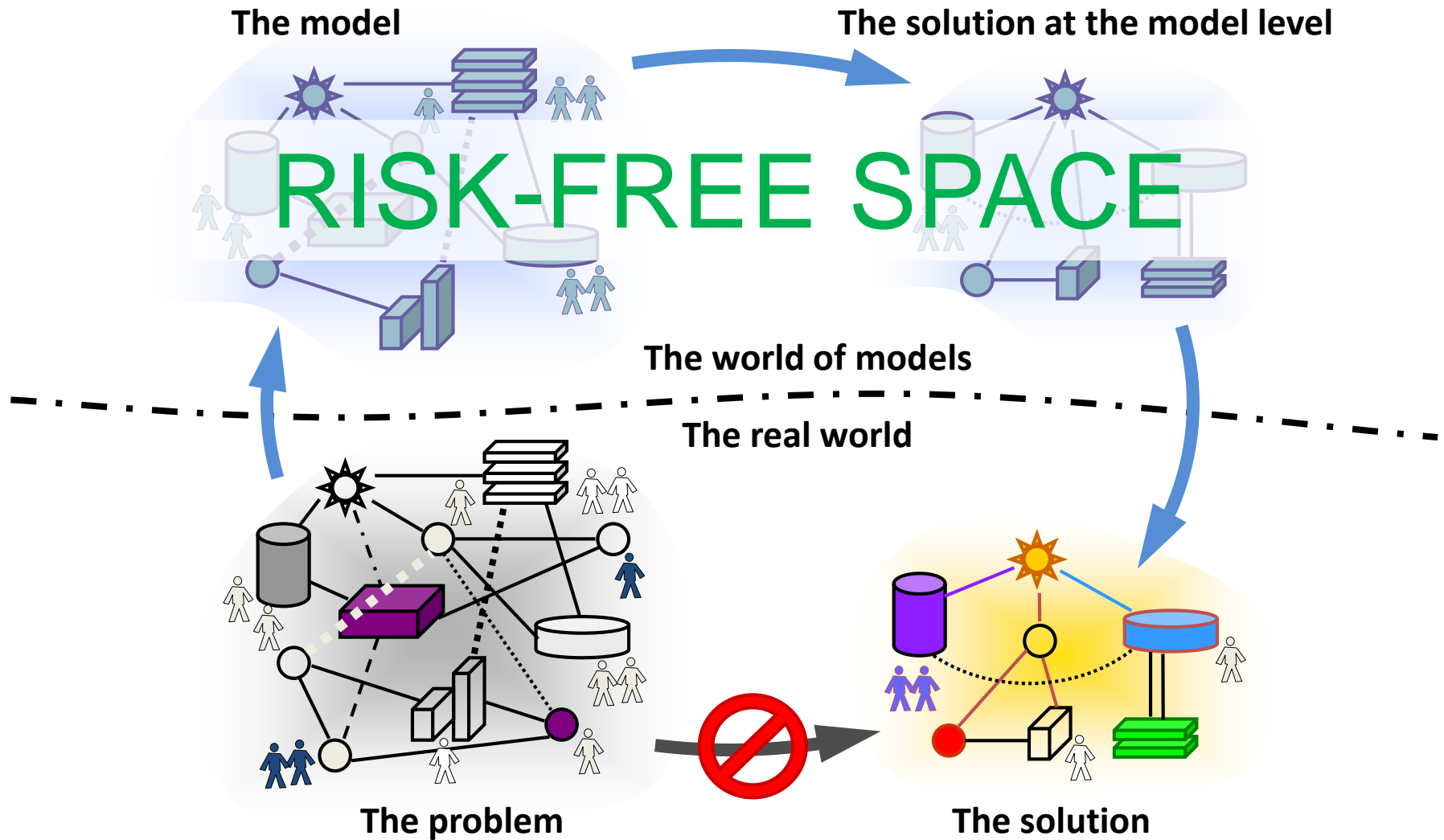
- Bio
  - Rainer has held engineering and management positions in the aerospace, oil & gas and consulting industries. He began his systems engineering career on the Space Shuttle Program at the Kennedy Space Center, where he was first introduced to the art and science of simulation modeling. He has managed projects and standing teams, founded a simulation consulting firm, and organized events and conferences around simulation modeling
  - He is a Regional Director with The AnyLogic Company and holds a B.S. in Electrical Engineering from Bradley University
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# Agenda

- Multi-Method Simulation Modeling
- The Model Development Environment
- Discrete Event Modeling
- The Factory Model
- System Dynamics Modeling
- The Bass Diffusion Model
- Agent Based Modeling
- Disease Spread Model
- Supply Chain Model
- Railway Station Model
- Group Exercise
- Further Information
- Distribution of Simulation Software

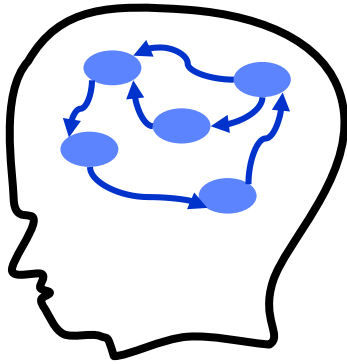
# Multi-Method Simulation Modeling

# Modeling

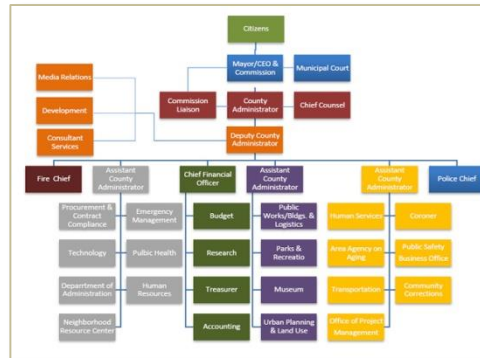


# Types of models

Mental models



Boxes connected with lines



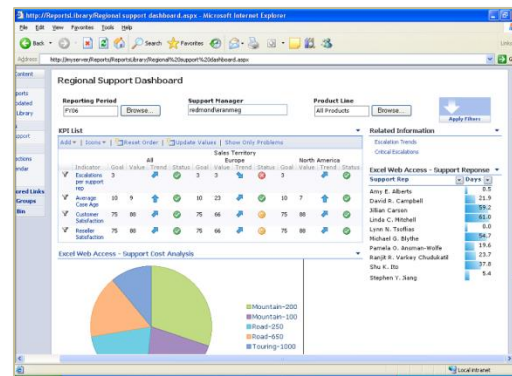
Physical models



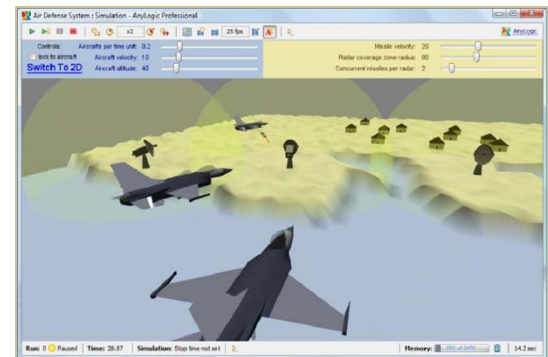
Formulas on a sheet of paper

$$\begin{aligned} \vec{F} &= m \vec{a} \quad \vec{p} = m \vec{v} \quad KE = \frac{1}{2} m v^2 = \frac{p^2}{2m} \quad W_{\text{tot}} = \Delta(KE) = KE_f - KE_i \quad A_{\text{gravitational}} = 4\pi r^2 \\ \frac{R}{r^2} &= k \frac{q_1 q_2}{r^2} = \frac{1}{4\pi \epsilon_0} \frac{q_1 q_2}{r^2} \quad \epsilon_0 = 8.85(10)^{-12} \left[ \frac{C^2}{N m^2} \right] \quad k = \frac{1}{4\pi \epsilon_0} \quad A_{\text{area}} = \pi r^2 \\ E &= \frac{F}{q} \quad E = k \frac{q}{r^2} = \frac{1}{4\pi \epsilon_0} \frac{q}{r^2} \quad V = k \frac{q}{r} = \frac{1}{4\pi \epsilon_0} \frac{q}{r} \quad V = \frac{U}{q} \quad \sim e^{-t/RC} \\ \sum_{\text{surf}} E_{\perp} \Delta A &= \frac{q}{\epsilon_0} \quad Q = VC \quad C = \frac{A \epsilon_0}{d} \quad \sigma = \frac{Q}{A} \quad V = Ed \quad E = \frac{\sigma}{\epsilon_0} \quad U = \frac{QV}{2} = \frac{Q^2}{2C} \\ \sum_{\text{junc}} I_j &= 0 \quad \sum_{\text{loop}} V_j = 0 \quad V = IR \quad P = IV = I^2 R = \frac{V^2}{R} \quad R_{\text{tot}} = R_1 + R_2 \quad \frac{1}{C_{\text{tot}}} = \frac{1}{C_1} + \frac{1}{C_2} \\ F &= q v B_{\perp} = q v B \sin(\theta) \quad B = \frac{\mu_0 I}{2 \pi r} \quad \mu_0 = 4 \pi (10)^{-7} \text{ Tm/A} \\ F &= I L B_{\perp} = I L B \sin(\theta) \quad \sum_{\text{circuit}} B_{\parallel} \Delta l = \mu_0 I_1 \end{aligned}$$

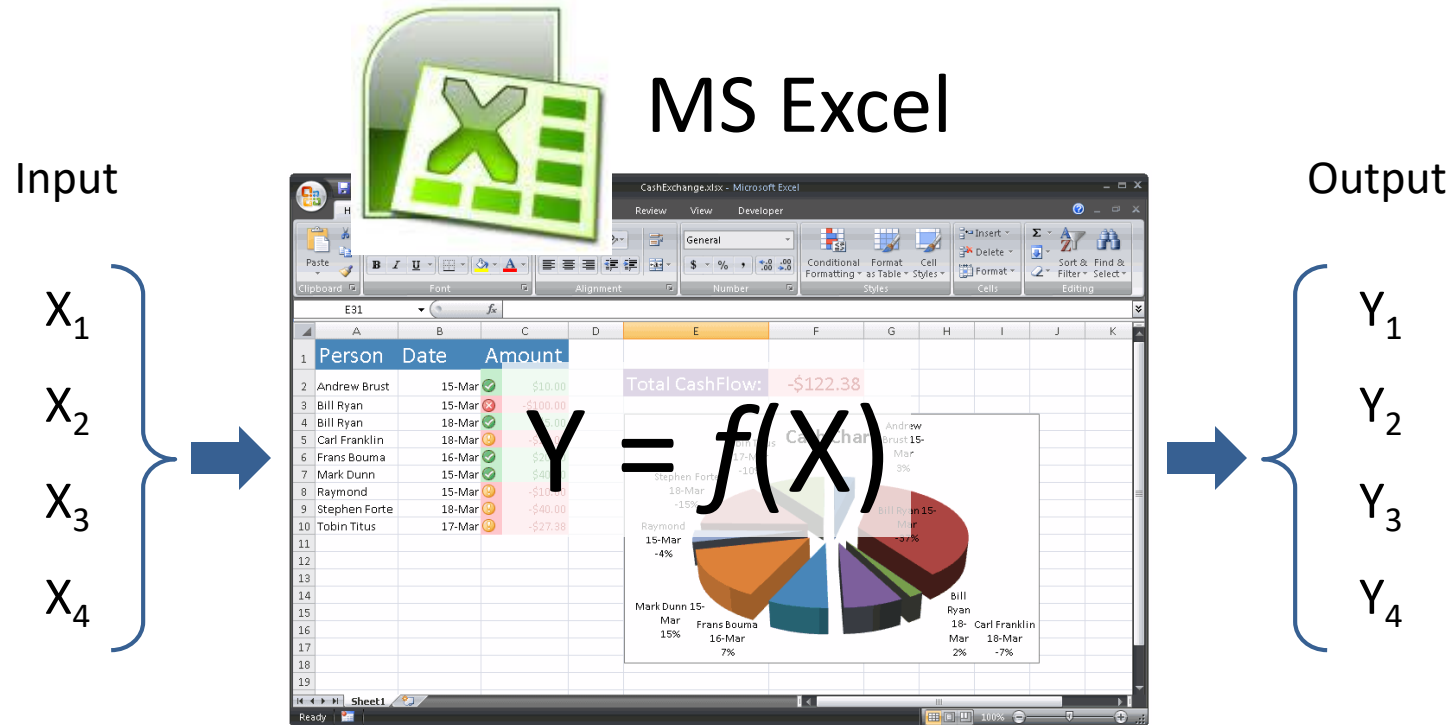
Excel spreadsheets



Simulation models



# The most popular modeling tool is:



Analytical solution  
(formulas and scripts)

# However...

- You can find an analytical solution if:
  - The number of parameters is 'manageable'
  - Behavior is linear
  - Dependencies are clear, easy to build a mental model
- But what if:
  - Too many parameters
  - Non-linear, non-obvious influences
  - Time and causal dependencies
  - Counter-intuitive behavior
  - Uncertainty (stochastic system)





# Example: Bank

- A simplistic case:
  - On average 10 clients per hour
  - Only one teller at the counter
  - Mean service time is 5 minutes
- We want to find out:
  - Mean waiting time in the queue
  - [Other metrics can be derived from that one]



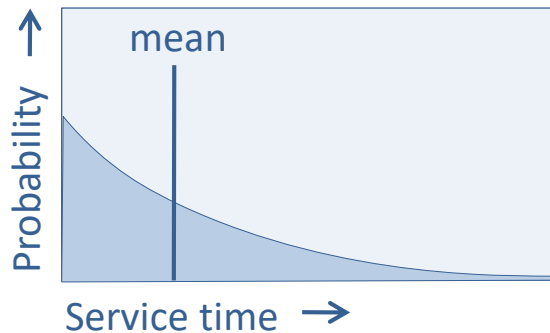
- 
- It'll take you a few seconds to find the analytical solution:

$$\text{Mean waiting time* } w = \frac{\lambda b^2}{1 - \lambda b}, \text{ where } \begin{array}{l} \lambda - \text{arrival rate} \\ b - \text{mean service time} \end{array}$$

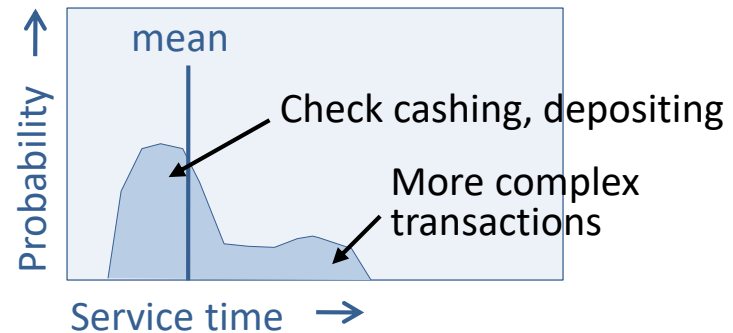
\* This holds only for a **Poisson stream** of clients (independent arrivals with constant rate) and **exponentially distributed** service time.

# Bank. Assumptions of the analytic approach

- What do these assumptions mean?
  - Independent arrivals of clients – this should be an OK assumption for the bank
  - Exponentially distributed service time:



This is far from reality. The distribution is more likely of this shape:



- Then the Internet search will suggest another formula:

$$w = \frac{\lambda b^2 (1 + C_b^2)}{2(1 - \lambda b)}, \text{ where } C_b - \text{coefficient of variation of service time}$$

# Bank. What if a bit less simplistic case?

- Let there be several ( $K$ ) tellers
  - This is so-called “multi-server queue model”. The analytic solution\*:

$$w = \frac{Pb}{K(1-\rho)}, \text{ where } \rho = \frac{\lambda b}{K} \text{ - system utilization,}$$

$$P = \frac{(K\rho)^K}{K!(1-\rho)} P_0, \text{ where } P_0 = \left[ \frac{(K\rho)^K}{K!(1-\rho)} + \sum_{i=0}^{K-1} \frac{(K\rho)^i}{i!} \right]^{-1}$$

- probability of all tellers being busy                      - probability of “no clients in the bank”

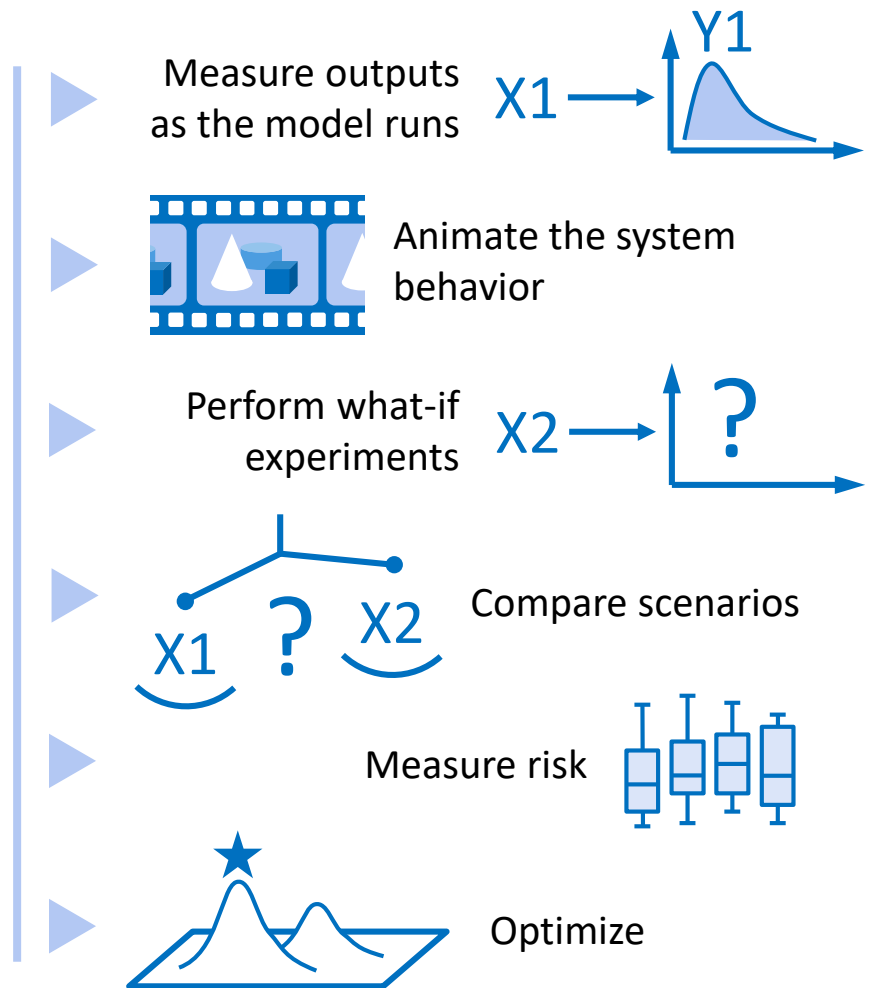
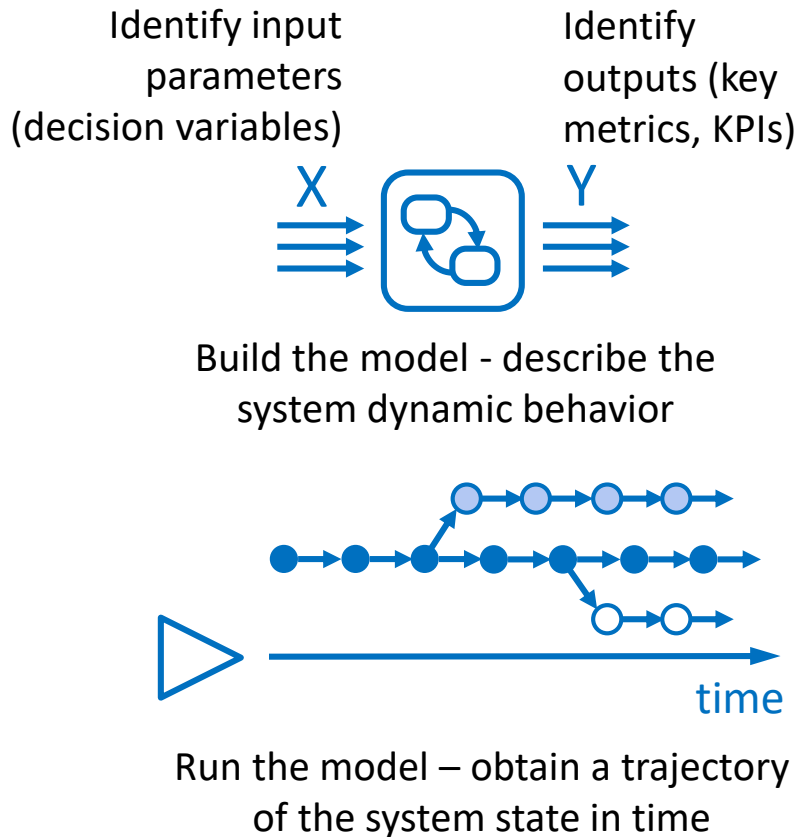
\* This, however, is valid only for Poisson stream of clients and exponentially distributed service time.

- And what if service time has a different distribution?
  - Even for such a simple system there is no analytic solution

# Bank model

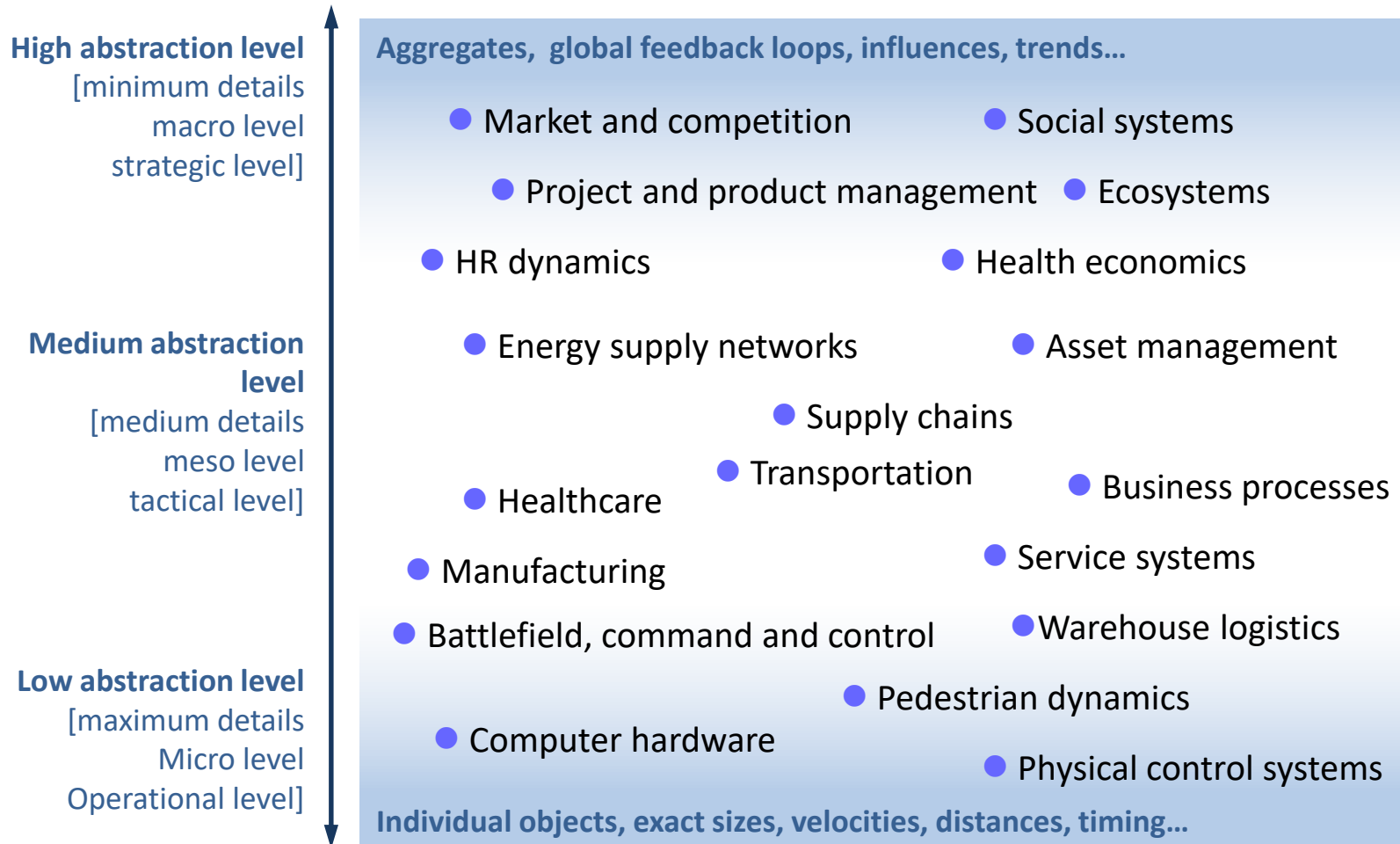
- In the real bank the process is far more complex:
  - Some transactions can be done only by some particular employees
  - The client can be redirected to other employees
  - The tellers may share resources, such as a printer or a copier
  - Different employees may have different skills and performance
  - Etc.
- The analytic solution probably does not exist
  - Even if it exists, who will find it for you?
  - Almost any change in the process makes the previous analytic solution void
- The only analysis method for such systems that has foreseeable complexity and guarantees the result is: simulation modeling

# Simulation modeling

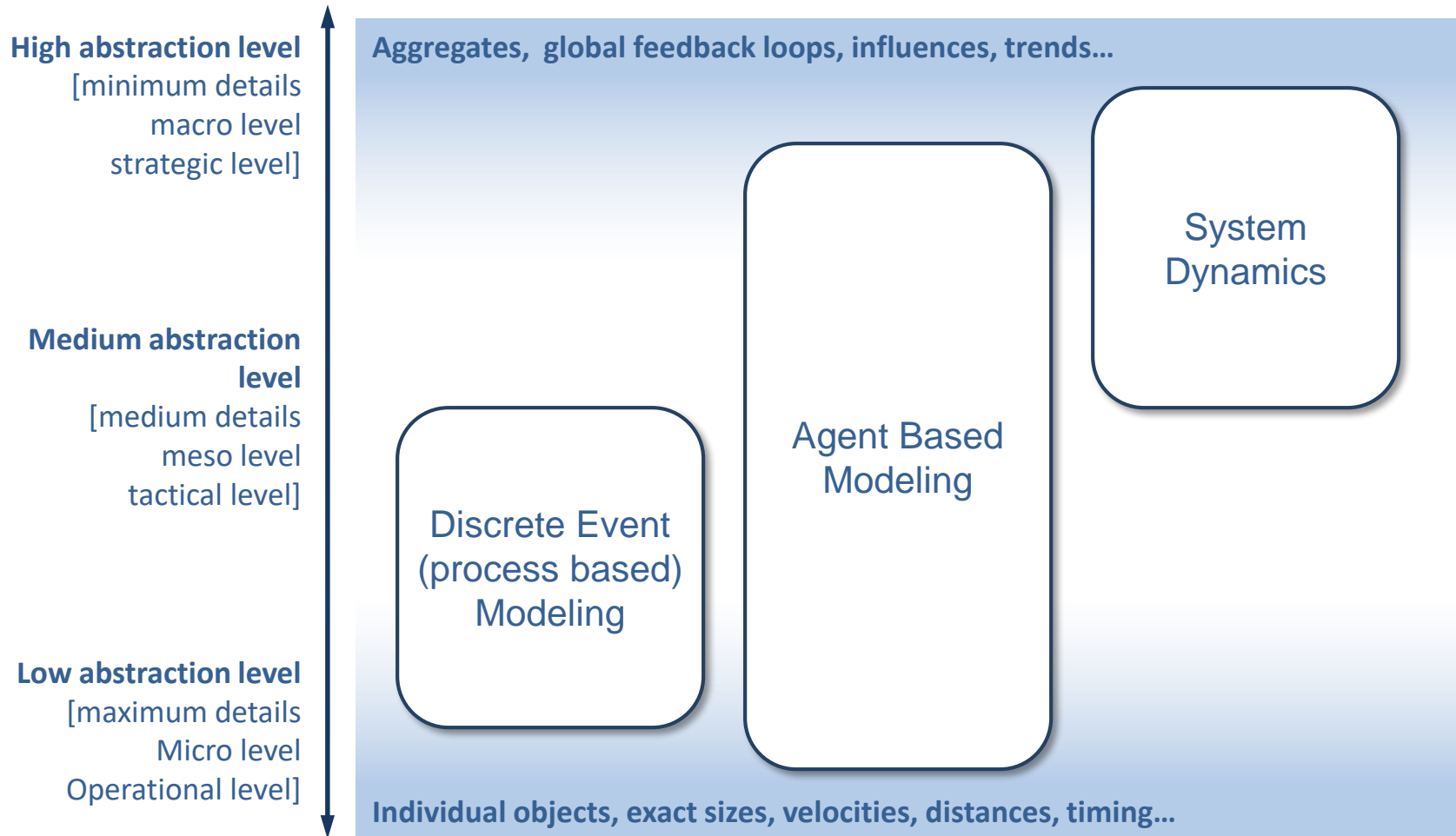


- Dynamic simulation enables much more detailed analysis and can solve problems that spreadsheet-based or LP-based analytics can't

# Application areas

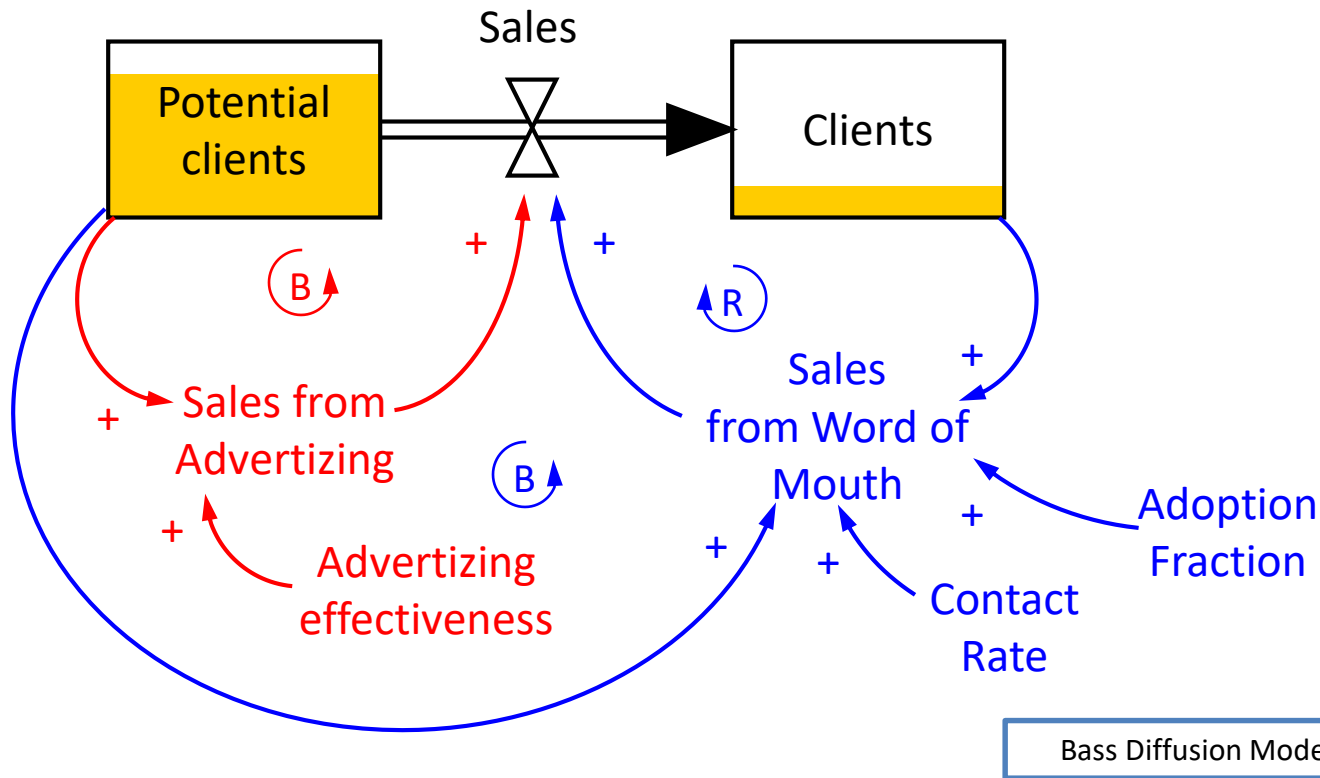


# Methods in simulation modeling



# System Dynamics Jay Forrester '50s

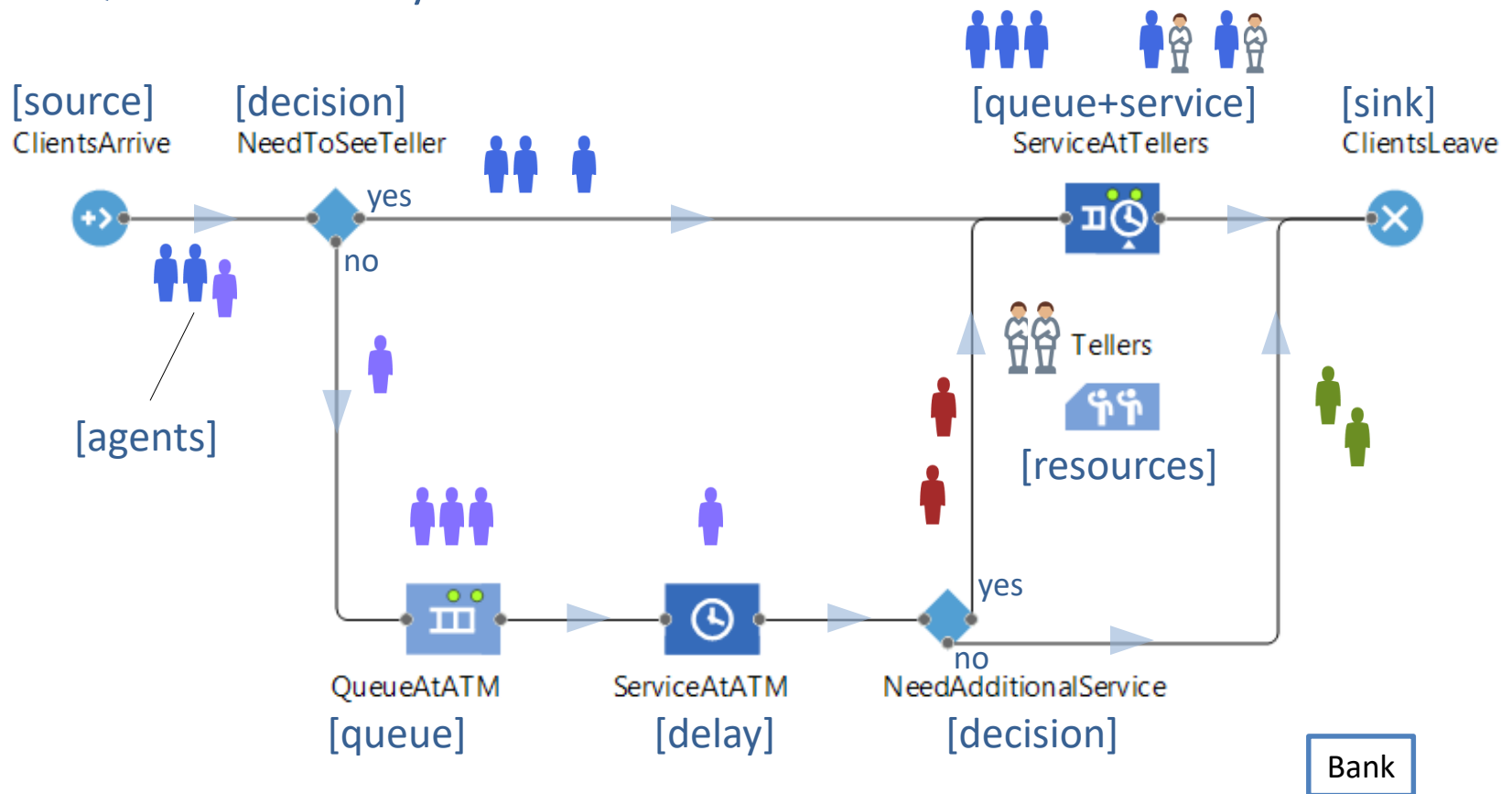
- Stocks, flows
  - Interacting feedback loops





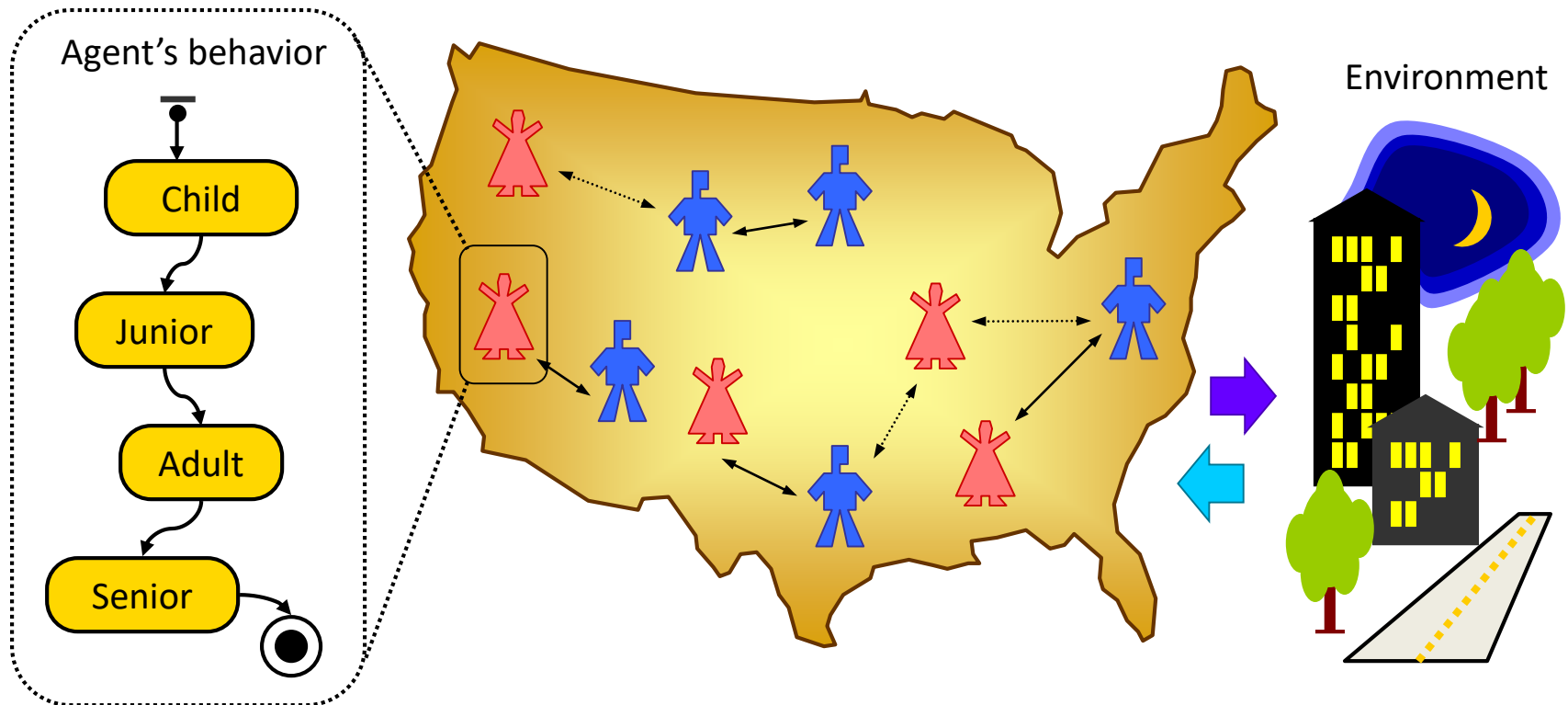
# Discrete event modeling. G. Gordon '60s

- Agents and resources. Flowchart diagram
  - Queues and delays



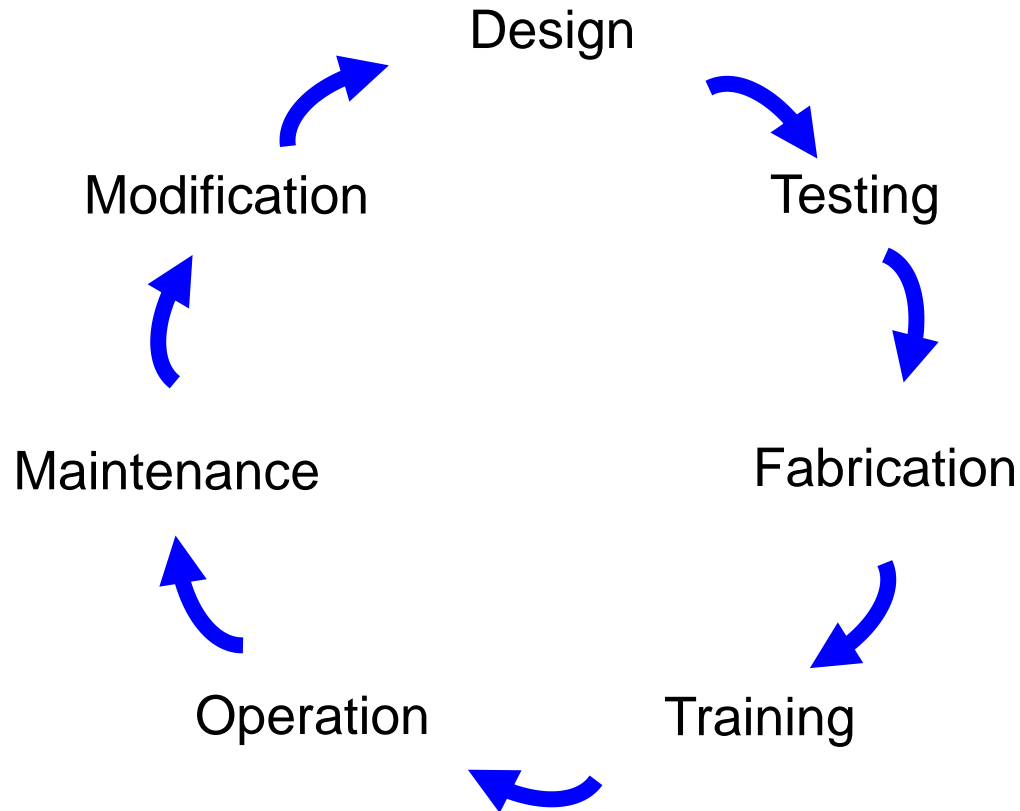
# Agent based modeling

- We focus on individual objects and describe their local behavior, local rules
  - Sometimes, we also model the dynamics of the environment



# When to simulate - the circle of life

*Simulation*



# Characteristics of a simulation model

- Takes random (stochastic) behavior into account
- May models each agent moving through a system
- Handles complex interactions
- Not all system details are modeled
- Abstracts the system to an appropriate level
- Compresses time
- Can animate system explicitly or conceptually

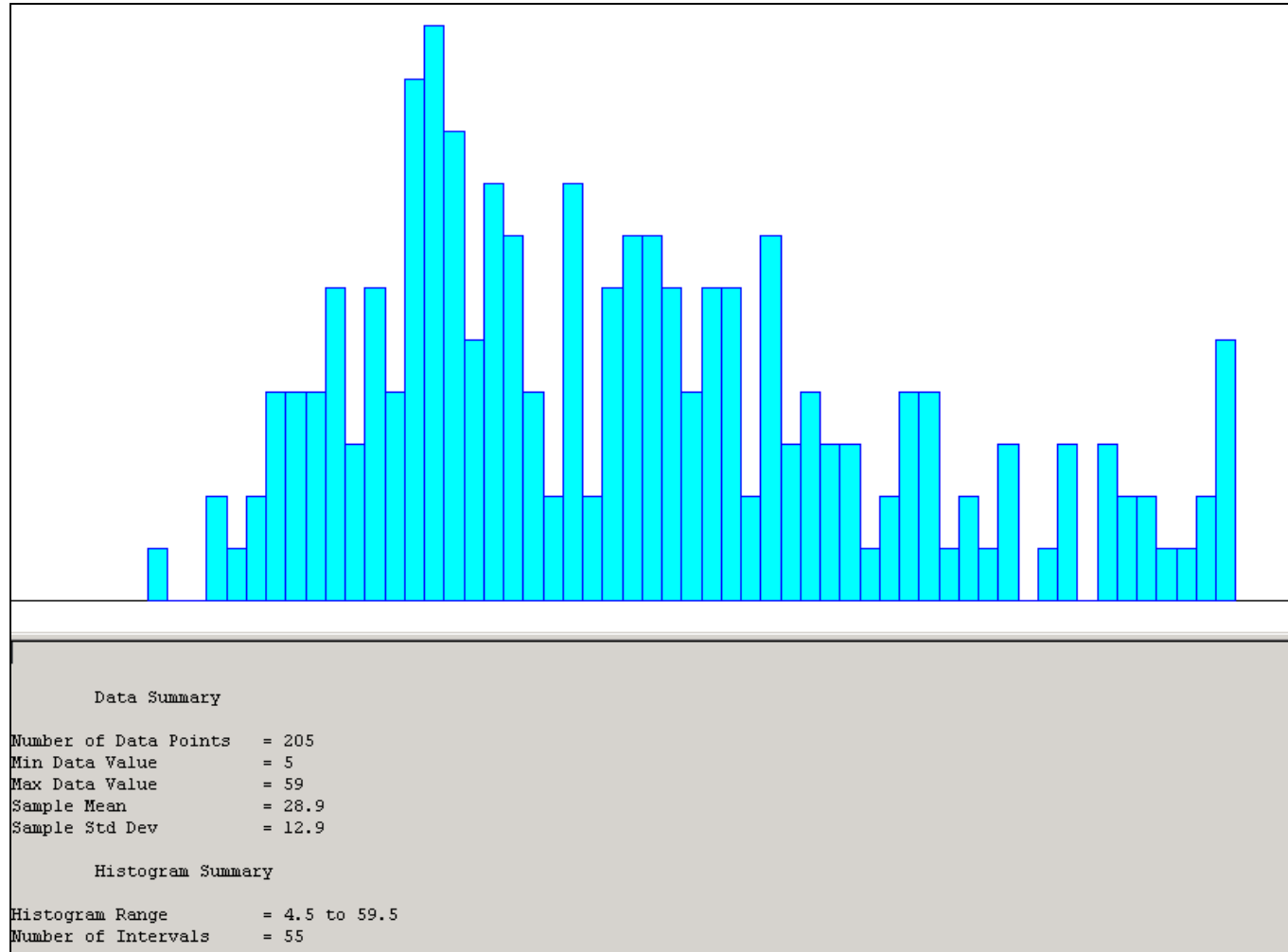
# Model input data

- On-line data
  - Direct observation, time study
  - Check sheets
  - Analysis of similar process
  - Review of manual documentation
  - Short-term automated data collection methods
- 
- Example: Lab test turn around time

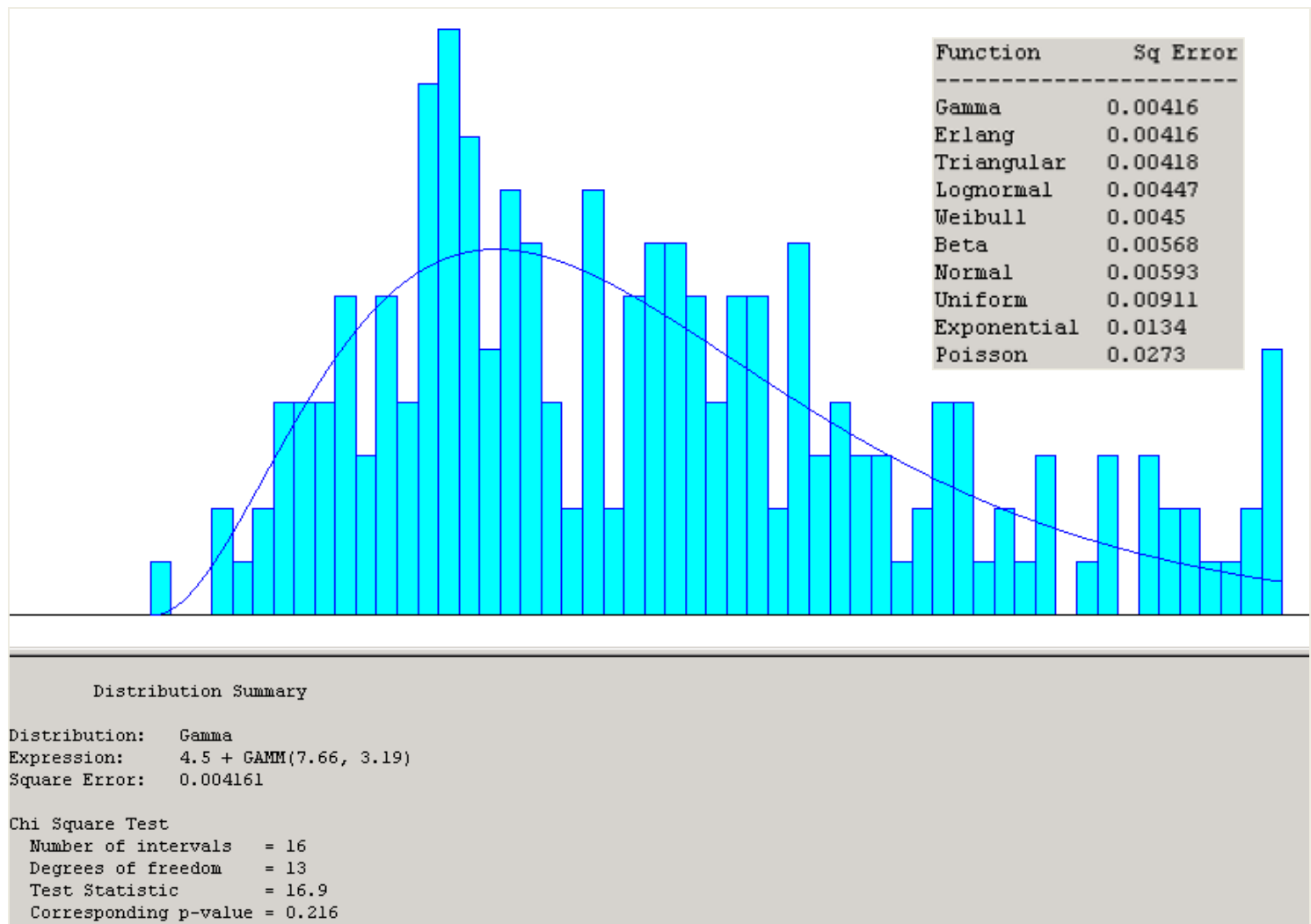
# Input data example: CBC turn-around time

| Test Code: CBC                  |              |             |                  |                     |
|---------------------------------|--------------|-------------|------------------|---------------------|
| Test Name: Complete Blood Count |              |             |                  |                     |
| Collection Time                 | Receive Time | Result Time | Result - Receive | Result - Collection |
| 0000                            | 0031         | 0045        | 14               | 45                  |
| 0001                            | 0012         | 0021        | 9                | 20                  |
| 0001                            | 0011         | 0029        | 18               | 28                  |
| 0001                            | 0010         | 0030        | 20               | 29                  |
| 0001                            | 0018         | 0032        | 14               | 31                  |
| 0005                            | 0023         | 0036        | 13               | 31                  |
| 0008                            | 0022         | 0048        | 26               | 40                  |
| 0010                            | 0030         | 0047        | 17               | 37                  |
| 0013                            | 0039         | 0049        | 10               | 36                  |
| 0035                            | 0039         | 0055        | 16               | 20                  |
| 0100                            | 0113         | 0122        | 9                | 22                  |
| 0102                            | 0123         | 0136        | 13               | 34                  |
| 0120                            | 0136         | 0156        | 20               | 36                  |
| 0124                            | 0133         | 0141        | 8                | 17                  |

# Input data example: CBC data histogram



# Input data example: CBC data – best fit function



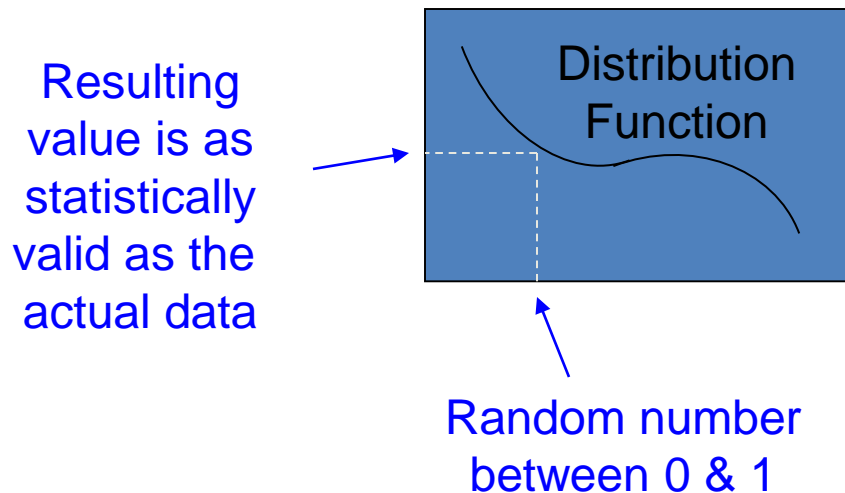


# Input data example: CBC data – use in the model

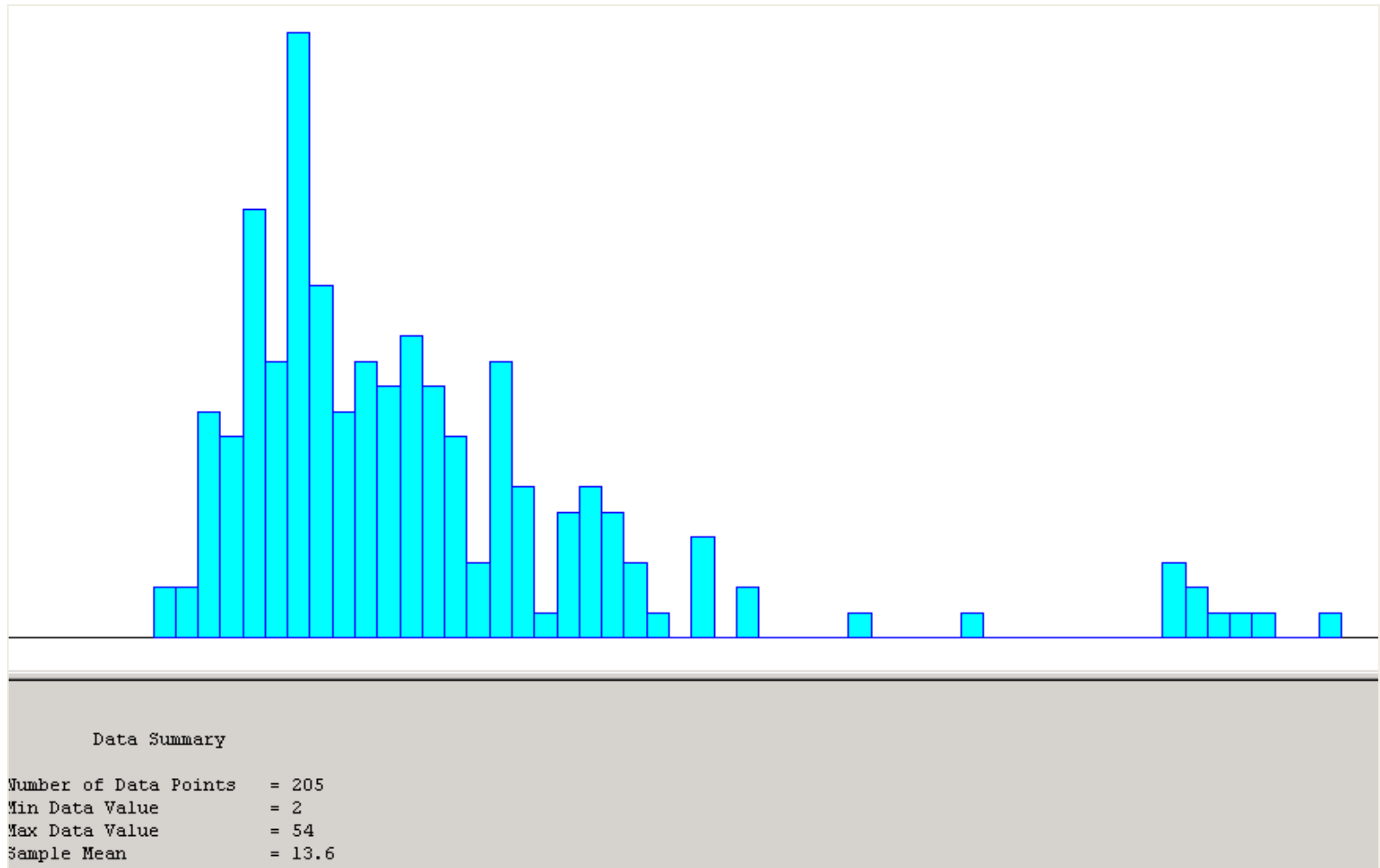
Simulation uses this probability density function  $\{(4.5 + \text{GAMM}(7.66, 3.19))\}$  each time a CBC is performed

Random number (x) drives the generation of a CBC time

Simulated time is statistically equal to actual time

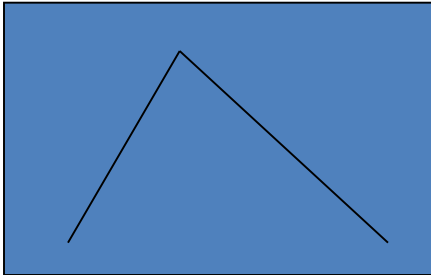


# Input data example: CBC data – bimodal?

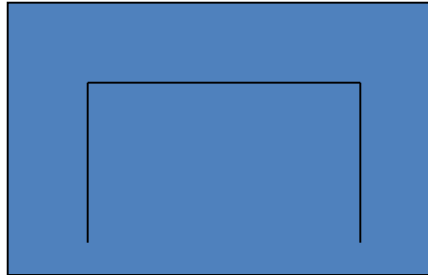


# Distributions: Types

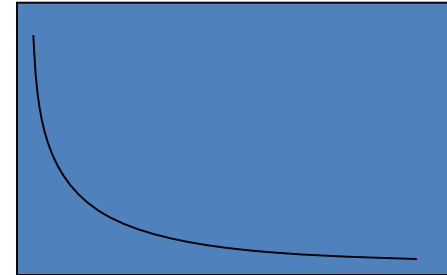
Triangular



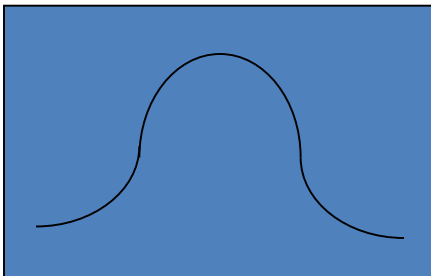
Uniform



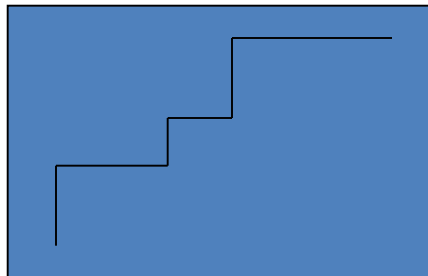
Exponential



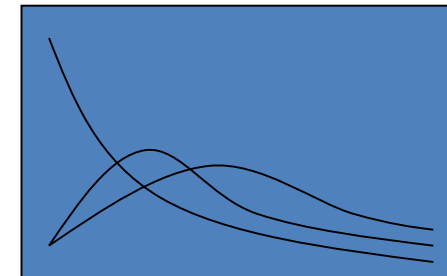
Normal



Discrete



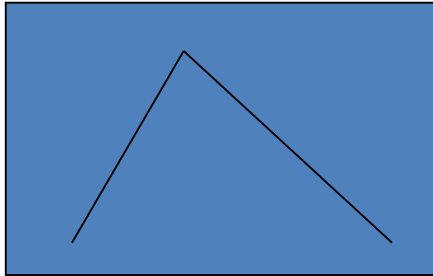
Erlang



Others: Beta, Gamma, Johnson, Weibull, Poisson,  
Continuous, Lognormal, User Defined

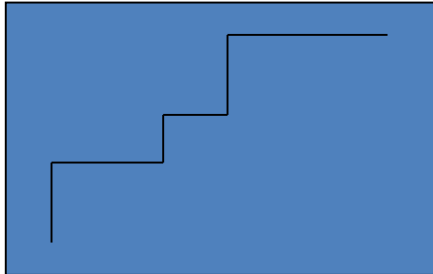
# Distributions: Typical uses

Triangular



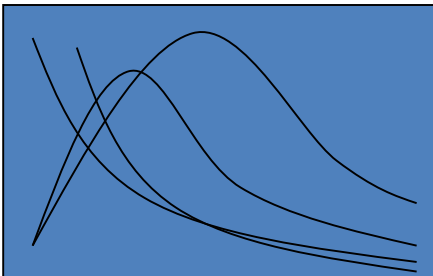
Distribution not known, but can estimate or guess minimum, maximum, and most likely

Discrete



Assignments such as attributes, sequences, batch sizes

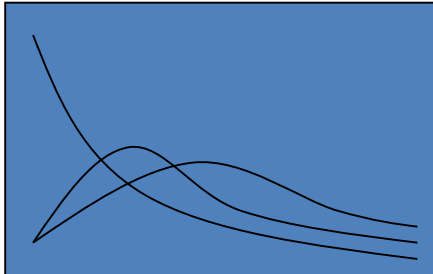
Weibull



Time between failures

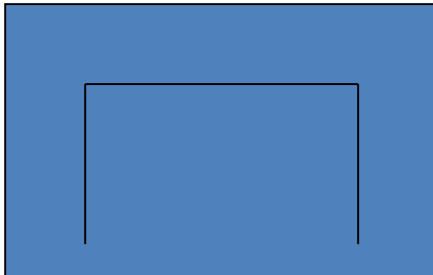
# Distributions: Typical uses

Erlang &  
Gamma



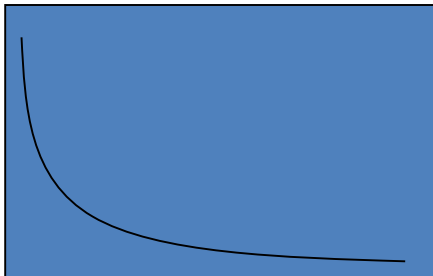
Often used to represent the time it takes to complete a task

Uniform



All values equally likely.  
No information other than range available

Exponential

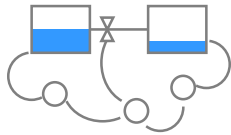


Inter-event times in arrivals  
and breakdowns

# Simulation modeling software

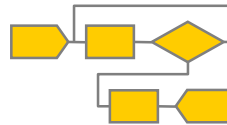
- A partial list of tools and the modeling approaches they support

## System dynamics



AnyLogic  
iThink  
PowerSim  
Stella  
VenSim

## Discrete event modeling



AnyLogic  
Arena  
AutoMod  
Enterprise Dynamics  
ExtendSim  
FlexSim  
PROMODEL  
Simio  
SimProcess

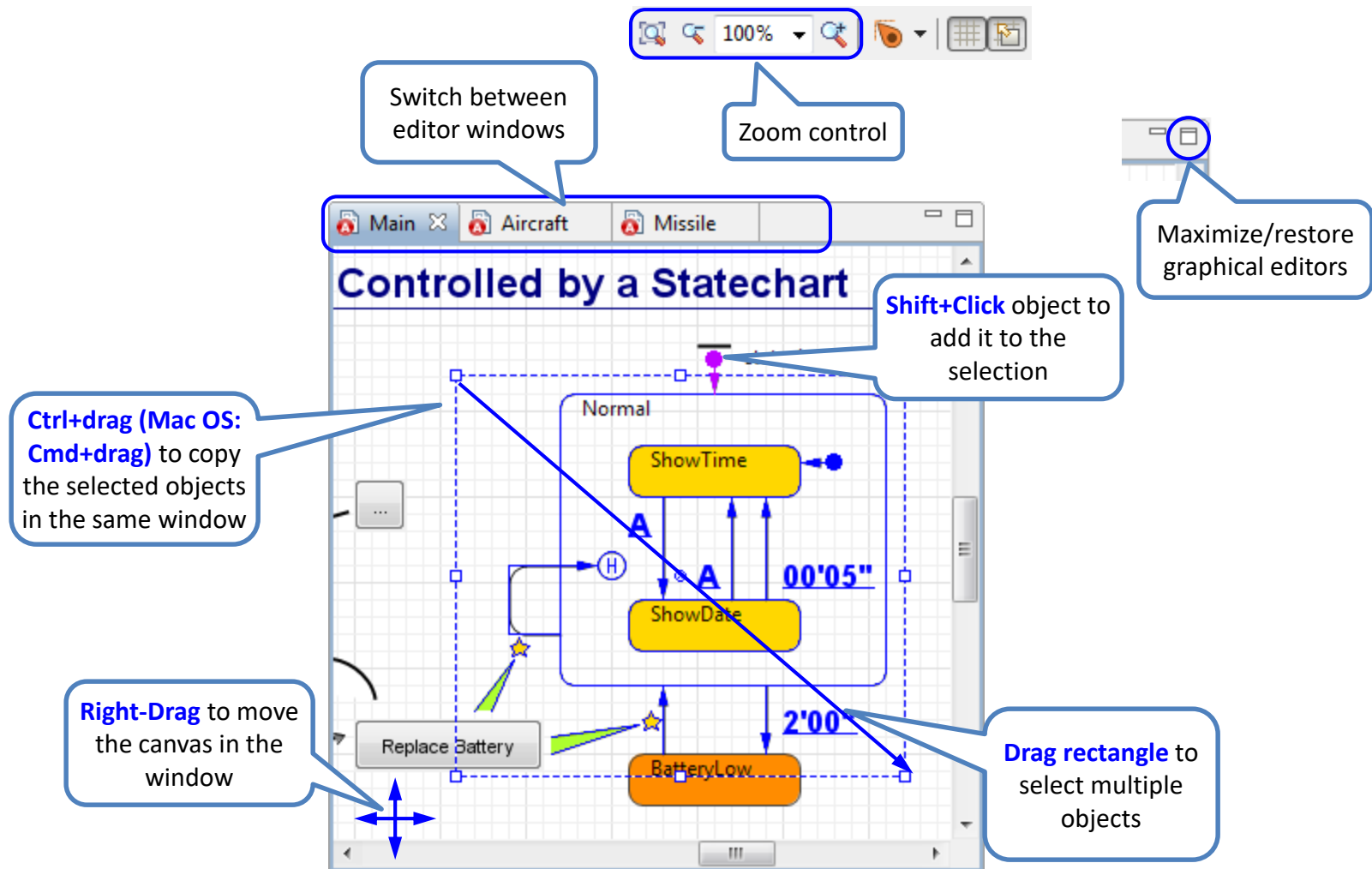
## Agent based modeling



AnyLogic  
Academic tools:  
ASCAPE  
NetLogo  
RePast  
Swarm

# The Model Development Environment

# Graphical Editor – Selecting & Copying





# Properties view

- The **Properties** view allows you to view and modify the selected item's properties (you select an item by clicking it in the graphical editor, or in **Projects** view).

## Legend:

= Static value

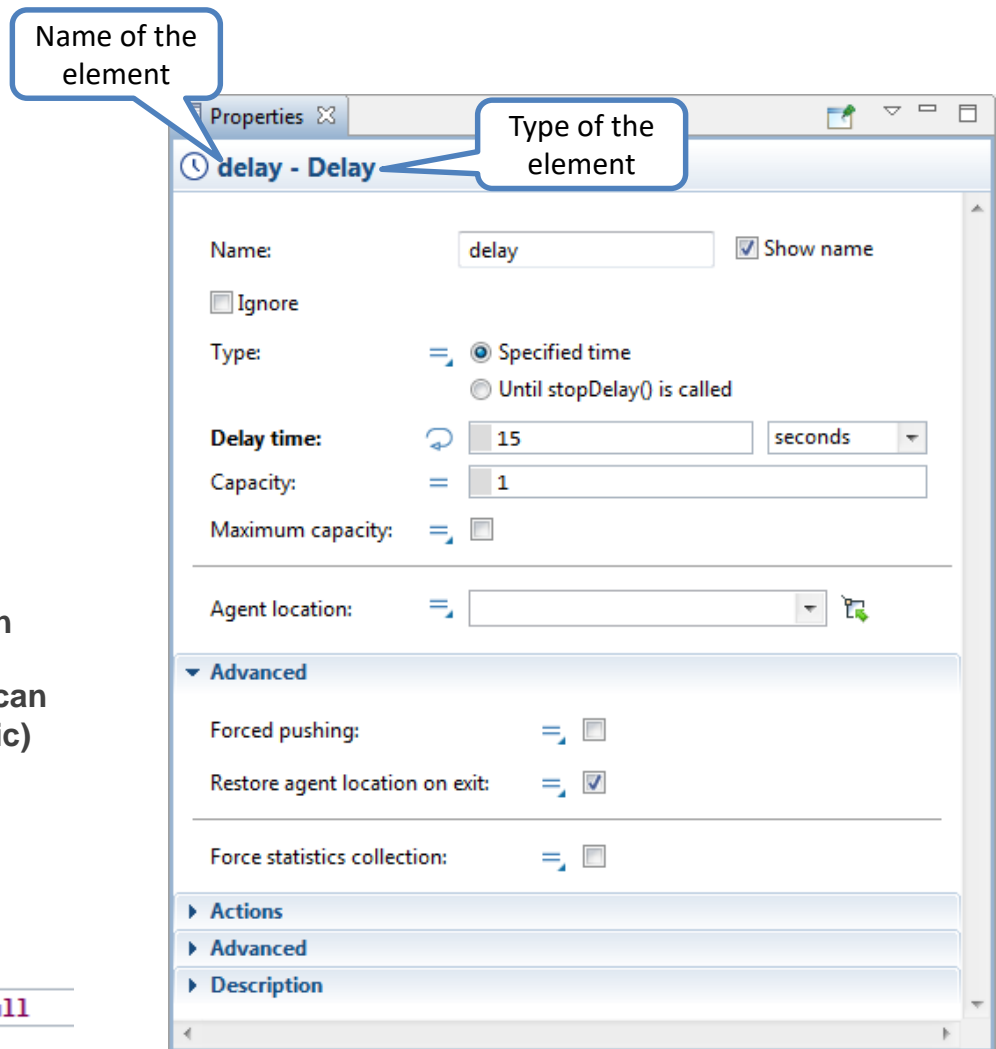
↻ Dynamically evaluated expression

≡ ← Small triangle indicates that you can switch between design-time (static) and run-time (dynamic) values

Fill color: = red



Fill color: ↻ `line.isVisible() ? red : null`



# Running the Model

The image shows the AnyLogic Professional software interface. The top window is the main workspace, and the bottom window is the presentation window for the 'Bass Diffusion' simulation.

**1. Click Run button**

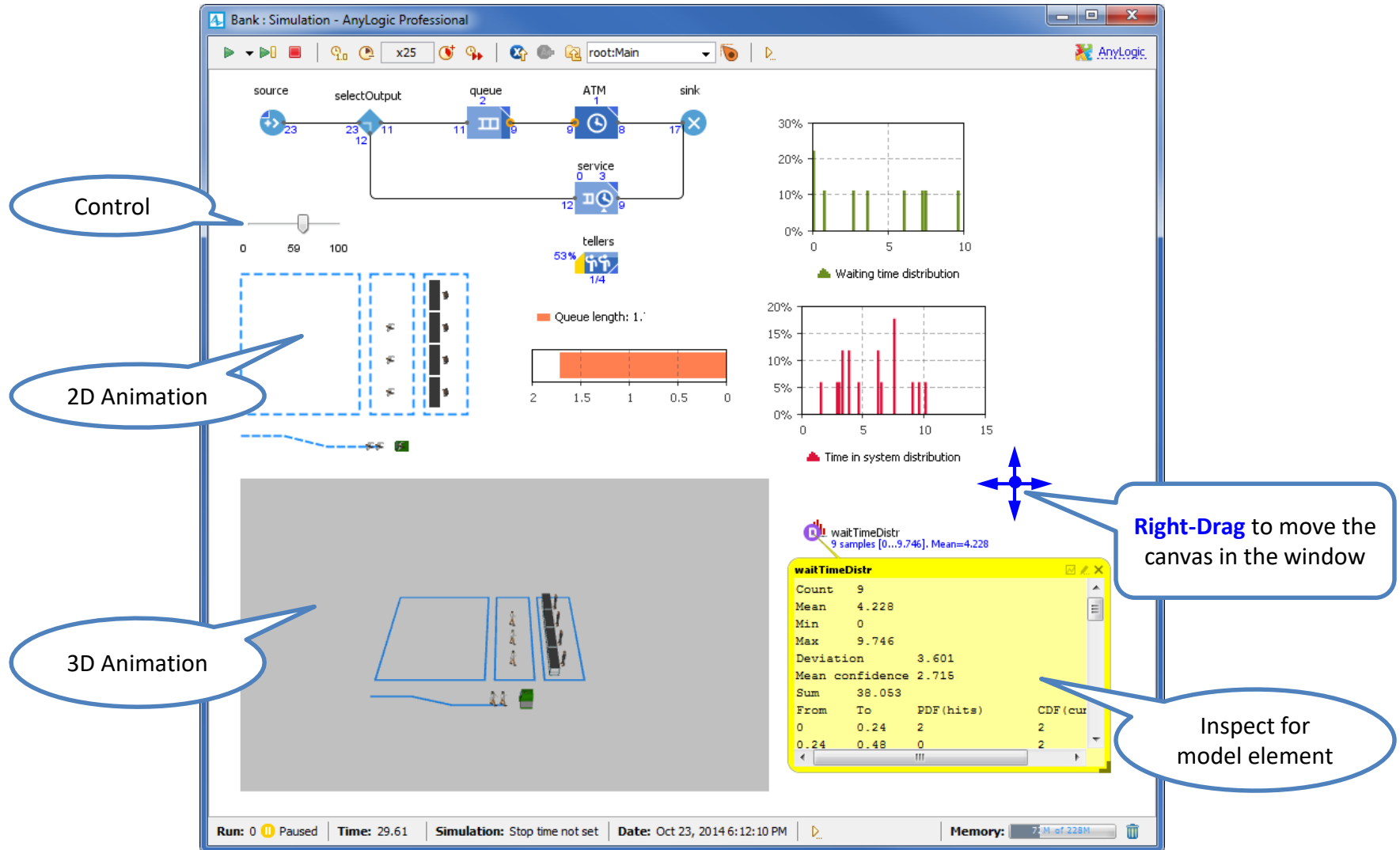
**2. Choose the experiment to run**

**3. You will see the **Presentation window** showing presentation designed for the experiment**

**4. Click the button to run the model and switch to **Main** agent type**

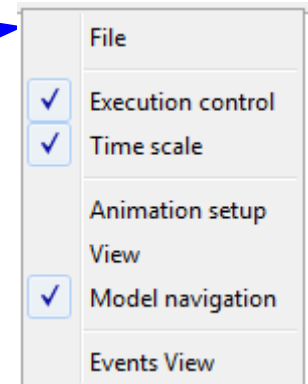
The presentation window displays the title 'Bass Diffusion' and a 'Run' button. The status bar at the bottom indicates the simulation is in 'Idle' state, with 'Run: 0', 'Time: -', 'Simulation: Stop time not set', 'Date: -', and 'Memory: 121M / 228M'.

# Presentation Window



# Major Toolbar Commands

- Toolbars and status bar can be customized



- Execution control

Only one is displayed at a time, depending on the model state

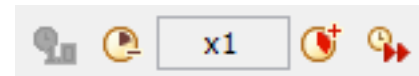
Run from the current state:  
Pause:  
Make a step:  
Terminate execution:



- Time scale

Real Time mode only

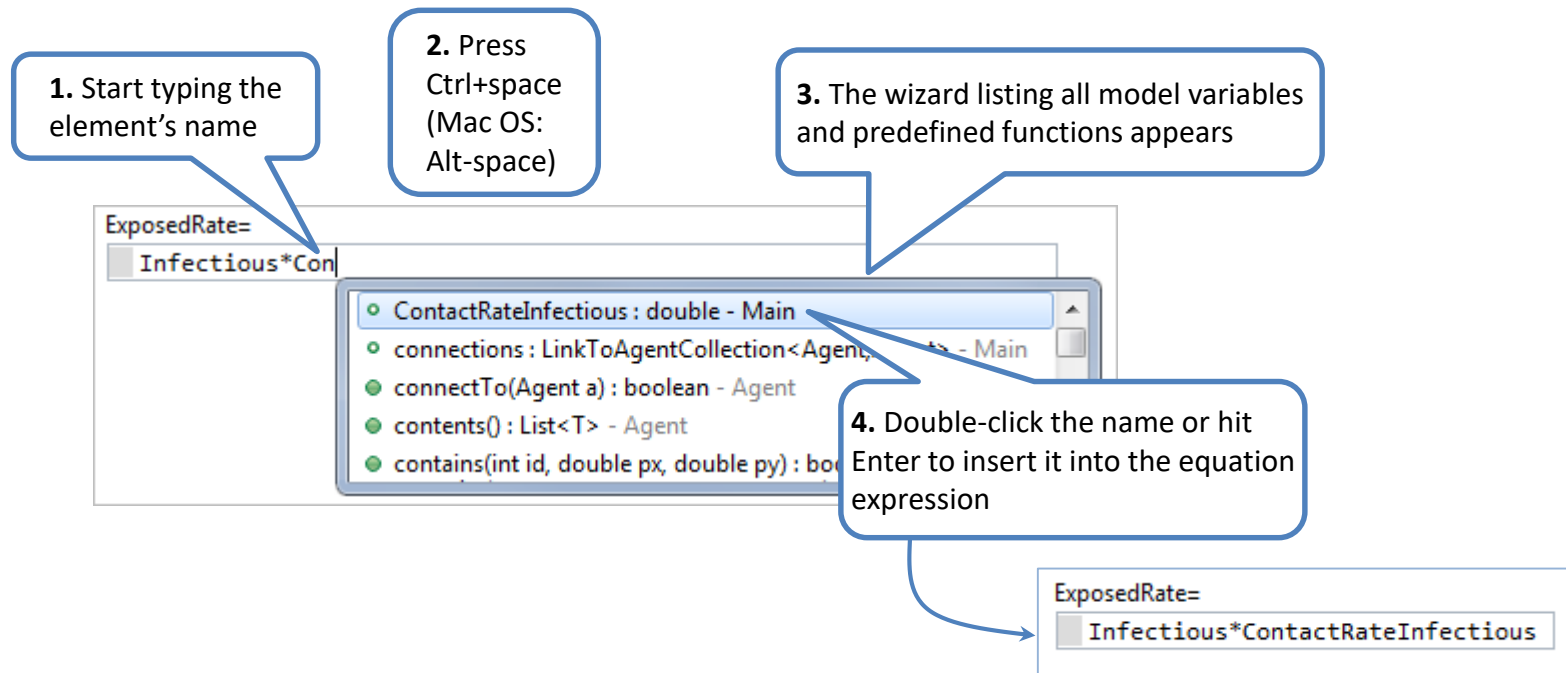
Set real time mode at default scale:  
Decrease execution speed:  
Select execution speed factor:  
Increase execution speed:  
Toggle Real/Virtual time modes:



# Code Completion Master

Intelli-sense mechanism:

The wizard looks as a list, containing variables, parameters, and functions. You can simply select the name in the list, and it will be inserted in the expression automatically.



# Help

AnyLogic Professional

File Edit View Draw Model Tools Help

AnyLogic Help

Welcome

Example Models

Help system supports search mechanism

Search: Go Scope: All topics

Contents

- AnyLogic Help
  - Release Notes
  - Using Help
  - Basic Concepts
  - AnyLogic User Interface
    - AnyLogic UI
    - Welcome page
    - Projects view
    - Palette view
    - Properties view
    - Problems view
    - Other AnyLogic views
  - Working with views
  - Graphical editor
    - Graphical editor
    - Graphical editor. Visible area and
    - Selecting shapes
    - Copying, moving and deleting
    - Moving and zooming the diagram
    - Aligning elements**
    - Diagram grid
    - Simultaneous work with several
  - Java editor
  - AnyLogic toolbars
  - AnyLogic statusbar
- Tutorials
- Library Reference Guides
- FAQ
- AnyLogic Classes and Functions

AnyLogic Help > AnyLogic User Interface > Graphical editor

## Aligning elements

You can align elements in the graphical editor.

To align elements, first, you should [select](#) them in the graphical editor, then right-click (Mac OS: Ctrl+click) the selection and choose the required alignment command from the **Align** submenu.

parameter1

parameter2

Cut Ctrl+X

Copy Ctrl+C

Paste Ctrl+V

Delete Delete

Align

- Horizontal Align Left
- Horizontal Align Center
- Horizontal Align Right
- Vertical Align Top
- Vertical Align Center
- Vertical Align Bottom

Please note that you can align elements of different types: presentation shapes, library objects, parameter, function, database icons, etc.

You can not align statechart and actionchart elements since this may distort their structure and logic.

Let's illustrate all alignment commands by example of three shapes:

Готово

Help also includes:

- Self-paced tutorials,
- Reference Guides on AnyLogic Libraries (Process Modeling, Pedestrian, Rail, ...)
- Java Documentation on all AnyLogic classes and functions

# Discrete Event Modeling

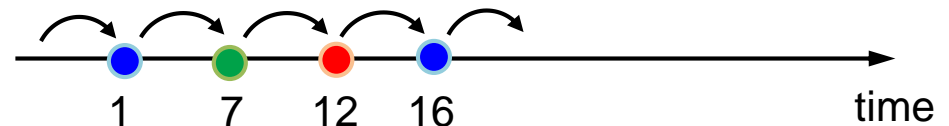
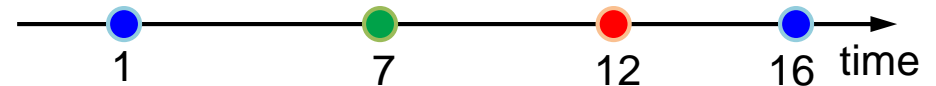
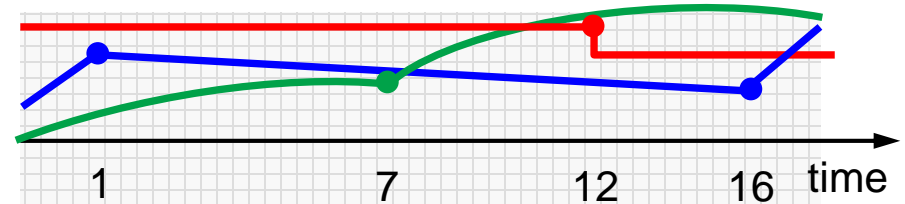
# Event

- We consider only “important moments” in the system’s lifetime, which are called *events*.
  - Any change in the model may happen only as a result of an event
- Examples:
  - Customer arrives at the bank office
  - Bill finishes processing
  - Amount of raw material reaches the minimum level
- Event:
  - Takes zero model time
  - Causes changes in the model
  - May schedule or cancel other events in the future



# Time as event order – Discrete Time

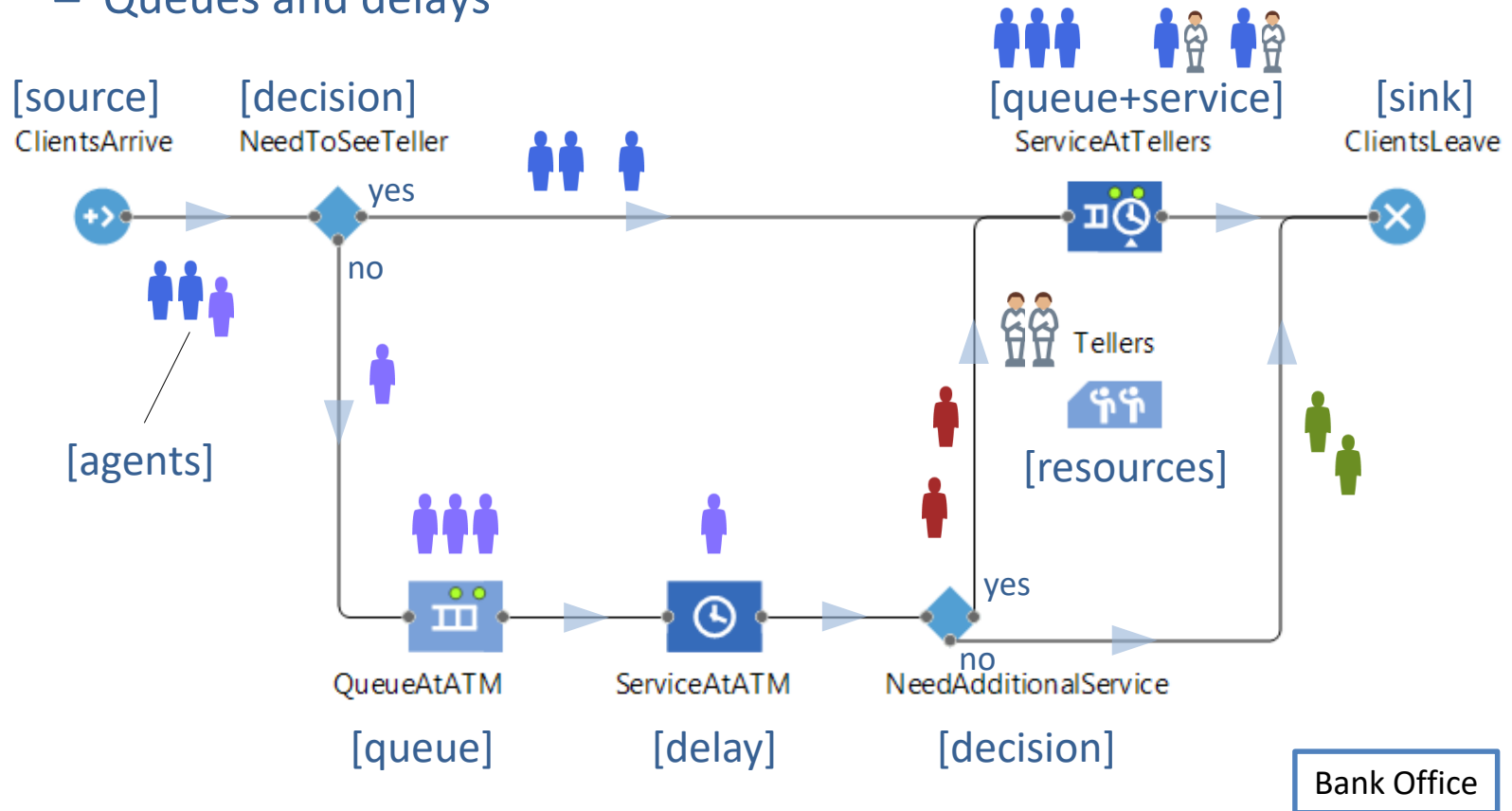
- We consider only a sequence of instant “discrete” events, while nothing happens in between
- No “continuous-time” processes
- Model time “jumps” from one event to another



This is [Discrete Event Modeling](#)

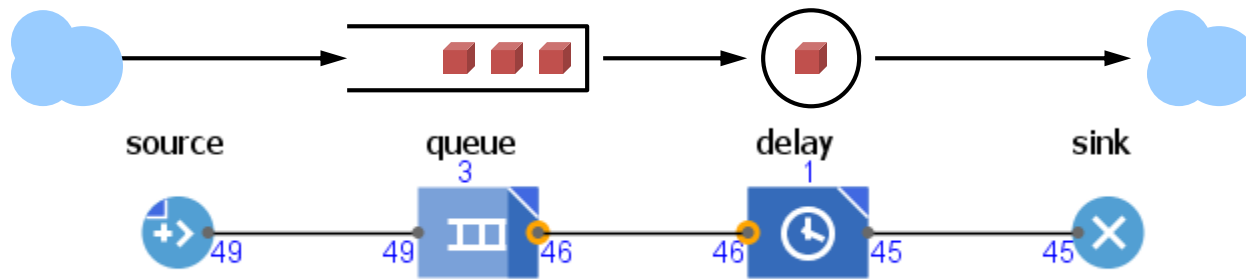
# Discrete event modeling. G. Gordon '60s

- Agents and resources. Flowchart diagram
  - Queues and delays



# The simple process based model

- Define the process with Process Modeling Library blocks with a simple drag and drop



**Arrivals defined by:** Rate

**Arrival rate:** 1

Limited number of arrivals:

New agent: Agent

Location of arrival:

On exit:

**Capacity:** 100

On enter:

On at exit:

On exit:

Enable exit on timeout:

Agent location:

**Delay time:** triangular( 0.5, 1, 1.5 )

**Capacity:** 1







On enter:

On exit:







Agent location:

On enter:







# Process Modeling Library. Essential blocks (1/3)

| Block name    | Icon in graphical editor  | Description  |
|---------------|---|--|
| Source        |    | Generates agents. Is usually a starting point of a process model.  |
| Sink          |    | Disposes incoming agents. Is usually an end point in a process model.  |
| Queue         |    | Stores agents in the specified order.  |
| Delay         |    | Delays agents by the specified delay time.   |
| SelectOutput  |   | Forwards the agent to one of the output ports depending on the condition.  |
| SelectOutput5 |  | Routes the incoming agents to one of the five output ports depending on (probabilistic or deterministic) conditions. |

# Process Modeling Library. Essential blocks (2/3)

| Block name | Icon in graphical editor  | Description   |
|------------|---|---|
| Conveyor   |    | Simulates conveyor. Moves agents at a certain speed, preserving order and space between them. |
| Split      |    | Creates a new agent (copy) of the incoming agent.   |
| Combine    |    | Waits for two agents, then produces a new agent from them.                                    |
| Batch      |    | Accumulates agents, then outputs them contained in a new agent.                               |
| Unbatch    |  | Extracts all agents contained in the incoming agent and outputs them.                         |
| MoveTo     |  | Moves an agent from its current location to new location.                                     |

# Process Modeling Library. Essential blocks (3/3)

| Block name          | Icon in graphical editor  | Description  |
|---------------------|---|--|
| RestrictedAreaStart |    | Using these blocks you can limit the number of agents in a part of flowchart between corresponding <b>RestrictedAreaStart</b> and <b>RestrictedAreaEnd</b> blocks. |
| RestrictedAreaEnd   |    |  |
| TimeMeasureStart    |    | <b>TimeMeasureEnd</b> and <b>TimeMeasureStart</b> compose a pair of blocks measuring the time the agents spend between them.                                       |
| TimeMeasureEnd      |    |  |
| Exit                |  | Takes the incoming agents out of the process flow and lets the user to specify what to do with them.   |
| Enter               |  | Inserts the (already existing) agents into a particular point of the process model.  |

# Parameters of Process Modeling Library blocks

- Simple static parameters:

= Evaluated **once**, but may be changed during the model execution

- Dynamically evaluated expressions (dynamic parameters):

Evaluated **each time they are needed**, e.g.

↻ each time the delay time, the speed or other property of an agent needs to be obtained

The corresponding agent is accessible as “agent”, etc.

- Dynamically executed code pieces (code parameters):

☰ Evaluated **each time a certain event occurs** at the object: the agent enters/exits it, conveyor stops, etc.

Capacity =

Delay time ↻

Condition ↻

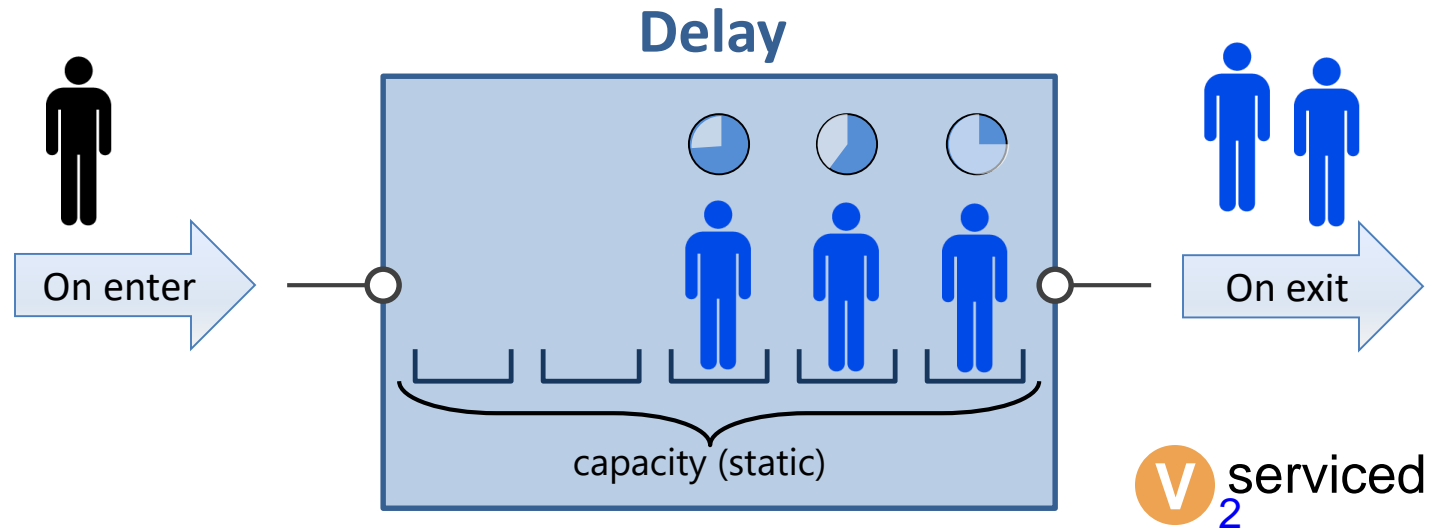
Speed ↻

## ▼ Actions

On exit ☰

On enter ☰

# Parameters. Examples



Capacity: = 5

Delay time: ↻ uniform( 2, 10 )

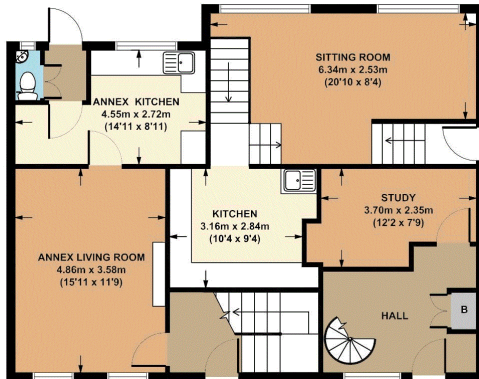
On enter: agent.setColor(blue );

On exit: serviced++;

- To change a value of the static `capacity` parameter, call: `delay.set_capacity(20)` ;
- You **add a semicolon** at the end of each line of Java code in **code parameter**
- You **do not add a semicolon** to the end of **static/dynamic parameter** expression









# Resources



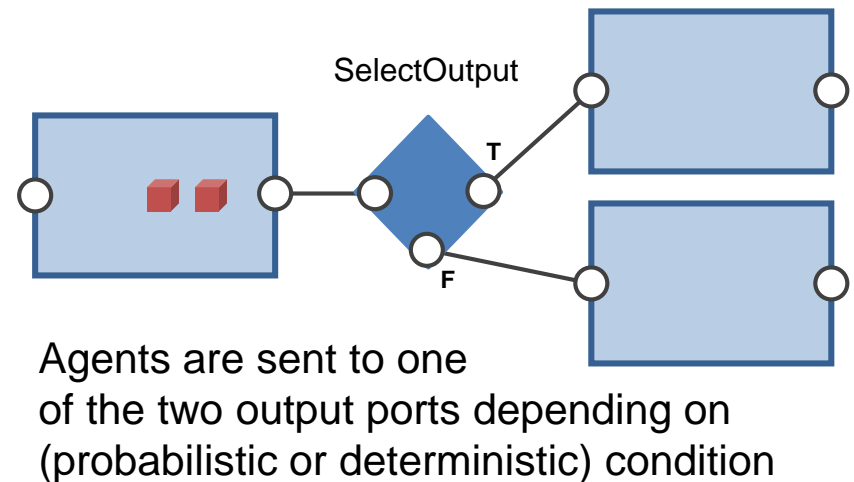
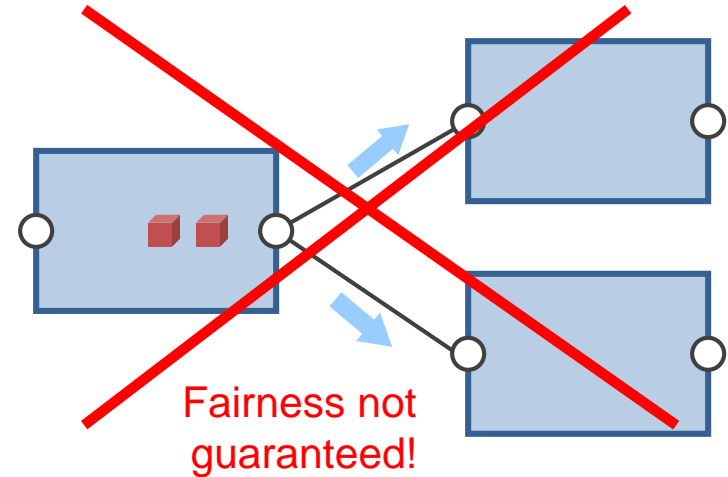
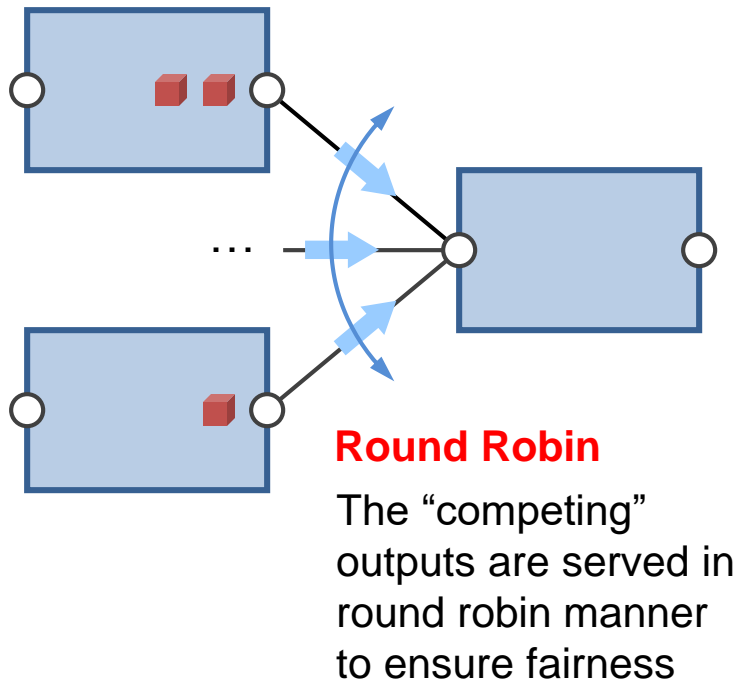
# Resource types

- Static (can't move and can't be moved): a room, a non-portable equipment, a passage, etc.
- Portable (can't move on their own, but can be moved): a wheelchair, portable xRay, etc.
- Moving (can move, carry portable resources): a doctor, a nurse, a forklift truck, etc.

# PML blocks associated with resources

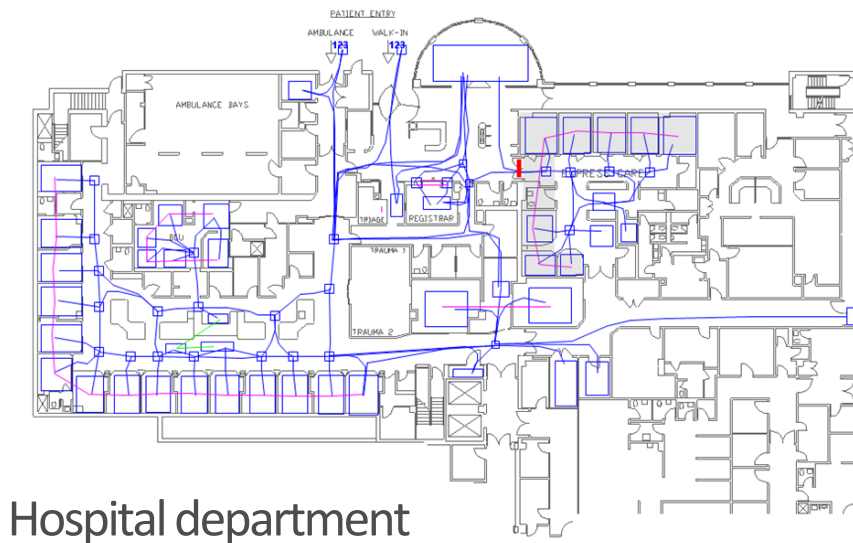
| Block name     | Icon in graphical editor  | Description   |
|----------------|---|---|
| ResourcePool   |    | Defines a set of resources of the specified type: how many resources of this type exist in the system, what are they attributes.                        |
| Seize          |    | Seizes the number of units of the specified resource required by the agent.   |
| Release        |    | Releases resource units previously seized by the agent.   |
| Service        |    | Seizes resource units for the agent, delays it, and releases the seized units. The block itself is a <b>Seize – Delay – Release</b> sequence of blocks. |
| Assembler      |   | Assembles a certain number of agents from several sources (5 or less) into a single agent.  |
| ResourceSendTo |  | Sends a set of portable and/or moving resources to a specified location.  |

# Agent flow at N:1 and 1:N connections

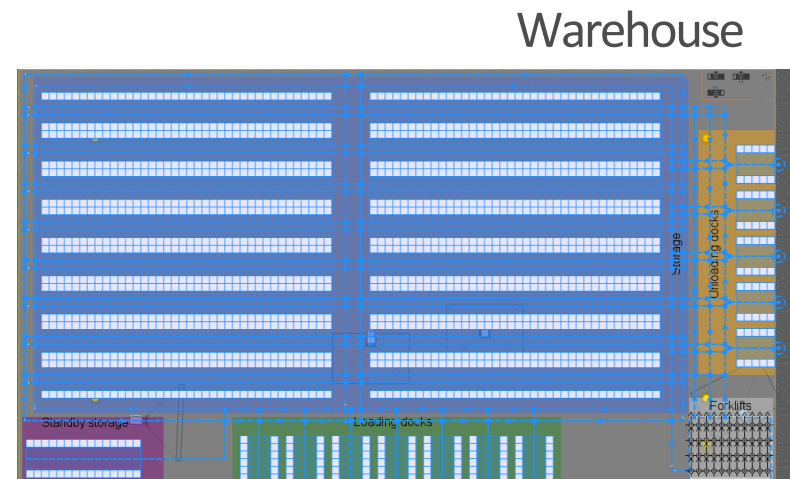


# Network-based modeling

- The Process Modeling Library provides better support for certain types of problems where layout is important
  - There is a network of locations and paths between them
  - Agents and resources move along the paths, route lengths matter



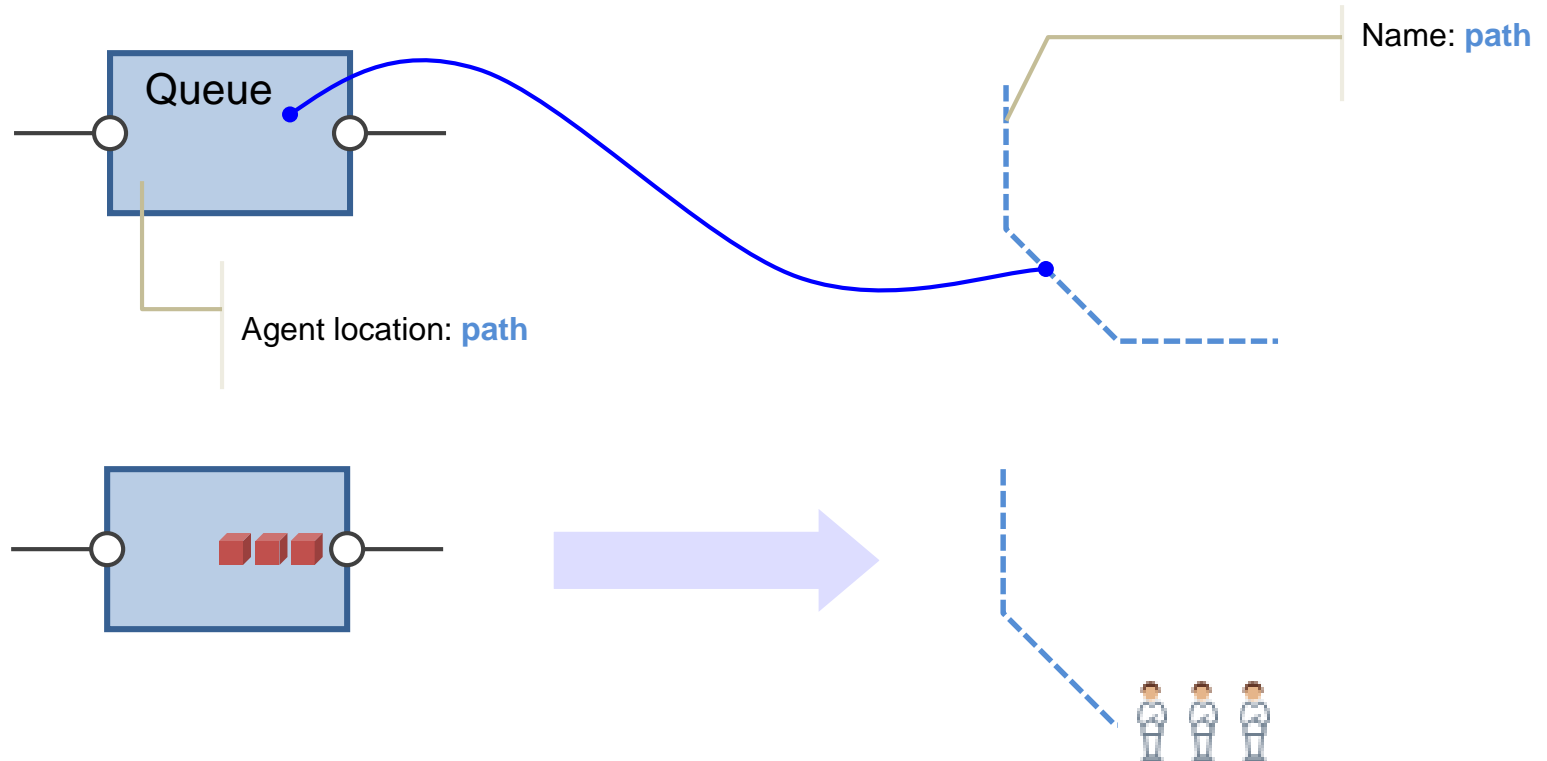
Hospital department



Warehouse

# Animation of Process Modeling Library models

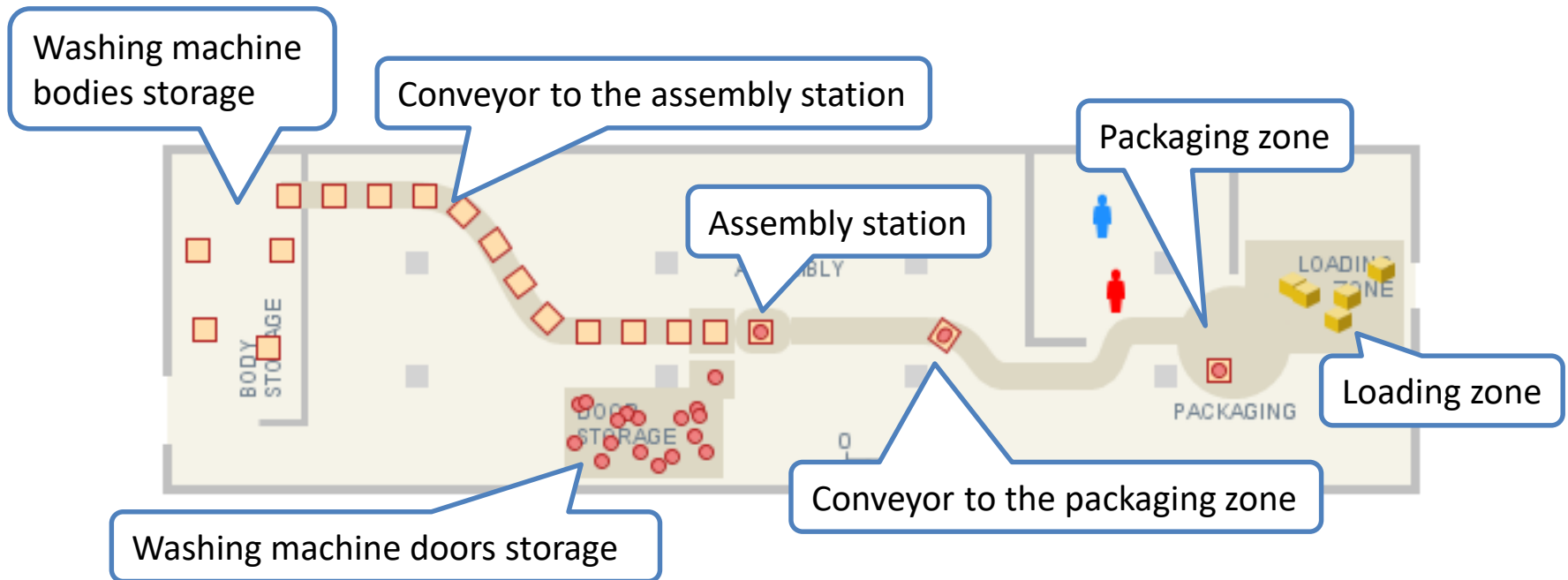
You can associate any object that contains agents with a **space markup** shape (**path** or **node**) defining the location of agent animations.



# The Factory Model



# The Factory Model

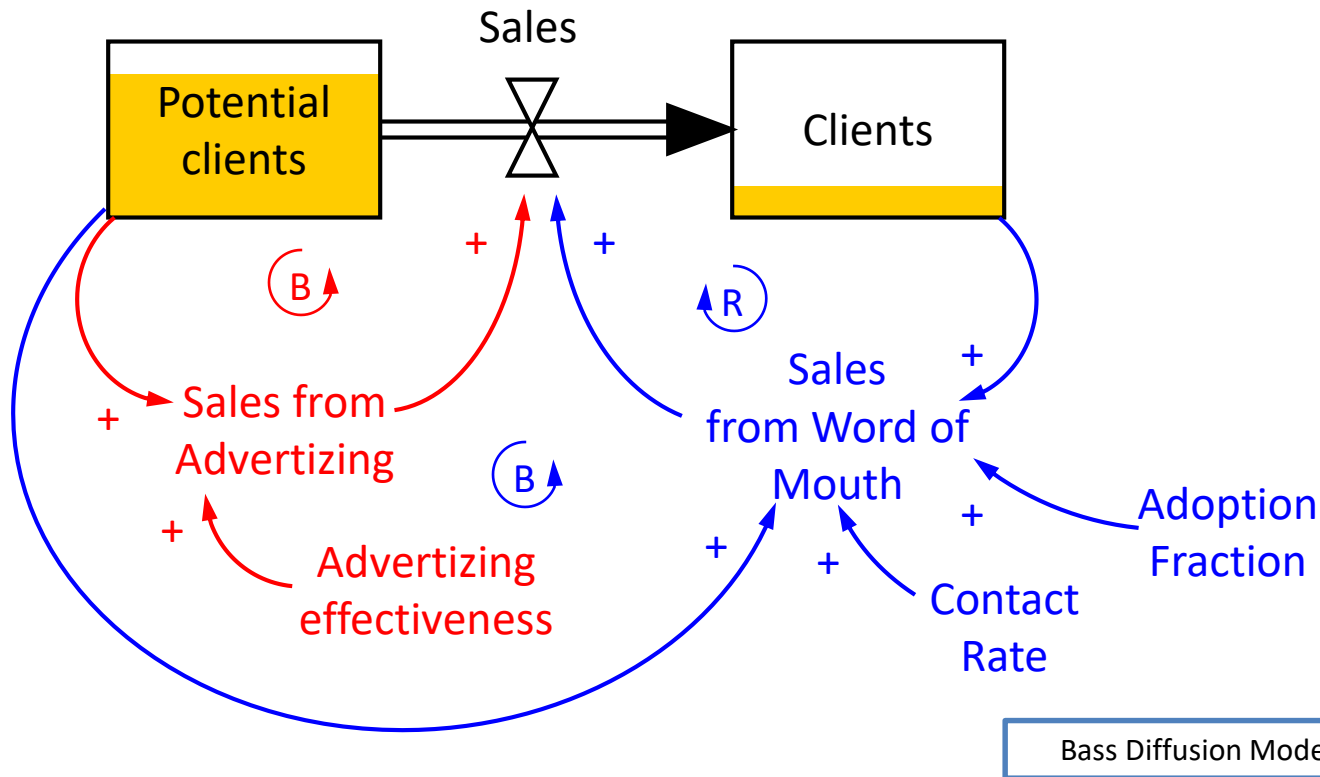




# System Dynamics Modeling

# System Dynamics Jay Forrester '50s

- Stocks, flows
  - Interacting feedback loops



# System Dynamics Jay Forrester '50s

- Stocks, flows
  - Interacting feedback loops

## The equivalent mathematical model:

$$d(\text{Potential clients})/dt = -\text{Sales}$$

$$d(\text{Clients})/dt = \text{Sales}$$

$$\text{Sales} = \text{Sales from Advertizing} + \text{Sales from Word of Mouth}$$

$$\text{Sales from Advertizing} = \text{Potential clients} * \text{Advertizing effectiveness}$$

$$\begin{aligned} \text{Sales from Word of Mouth} = & \\ & \text{Clients} * \text{Contact Rate} * \\ & \left( \text{Potential clients} / (\text{Potential clients} + \text{Clients}) \right) * \text{Adoption Fraction} \end{aligned}$$

Bass Diffusion Model

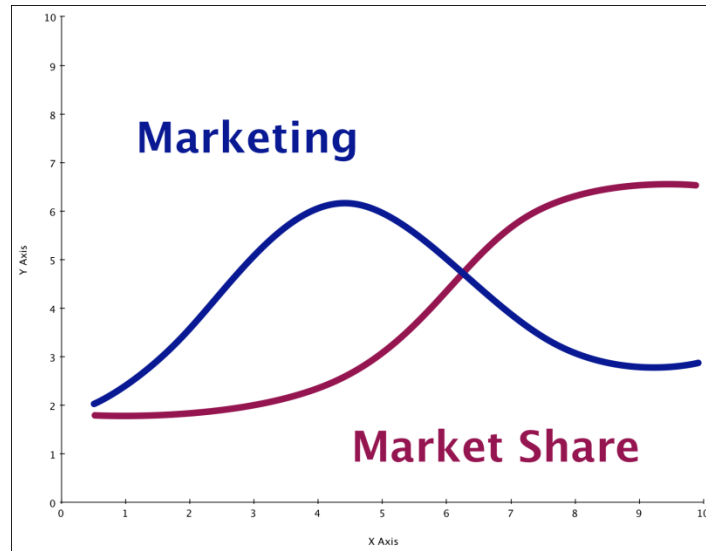
# System Dynamics excels at certain things...



## Cause and Effect

- Representing Causality and relationships
- System dynamics allow you to represent non-physical relationships too
  - *Morale -> Productivity, Advertising -> Perception,*

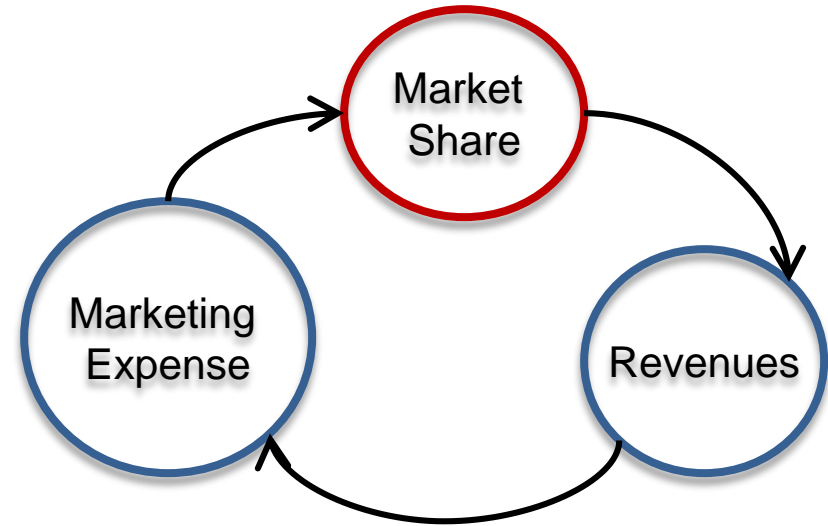
# System Dynamics excels at certain things...



## Delays

- It takes time for certain effects
- This can be from the nature of the elasticity between variables or from the effects of other mitigating effects
  - *Advertising -> Perception, Actions -> Reputation, Fame -> Perception*

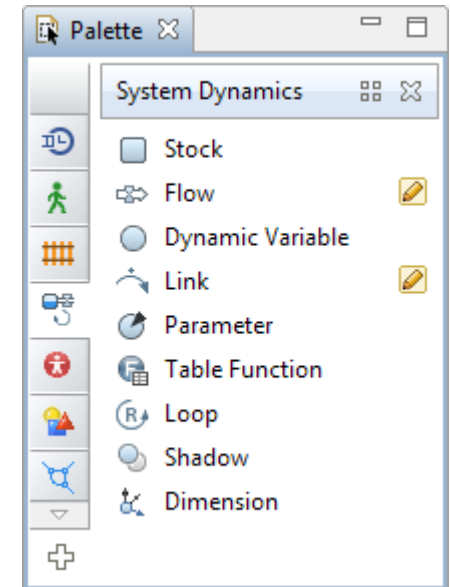
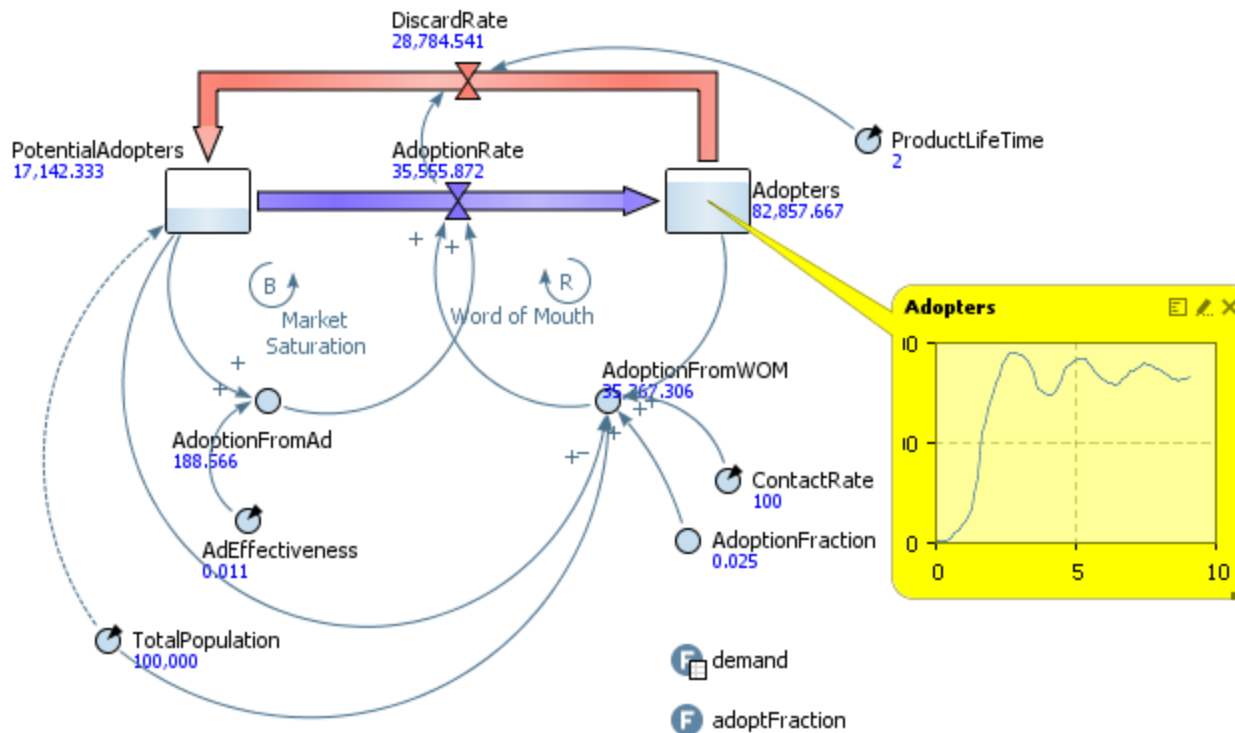
# System Dynamics excels at certain things...



## Feedback Effects

- “Practically” unique to System Dynamics, but common in the real world
- A logic error in excel
- Reinforcing Feedback Loops and Correcting Feedback

# Stock & flow elements



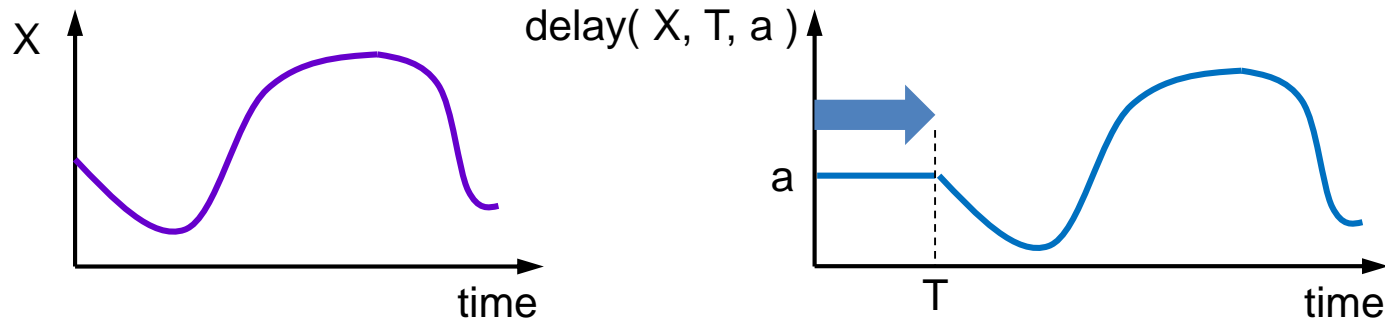
# Built-in functions

## Mathematical functions

`abs(x)` `cos(x)` `exp(x)` `floor(x)` `limit(min,x,max)` `log(x)`  
`max(a,b)` `min(a,b)` `pow(x)` `round(x)` `sin(x)` `sqrt(x)` `tan(x)` ...

## Special system dynamics functions

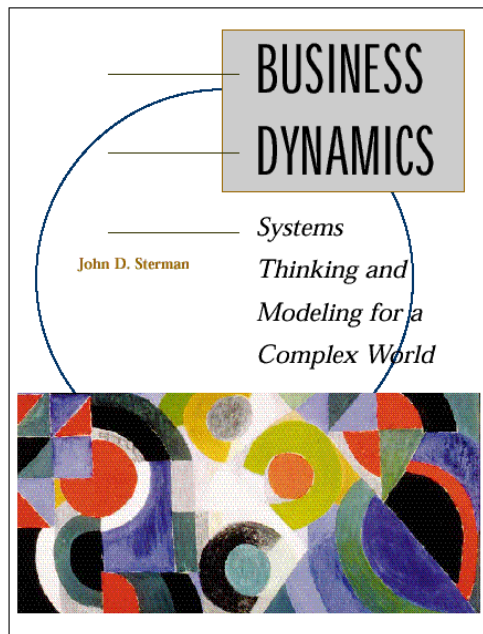
`delay()` `delay1()` `delay3()` `delayInformation()`  
`delayMaterial()` `forecast()` `npv()` `npve()` `smooth()` `ramp()`  
`smooth3()` `trend()` ...



See full list of functions in AnyLogic Help -> Advanced Modeling with Java -> AnyLogic functions -> System dynamics functions



# The Sacred Book of System Dynamics Modeler



John Sterman

“Business Dynamics:  
Systems Thinking and Modeling  
for a Complex World”

2000. McGraw Hill, 1008 pages

<http://www.anylogic.com/business-dynamics-book-models>

[What's New in AnyLogic](#) [Professional Features](#) [Example Models](#) [Ask Question/Get Support](#)

Examples (101)

Models from 'The Big Book of Simulation Modeling' (1)

How-To Models (91)

**Models from the 'Business Dynamics' Book (50)**

[All models \(50\)](#)

[Chapters 4-8 \(6\)](#)

[Chapter 9 \(9\)](#)

[Chapters 10-11 \(6\)](#)

[Chapter 12 \(5\)](#)

[Chapter 13 \(3\)](#)

[Chapters 15-16 \(2\)](#)

[Chapter 17 \(3\)](#)

[Chapter 18 \(5\)](#)

[Chapter 19 \(3\)](#)

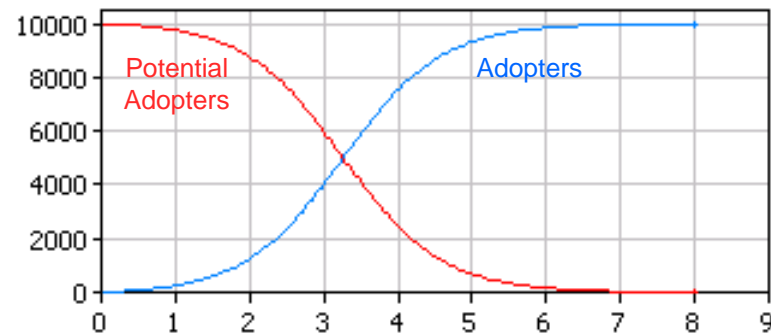
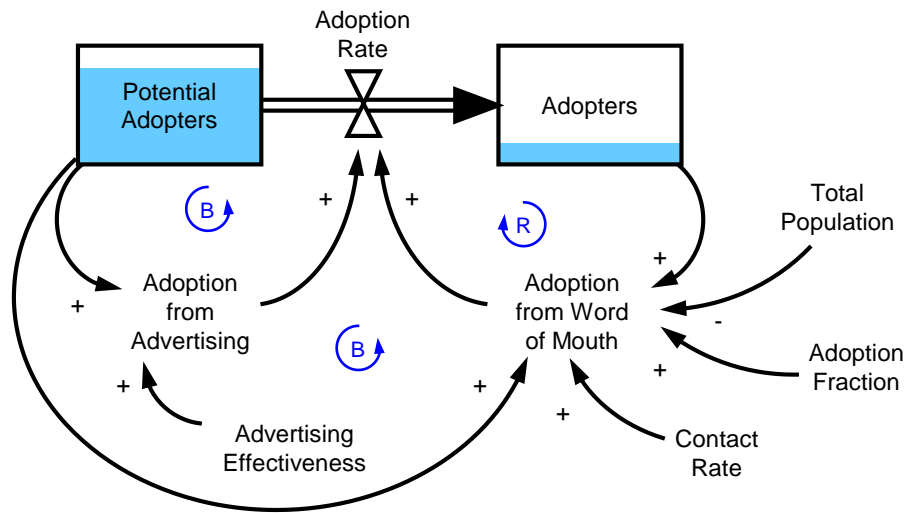
[Chapters 20-21 \(4\)](#)

[Appendices A and B \(4\)](#)

## 'Business Dynamics' Book Models

|  |                                       |   |  |
|--|---------------------------------------|---|--|
| <a href="#">Adaptive Exp Random Walk</a> | <a href="#">Adaptive Expectations</a> | <a href="#">Bass Model</a>                | <a href="#">Bass Repeat Purch Flow</a> |
| <a href="#">Bass with Discards</a>       | <a href="#">Capital Labor Coflow</a>  | <a href="#">Capital Vintaging Coflow</a>  | <a href="#">Commodity1</a>             |
| <a href="#">Faculty Aging Chain</a>      | <a href="#">First Order Neg FB</a>    | <a href="#">First Order Neg with Goal</a> | <a href="#">First Order Pos FB</a>     |
| <a href="#">Floating Goals</a>           | <a href="#">Hillclimb</a>             | <a href="#">Hiring Chain 1</a>            | <a href="#">Inv-WF Noise Switch</a>    |
| <a href="#">Inv-WF with Noise</a>        | <a href="#">Labor Learning Curve</a>  | <a href="#">Labor w Layoffs</a>           | <a href="#">Linear Population</a>      |
| <a href="#">Logistic Model</a>           | <a href="#">Market Growth 1</a>       | <a href="#">Multiplier Simul Eqns</a>     | <a href="#">Network Effect</a>         |
| <a href="#">Nonlinear Polya Process</a>  | <a href="#">Nonlinear Population</a>  | <a href="#">Nonlinear Smoothing</a>       | <a href="#">Pink Noise</a>             |
| <a href="#">Pink Noise Normal</a>        | <a href="#">Polya Process</a>         | <a href="#">Pop and Carrying Capacity</a> | <a href="#">Population Model</a>       |
| <a href="#">Price Discovery</a>          | <a href="#">Price Sector</a>          | <a href="#">Richards Model</a>            | <a href="#">SI Innovation Model</a>    |
| <a href="#">SI Model</a>                 | <a href="#">SIR Model</a>             | <a href="#">SIR Model Threshold</a>       | <a href="#">Stock Mgt 1st Order</a>    |
| <a href="#">Stock Mgt1</a>               | <a href="#">Stock Mgt2</a>            | <a href="#">Summary Statistics</a>        | <a href="#">TREND</a>                  |
| <a href="#">W2Stage w DD FB</a>          | <a href="#">Widgets</a>               | <a href="#">Widgets w Backlog</a>         | <a href="#">Widgets w Labor</a>        |
| <a href="#">Widgets w Labor and OT</a>   | <a href="#">Widgets w Mat Inv</a>     |   |  |

# Bass Diffusion Model



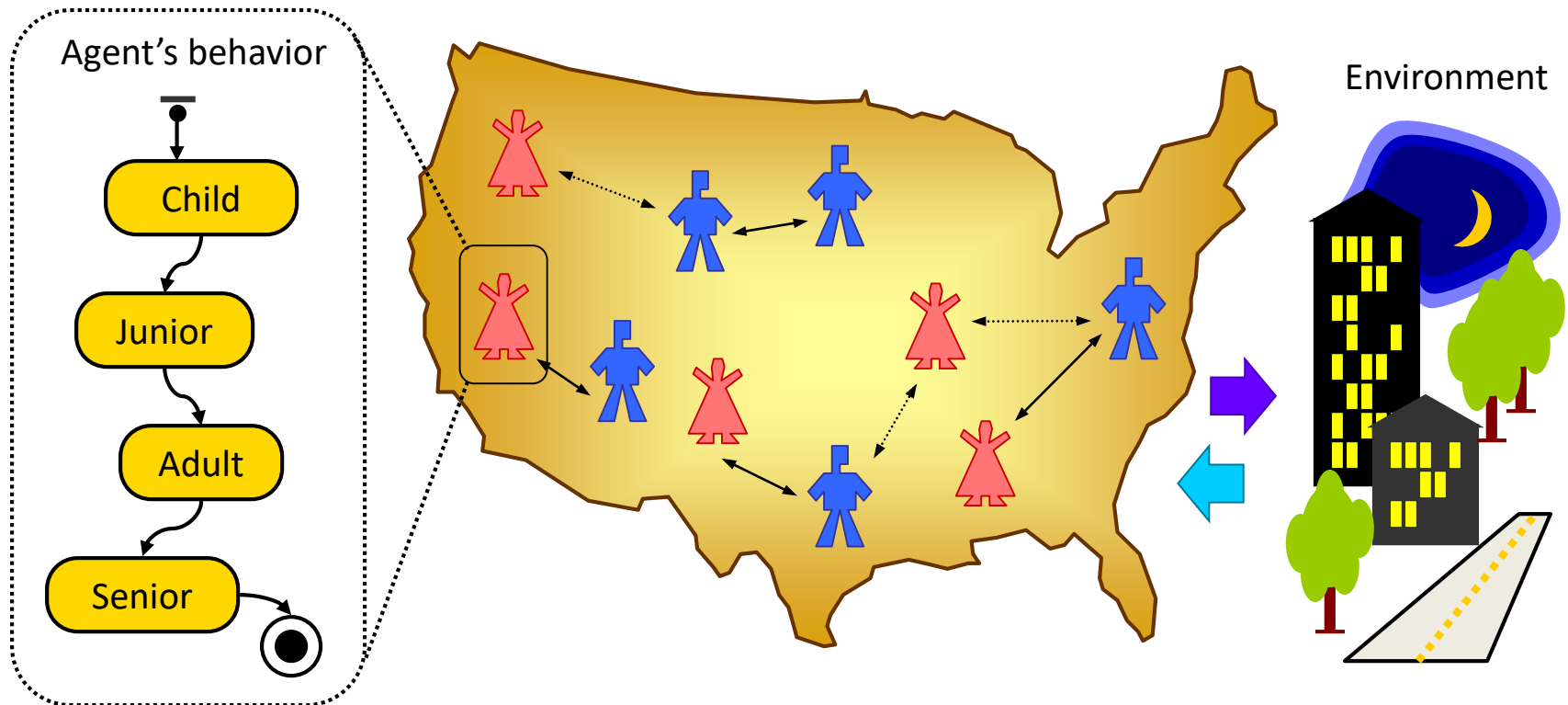
# Bass Diffusion

- SD classical textbook model of product, or innovation diffusion
- A population group is considered to consist of **Potential Adopters** and **Adopters**; all people behave exactly same way
- **Potential Adopters** become **Adopters** at **Adoption Rate** which depends on advertising
- Advertising goes on all the time, and every time unit it converts **Advertising Effectiveness** part of **Potential Adopters** into **Adopters**
- Initially:
  - *Potential Adopters = 100000*
  - *Adopters = 0*
- Parameter values:
  - *Advertising Effectiveness = 0.011*

# Agent Based Modeling

# Agent based modeling

- We focus on individual objects and describe their local behavior, local rules
  - Sometimes, we also model the dynamics of the environment



# Agents can be:

## People:

consumers, habitants, employees,  
patients, doctors, clients, soldiers, ...



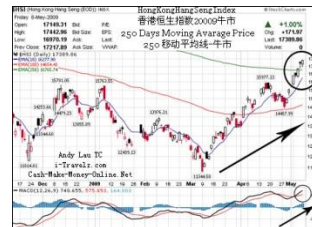
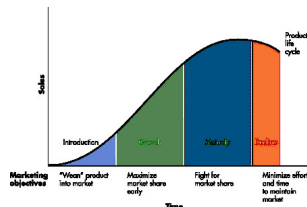
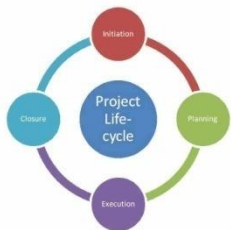
## Vehicles, equipment:

trucks, cars, cranes, aircrafts, rail cars, machines, ...



## Non-material things:

projects, products, innovations, ideas, investments ...

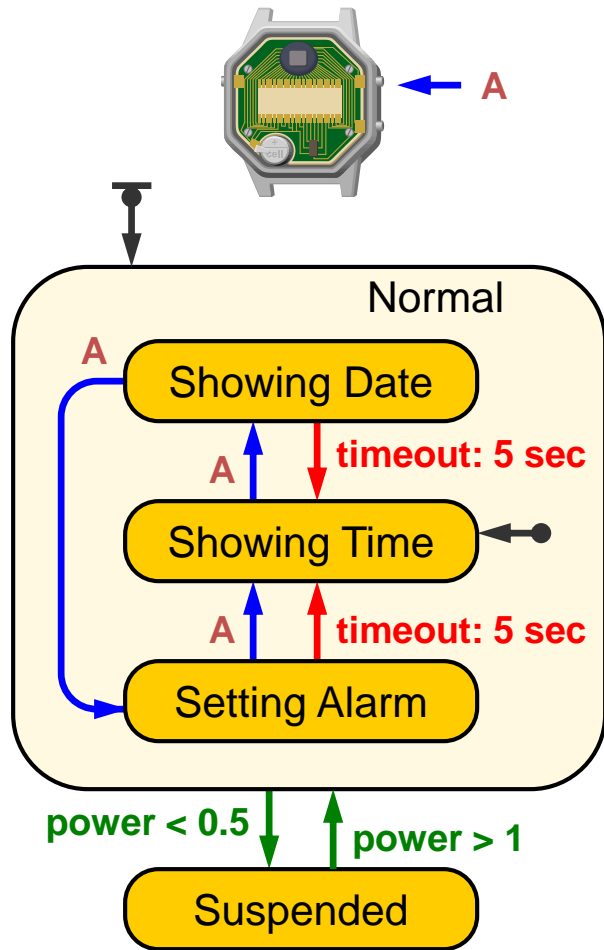


## Organizations:

companies, political parties, countries, ...

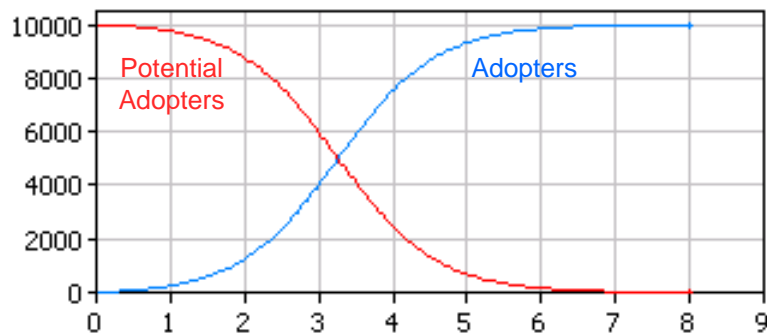
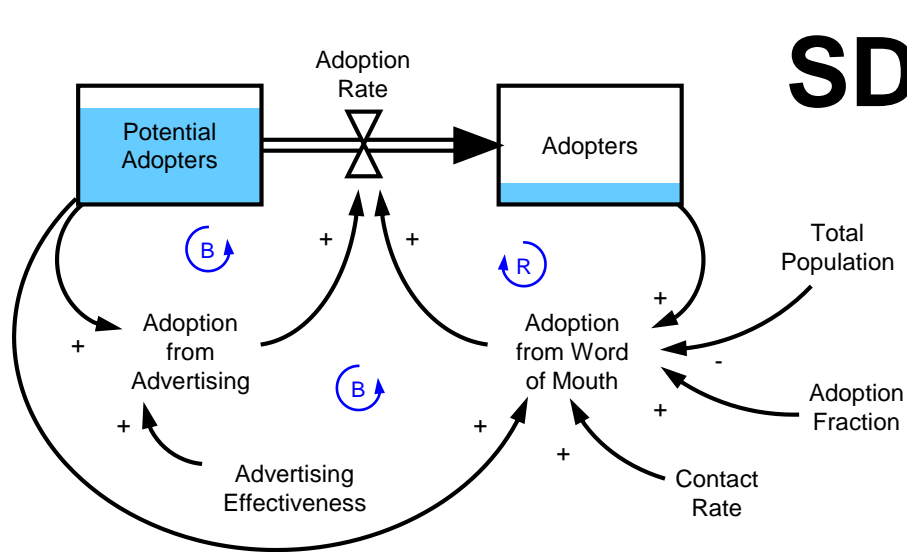


# Statecharts

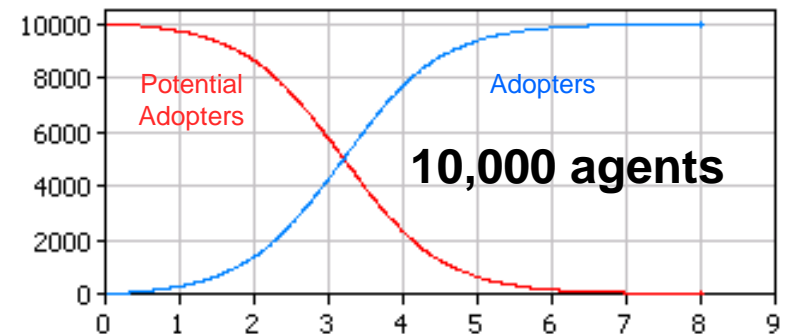
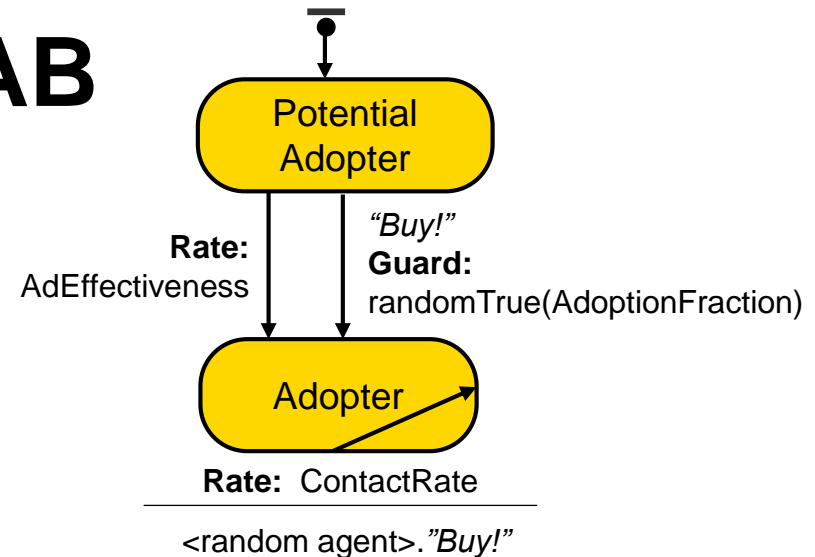


- The most powerful and naturally visual construct
- Statecharts can be used to define:
  - object states / modes of operation
  - response to the external or internal signals and conditions
  - event and time ordering

# Bass Diffusion – Agent Based version



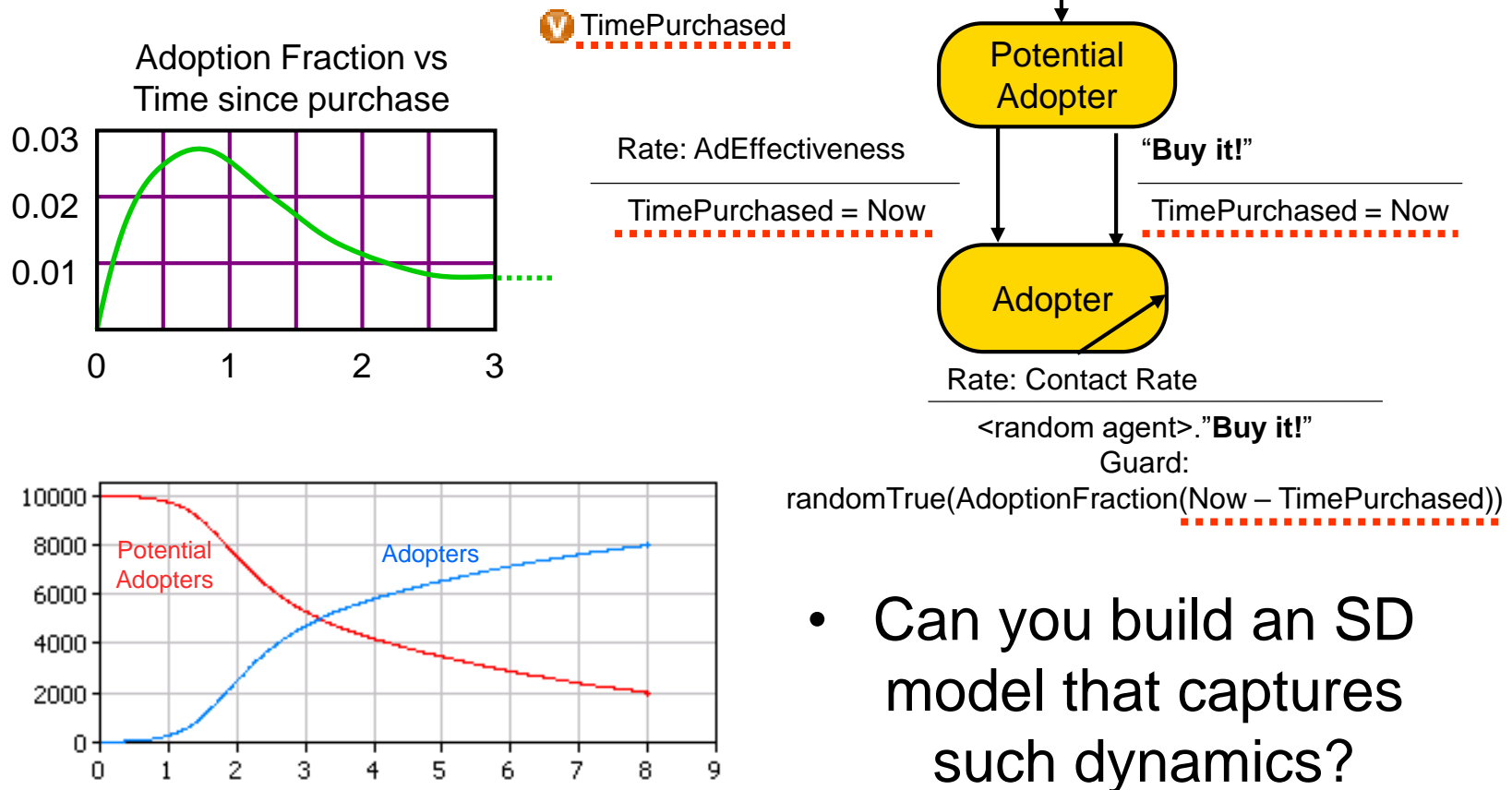
**AB**





# Capturing more with AB Model

- Let the word-of-mouth influence of an adopter depend on how recently he has purchased



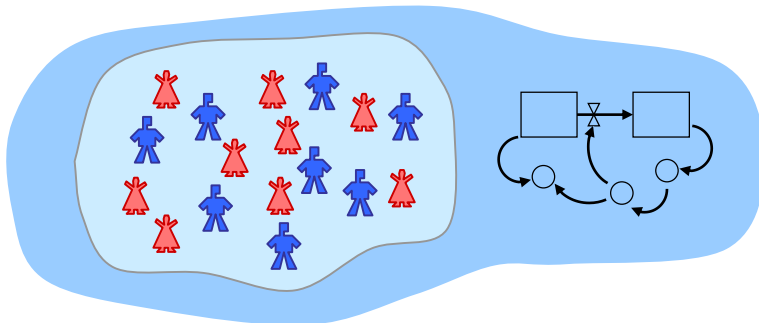
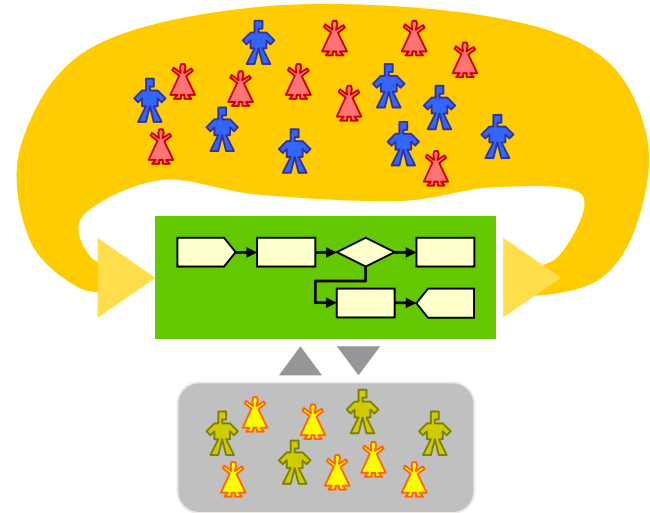
- Can you build an SD model that captures such dynamics?

# Which approach to use?

- If the problem requirements fit well into the DE or SD modeling paradigms – you can safely use these *traditional approaches*
- In cases where your system contains active objects (people, business units, animals, vehicles, or projects, stocks, products, etc.) with timing, event ordering or other kind of individual, autonomous behavior – *You will benefit from applying the AB approach*
- Sometimes these requirements are at the sub-model level. Then you can consider mixing different approaches in one model and applying most appropriate technique where needed

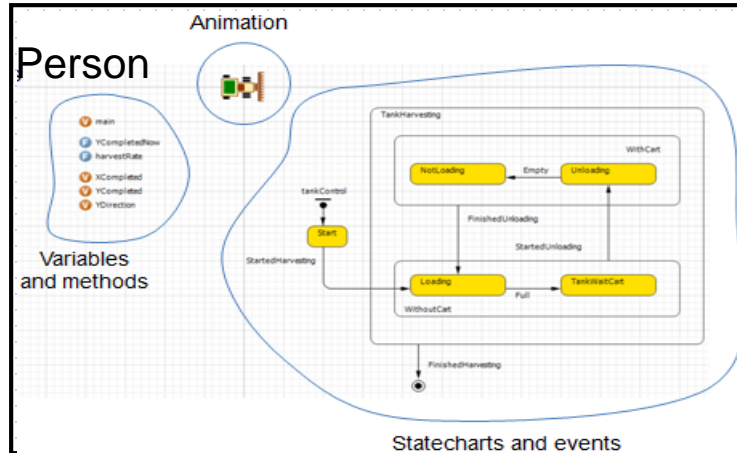
# Multi-paradigm model architectures

Agents (e.g. customers) interact with other agents (staff) in a Discrete Event flowchart

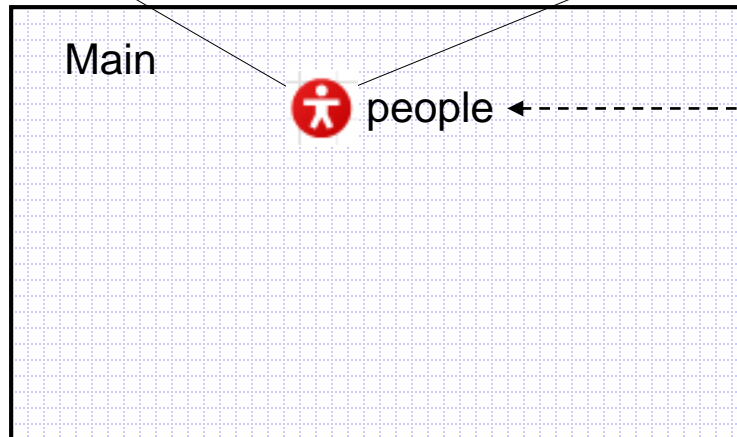


Agents live in an Environment modeled in System Dynamics way

# Typical architecture of an AB model



Name: *people*  
Type: *Person*  
Replication: *100000*



Adding/removing people:

```
add_people();  
remove_people( p );
```

Iterating through all people:

```
for( Person p : people ) {  
    ...  
}
```

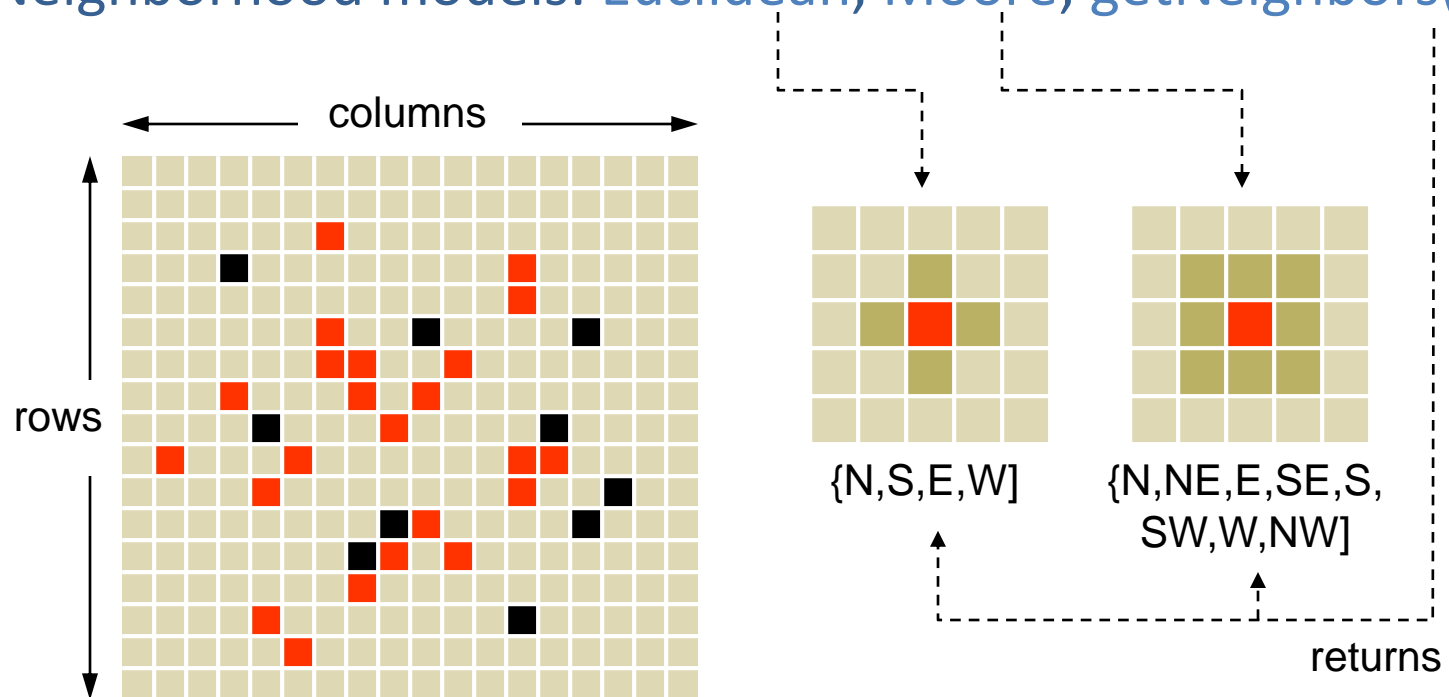
# Space: Discrete

- 2D array of cells *Rows* by *Columns*

At most one agent per cell; to retrieve location: `getR()`, `getC()`

Movement: `jumpToCell()`, `jumpToRandomCell()`, etc.

Neighborhood models: Euclidean, Moore; `getNeighbors()`



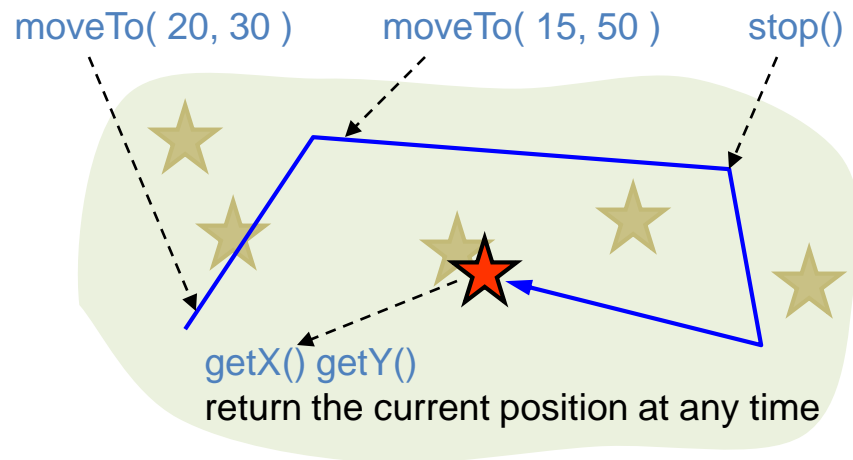
# Space: Continuous

- Agent has (x, y, z) coordinates in 3D space

- Use agent API:

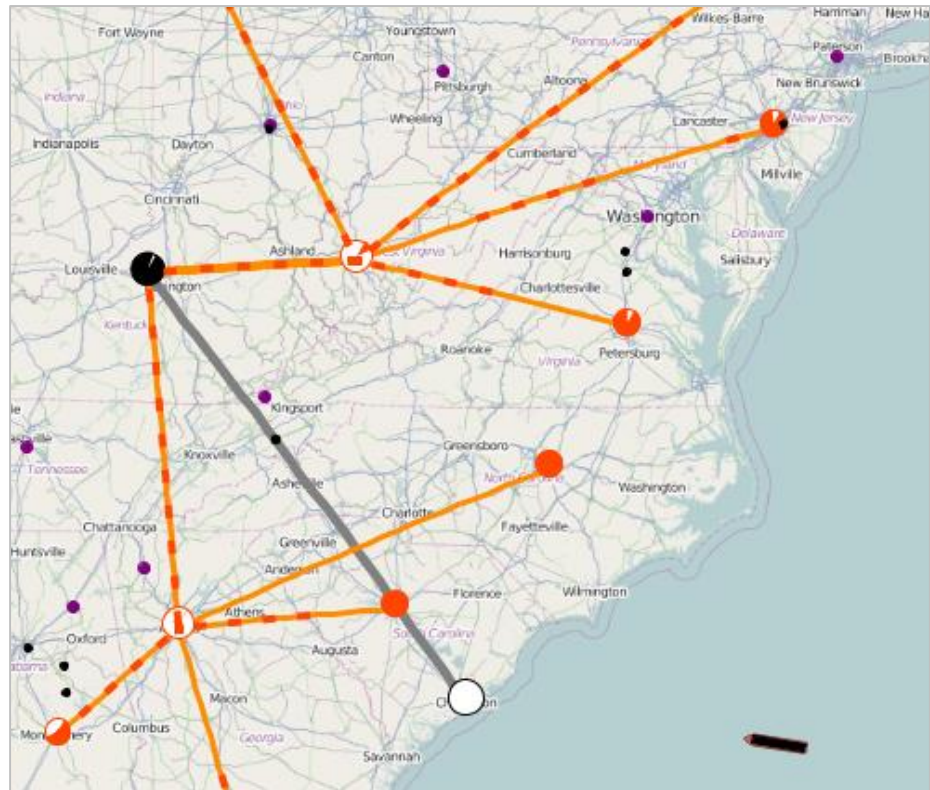
```
getX(); getY();  
distanceTo( agent );  
moveTo( x, y, z );  
jumpTo( x, y );  
stop();  
isMoving();  
timeToArrival();  
setSpeed ( speed );
```

- Define action:  
On arrival



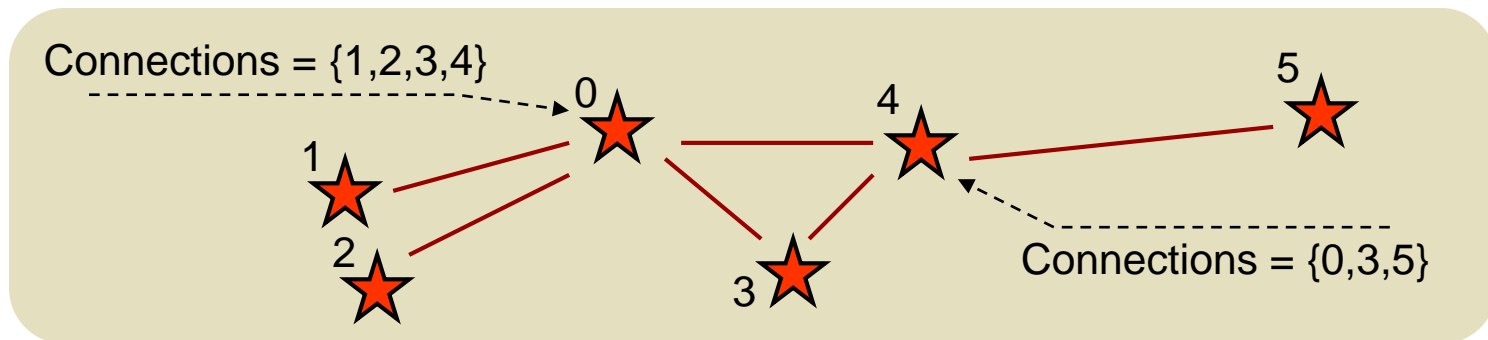
# Space: GIS

- Agents in a geospatial environment defined by GIS map
- Agent has real (latitude, longitude) coordinates in space
- Use agent functions:  
*getLatitude();*  
*getLongitude();*  
*distanceTo( agent );*  
*jumpTo( x, y );*  
*moveTo( x, y );*  
*stop();*  
*isMoving();*  
*timeToArrival();*  
*setSpeed ( speed );*
- Define action:  
On arrival



# Network: connections and communication

- Every agent has a list of connections – other agents
  - Use standard network types or define your own using API:  
`connectTo( agent ); disconnectFrom( agent );`
  - Access the collection of connected agents:  
`getConnections(); getConnectedAgent( i );`
  - Communication in network:  
Send messages:  
`sendToAll(msg); sendToRandom(msg); sendToAllConnected(msg);`  
`sendToRandomConnected(msg); send(msg, agent)`  
Define reaction in *connections* element: On message received





# Network: Standard types

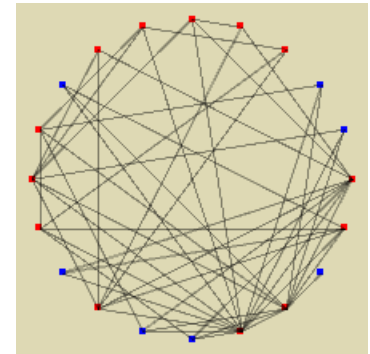
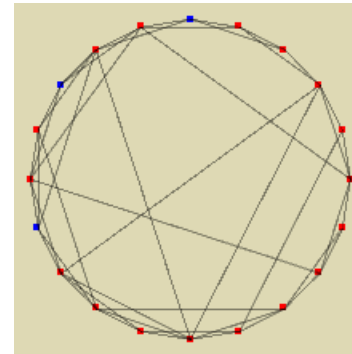
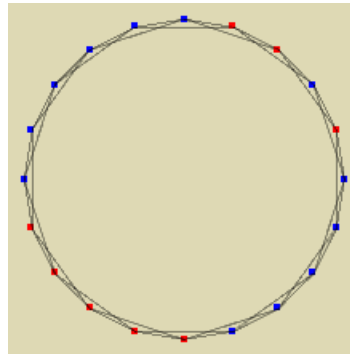
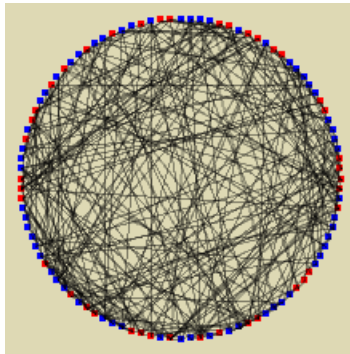
- Standard network types:

Random,

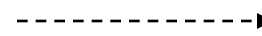
Ring lattice,

Small world,

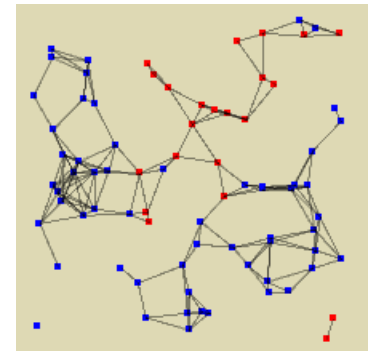
Scale free,



Distance based (layout dependent)



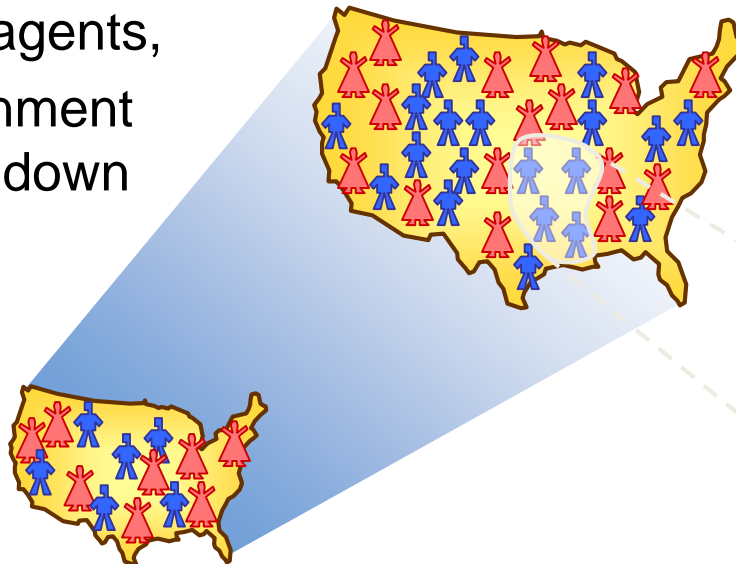
- You can
  - combine standard and custom networks
  - re-apply standard network during run, etc.



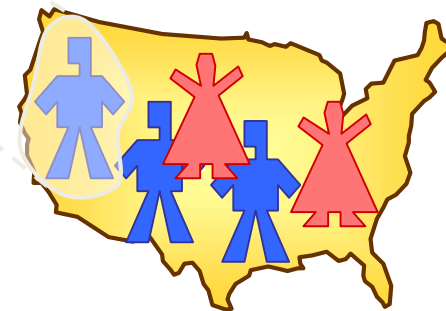
# How many agents to simulate?

- If I need to model the US population do I need to simulate 300,000,000 agents? **Fortunately not!**
- Two main “model scaling” techniques are used:

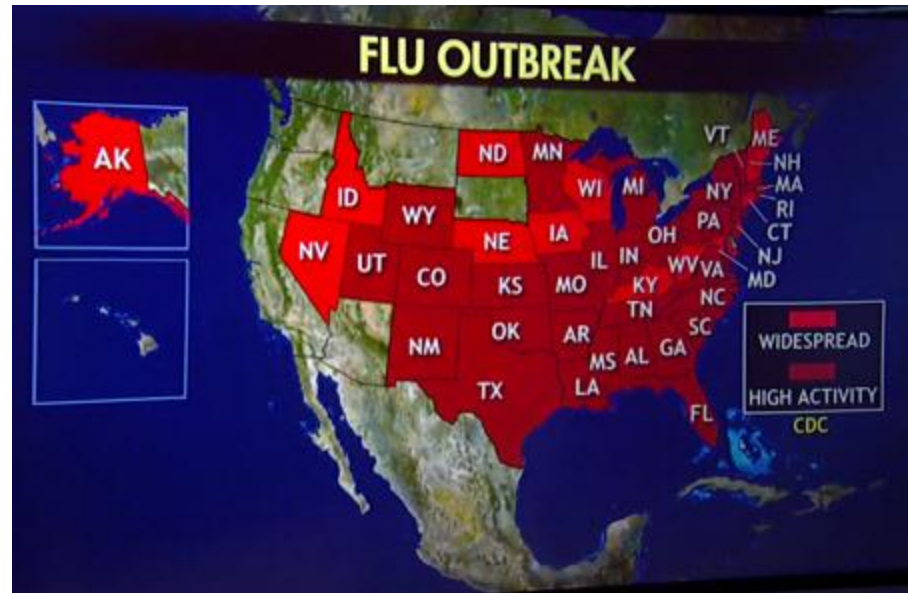
- Same agents,
- Environment scaled down



- Same environment
- Agents represent groups



# Disease Spread Model



# Disease Spread Model

- In the model each person has 3 possible states: **Susceptible**, **Infectious** or **Recovered** (SIR). Initially all but a few people are susceptible, and a few are infectious. Upon contact with an infectious person a susceptible person will get the disease based on a certain probability.
- The agents are placed in a continuous space. The contacts occur between random agents.

# Supply Chain Model



# Pedestrian Modeling

# What are pedestrian models built for?

- At a preliminary project assessment stage
  - Assess the ability of a facility to cope with a planned loading and comply with safety requirements
- At the stage of the design of a new facility
  - Assess alternatives, promptly assess revisions, seek the best solutions
- During construction /maintenance works at an operating facility
  - Seek the least inconvenient temporary routes
- As well as for presenting your project in a contest
  - Pedestrian models enable to obtain high quality and convincing animation and vividly demonstrate your offer
- At operating facility
  - Increase a throughput capacity, arrange queues
  - Optimize the operation of services (number of personnel, working hours)
  - Allocate signage
  - Assess the throughput capacity of a facility at a planned increase of loading
  - Optimize time schedules (for example, train schedules)
  - Allocate advertisement, goods, retail outlets
- Safety
  - Plan escape routes
  - Vulnerability assessment for terroristic attacks and catastrophes

# Which facilities are modeled?

## transport

- Railway stations
- Metro stations
- Airports
- Pedestrian passageways

## “attractions”

- Shopping malls
- Museums
- Amusement parks

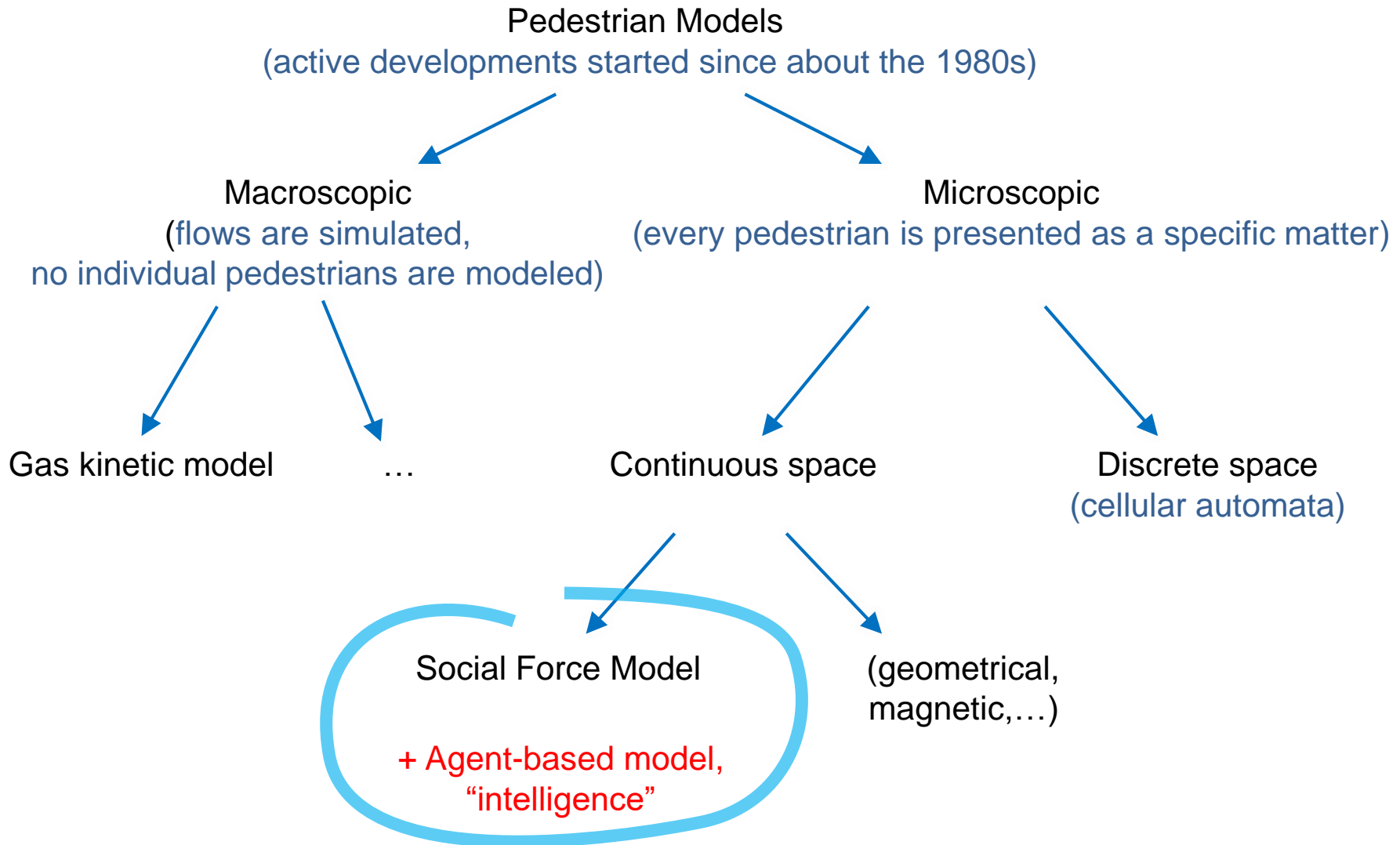
## events

- Stadiums
- Concert halls
- Street events (festivals, rallies, demonstrations)

In general all the facilities where the arrangement of physical space for pedestrians affects throughput capacity, quality of service, and safety

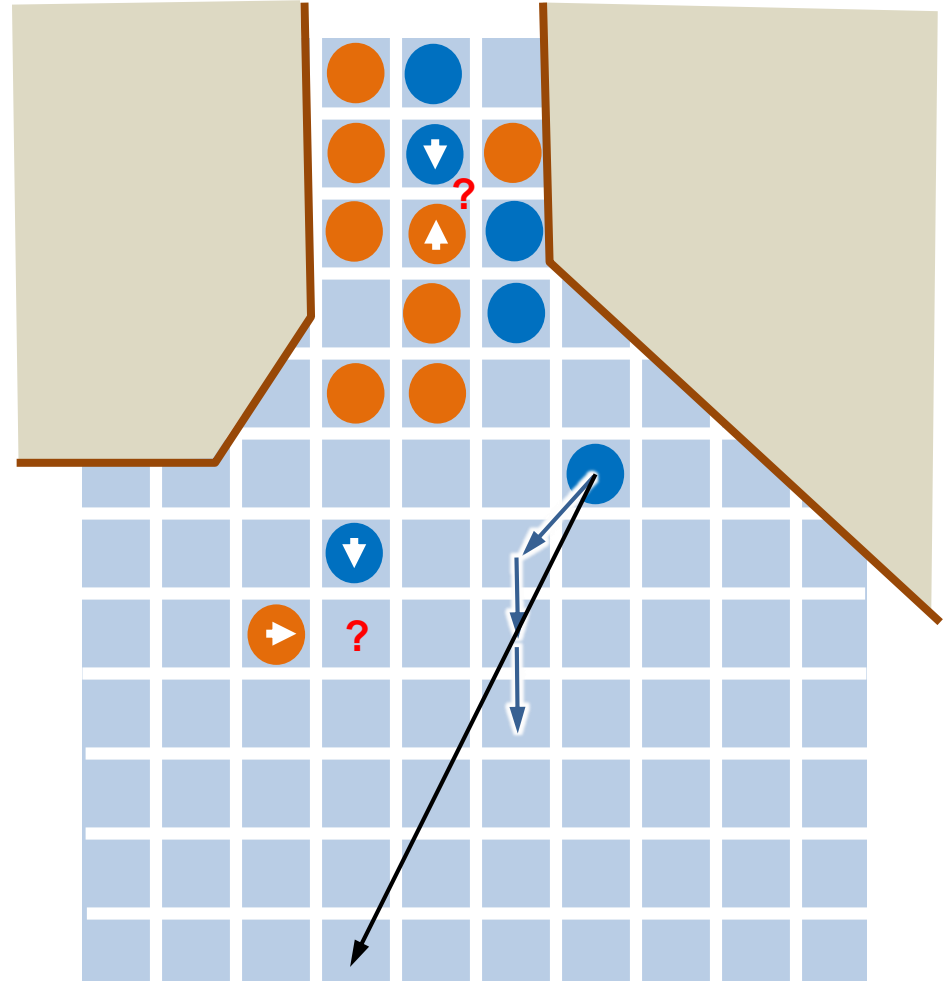


# Theory. Pedestrian Model Types



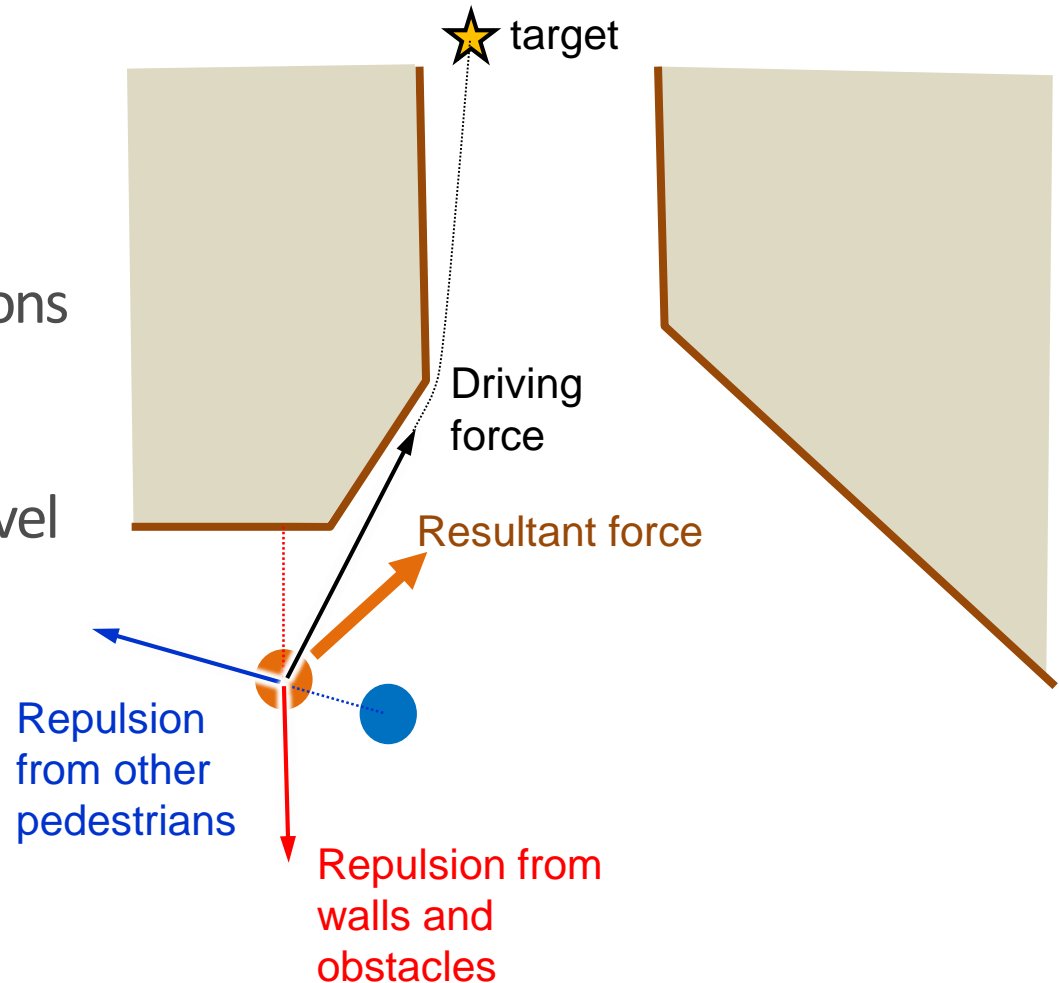
# Cellular automata

- Easy local rules
- Fast-to-calculate
- Can be well-calibrated
- Poor animation
- See Blue & Adler

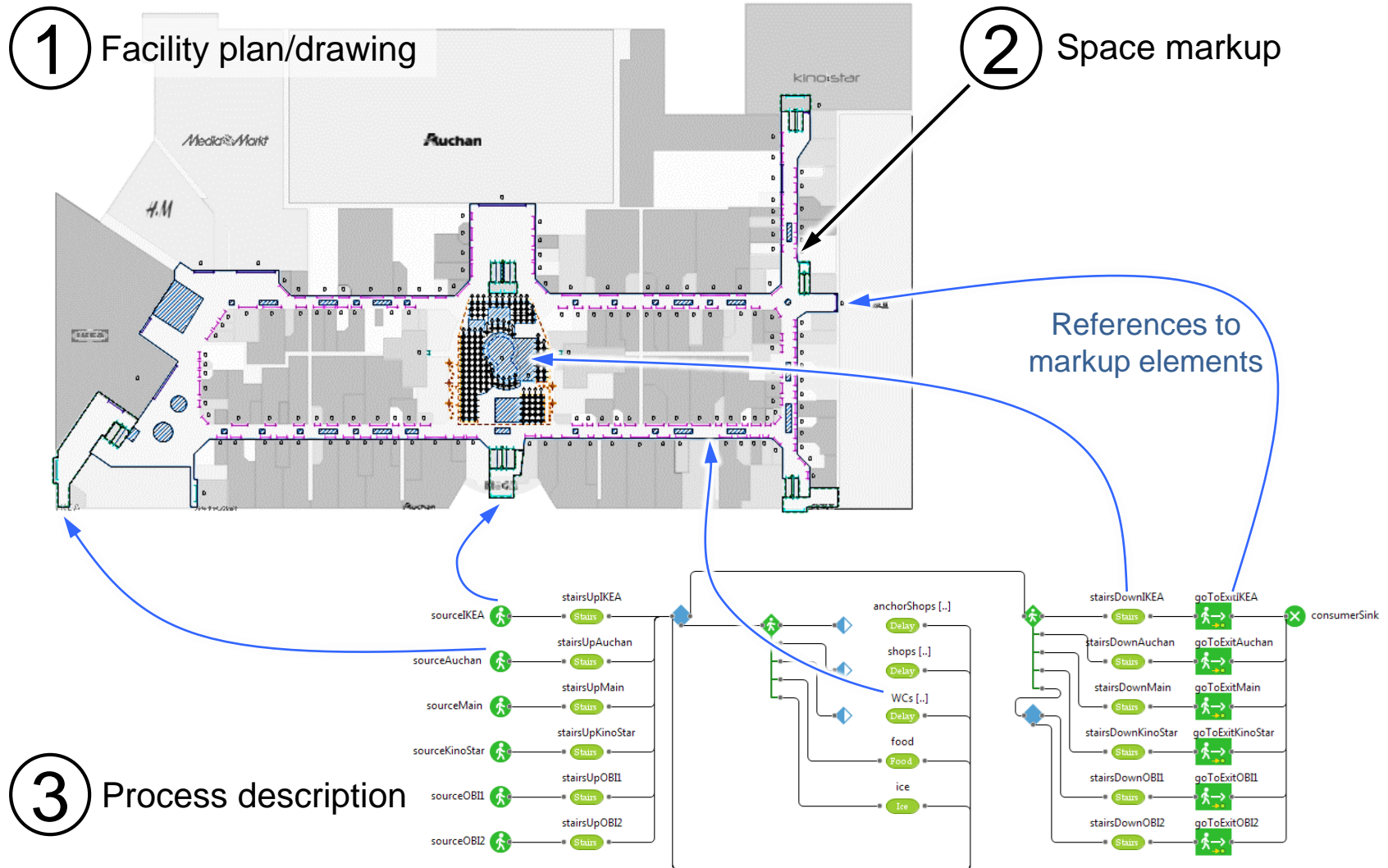


# Social Force Model

- Newton mechanics
- Realism
- Relatively slow calculations
- Very realistic animation
- Extended with higher level decision making logic
- See Helbing & Molnar

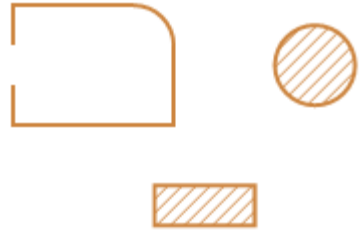


# How are pedestrian models built?



# Space Markup elements

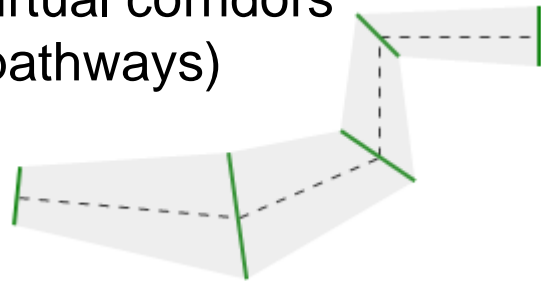
Walls



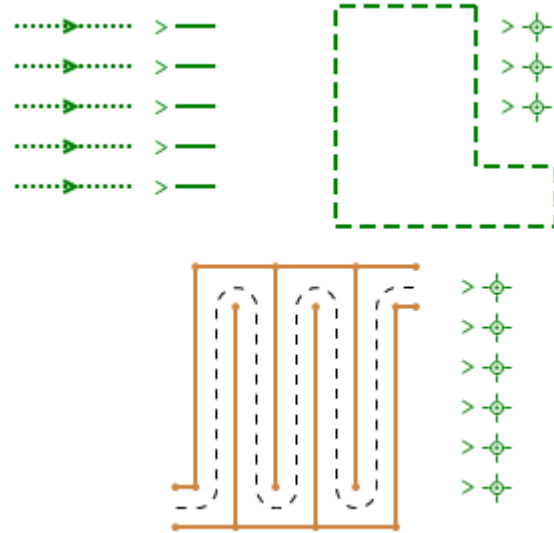
Target lines / pedestrian appearance lines



Virtual corridors (pathways)



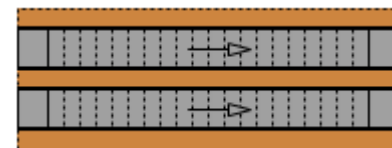
Services (service points) and queues



Waiting areas / target areas



Escalator



# Process Description Basic Blocks

## PedSource



Creates pedestrians on a line, at a point or in an area with a given rate, according to a time schedule, etc.

## PedService



Sets servicing parameters (where is a delay, the selection of a queue, etc.)

## PedGoTo



Sets up an objective or a route

## PedWait



Sets waiting parameters (where to wait, in relation to time, until an event)

## PedSelectOutput



Divides a passenger flow

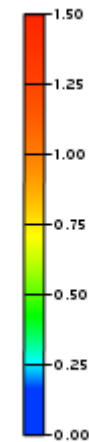
## PedSink



Deletes passengers from the model

# Measurements and Statistics in Pedestrian Models

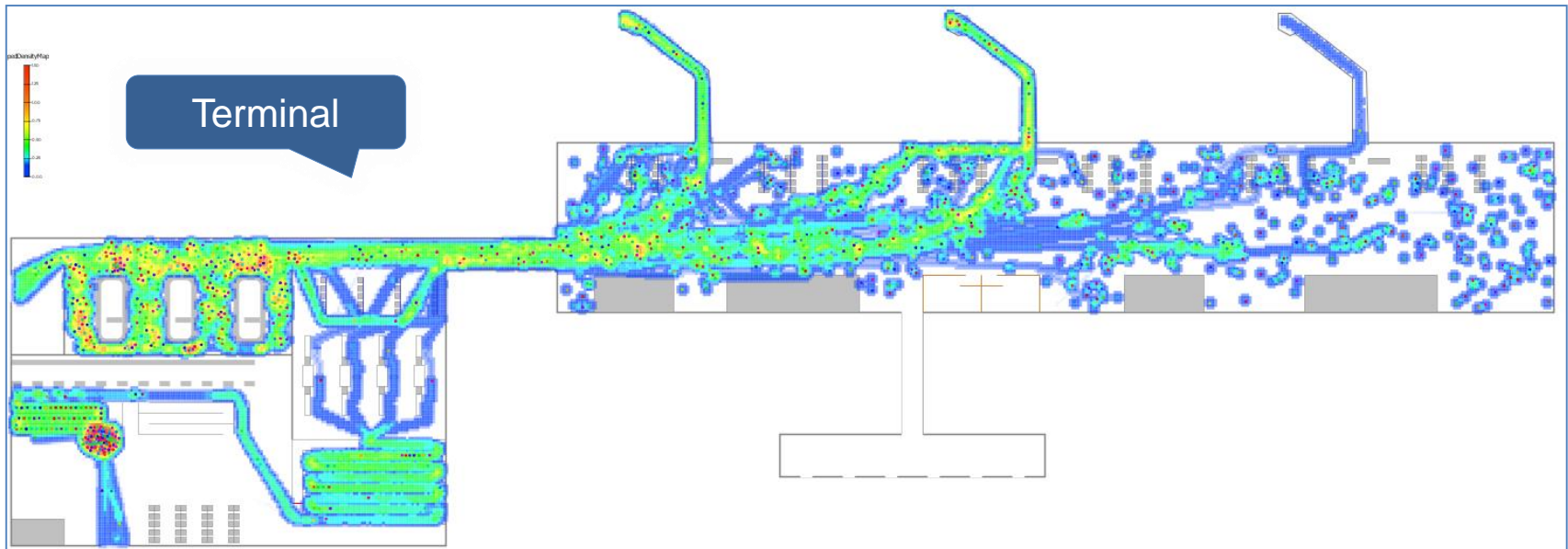
- Metrics specific for pedestrian models
  - Flow characteristics: the total number of passenger having passed through a section per a unit of time, the same quantity per a unit of length
  - Density in a certain area: the number of passengers per square meter (average per a unit of time); density charts



PedFlowStatistics



PedestrianDensityMap



# Individual Features of a Pedestrian

- Since each pedestrian is modeled as an agent, individual features can be adhered to them
- Features built in a basic model:
  - Comfortable speed
  - Dimension (“diameter”)
- These can be added to them:
  - Individual targets (flight, platform, shop)
  - Servicing class (first / business / economy)
  - Citizenship (US/EU/other, ...)
  - Servicing speed
  - ...
- These features can be checked during the pathway of a pedestrian throughout a process diagram and affect their behavior



# Groups

- Pedestrian behavior in groups considerably differs from that of independent pedestrians
  - Hold together; how to go (“in a rank”, “in a convoy”, “in a flock”)?
  - The presence or absence of a leader (for example, a guide)
  - Service: one pedestrian is serviced for all? (buys tickets for all, whereas a security check should be passed by everybody)
  - Does everybody stand in a queue? Where are those who are not standing in a queue waiting?

**PedSource** Is able to set groups, sets initial construction as well as default behavior at servicing points



**PedGroupChangeFormation**



Changes a group formation type

**PedGroupAssemble**



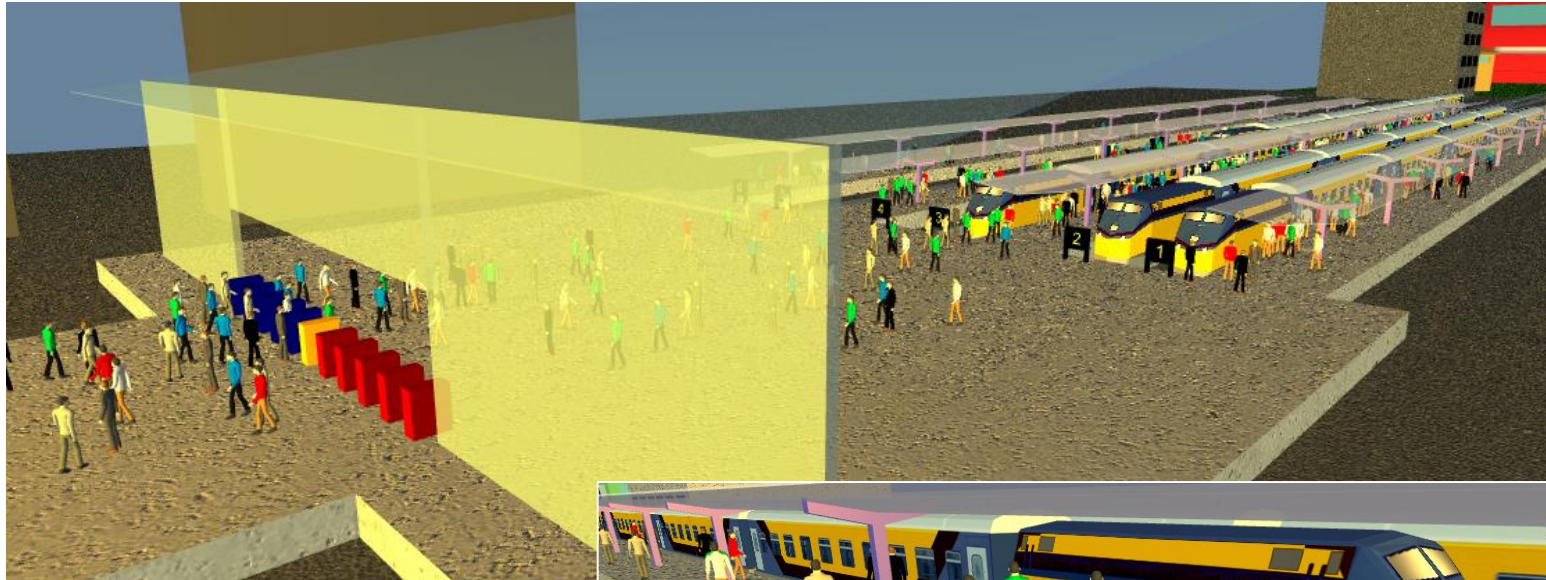
The same but out of the existing independent pedestrians

**PedGroupDisassemble**



Divides a group into individual independent pedestrians

# Railway Station Model



# Group Exercise

# Instructions

1. Break into teams and select a team name
2. Review the details and performance metrics of the existing process
3. From the list of improvement options, select the ones you believe will be the most impactful. Each option has a cost and the team has a budget
4. Reconvene and a simulation model will be used to show the outcome for each team's selections

# Further Information

# Steps For a Successful Project

- Follow a structured methodology
- Formalize the team
- Select the software
- Commit to the project
- Define success
- Consider key success factors
- Keep up with the industry

# Steps: Structured simulation methodology

- Define the problem or objective
- Develop a formal Simulation Specification
- Model the real or proposed system
- Gather model data
  - Historical
  - Observation / time studies
  - Estimates
- Verify and validate model
- Run “what-ifs” & analyze results
- Implement the changes!

# Steps: Define the objectives

- Communicate the written objectives
- Appreciate the unwritten objectives
  - Upfront and unbiased planning
  - Other methods have failed
  - Validate someone's ideas
  - Justify something already done
  - Provide a check and balance
  - Try out a gee-whiz tool
  - Visualize the process
  - Develop a training tool
  - Build a baseline for future use



# Steps: Develop a Simulation Specification

- Objective and scope
- System Description
- Assumptions
- Deliverables
- Schedule
- Structure (approach, tool(s), animation)
- Interface, inputs, outputs
- Data collection strategy
- Validation methods
- Resource requirements
- Planned scenarios

# Steps: Model validation (ER example)

- Compare actual versus simulation
  - Correlation study
- Comparison to direct observation. For emergency department, for example:
  - Arrivals (numbers, day, time)
  - Patients in waiting room
  - Patients in hallway
- Subject matter expert review
- Demo of model animation for the users
  - Queues, paths, bottlenecks

# Steps: Formalize the team

- Project manager
- Process designers
- Process owners
- Process users
- Data sources
- Upper management
- Simulationists
- Simulation users

# Steps: Today's simulation tools

Easier to user interface

Industry-specific custom templates

Improved model build and run time

Used throughout system lifecycle

Numerous simulation applications

# Steps: Tool considerations

- User interface
- Flexibility
- Upgrade progression
- Data exchange
- Animation (none, 2D, 3D)
- Run-time license or viewer
- Object-oriented design
- Custom object and template development
- Continuous and/or discrete
- Optimization
- Customer care
- Market breadth
- Price

# Steps: Commit to the project

- Allocate \$ for software purchase and maintenance/support
  - Initial software purchase (\$1-25K)
  - Annual software maintenance
    - *Higher cost software - % of purchase*
    - *Lower cost software – purchase upgrade*
- Attend offsite or uninterrupted training
  - General appreciation-level
  - Detailed simulationist-level
- Identify the organization and person(s) responsible for simulation in the company
- Conduct a small pilot project
- Provide visible management support
- Maintain proficiency

# Steps: Define success

- Tangibles
  - Results that drive decisions
  - Verified improvement
- Intangibles
  - Process understanding
  - Team building
  - Employee involvement
  - Management visibility
  - Success story

# Steps: Consider key success factors

- Start small & with a pilot project
- Build ownership of the model & results
- Bound the project through defined scope
- Use a hierarchical modeling methodology
- Spend enough time developing and communicating assumptions
- Get the help you need
- Target the lowest fidelity level possible
- Ensure management visibility
- Maintain momentum



# Steps: More key success factors

- Involve as many as possible as early as possible
- Take pictures or movies of the actual system and use them in discussions
- Collect more than process step data
- Develop descriptive (yet clear) graphics
- Validate the model with all constituents
- Consider the downstream user
  - Interface tailored to user
  - Reuse
  - Documentation
- Develop the “believable baseline”

# Steps: Keep up with the industry

- Societies
  - Institute of Industrial & Systems Engineers ([www.iise.org](http://www.iise.org))
  - The Society for Modeling & Simulation International ([www.scs.org](http://www.scs.org))
  - Institute for Operations Research and the Management Sciences ([www.informs.org](http://www.informs.org))
- Conferences
  - The Winter Simulation Conference
  - INFORMS Annual and Analytics Conferences
  - Some vendors have user conferences
- Books & Periodicals
  - The Big Book of Simulation Modeling
  - AnyLogic in 3 Days
  - Conference Proceedings
- Search the web!