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# Program and Portfolio Tradeoffs Under Uncertainty Using Epoch-Era Analysis

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# Presentation Outline



## Motivation

- Influence of Uncertainty on Lifecycle Value Delivery

## Research Approach

- Strategies for Considering Uncertainty
  - Epoch-Era Analysis (EEA)
  - Modern Portfolio Theory (MPT)
- Joint EEA and MPT Design Method for Portfolios

## Case Application

- Carrier Strike Group (CSG) Portfolio

## Conclusion

# THE CHALLENGE OF DESIGN UNDER UNCERTAINTY

# Design for Value Sustainment



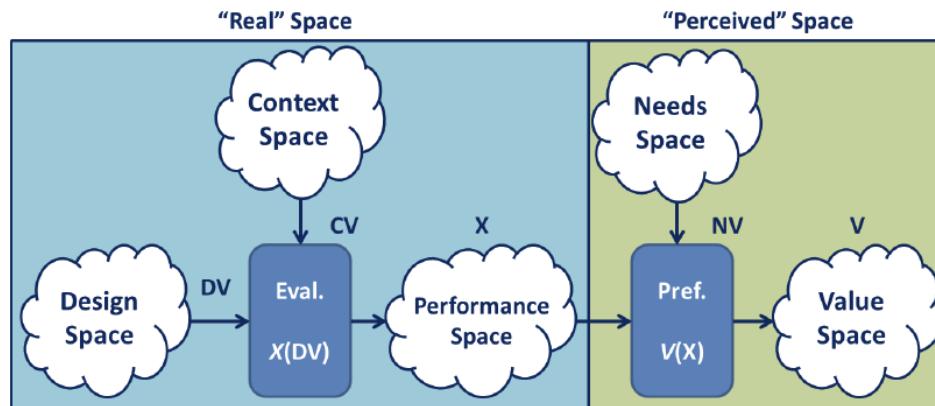
Many systems exist in a global environment that will inevitably experience dramatic, dynamic shifts in context

Exogenous uncertainties exist in the acquisition and operational environment

- Emerging technologies (e.g., UAS maturation)
- Political transition (e.g., low carbon fuels mandate)
- Economic shifts (e.g., global recession)
- Resource availability (e.g., rare-earths crisis)

Stakeholder needs may vary with the decision context

- Change of stakeholder *preferences*
- Change of mission *objectives*



(Beesemyer, 2012)

Design for value sustainment seeks to maximize portfolio value across a variety of foreseeable contexts and needs

# Design for Affordability



- 74 US Nunn-McCurdy cost breaches between 1997 and 2011
- Numerous breaches corresponded to **context changes** in the environment of the acquisition programs<sup>(GAO, 2011)</sup>
- A variety of **system-design** methodologies have been developed in response to the Better Buying Power (BBP) mandates<sup>(Carter, 2010)</sup>



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Can aspects of MPT and EEA be combined to create sustained lifecycle **affordability** for engineering portfolios despite changing contexts?

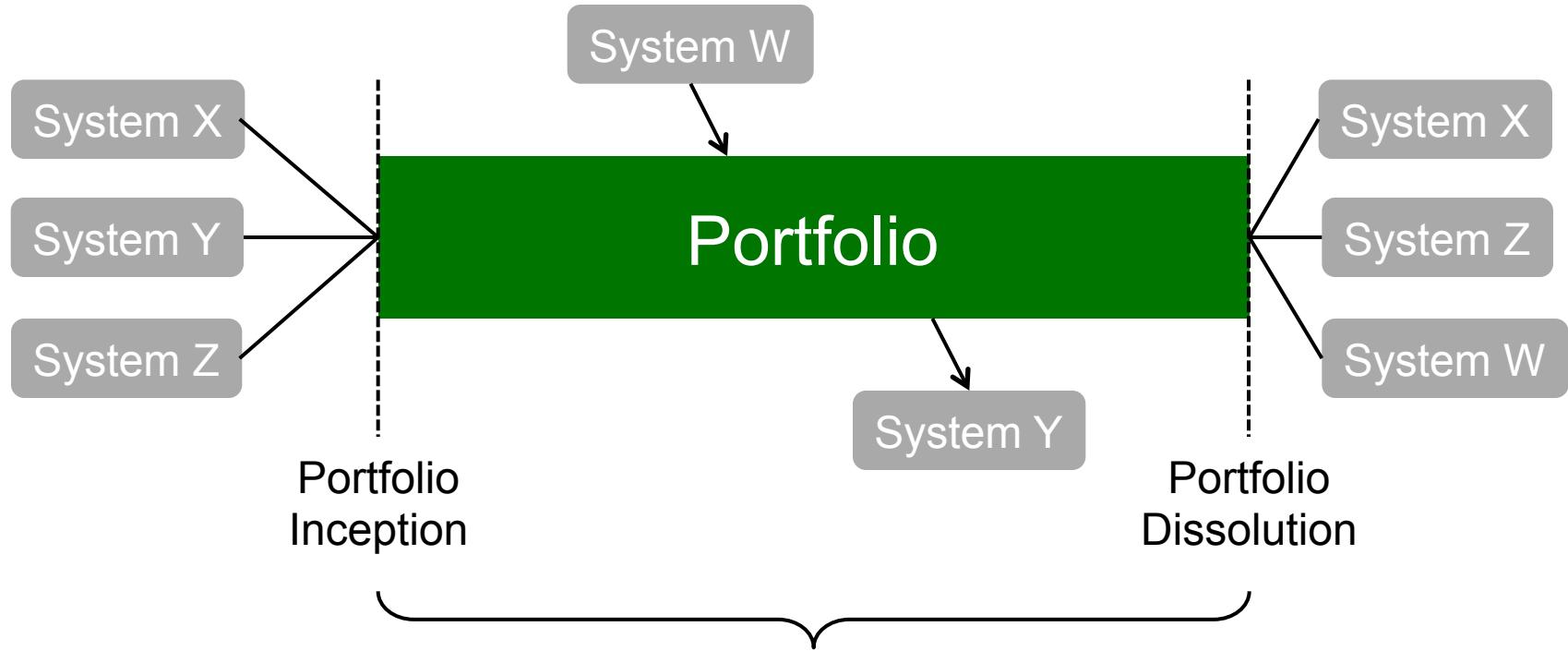
# Design for Affordability



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Affordability may be defined as “the property of becoming or remaining feasible relative to resource needs and resource constraints over time” (Wu, Ross, Rhodes, 2014)



# RESEARCH APPROACH

# Design Abstraction Terminology

Acquisition and development efforts face different challenges and opportunities contingent on the **scope** of the design abstraction

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System-Level: a singular major architectural element



Program-Level: multiple elements fulfilling common capability requirements



Portfolio-Level: multiple elements that collectively fulfill a set of joint capability requirements

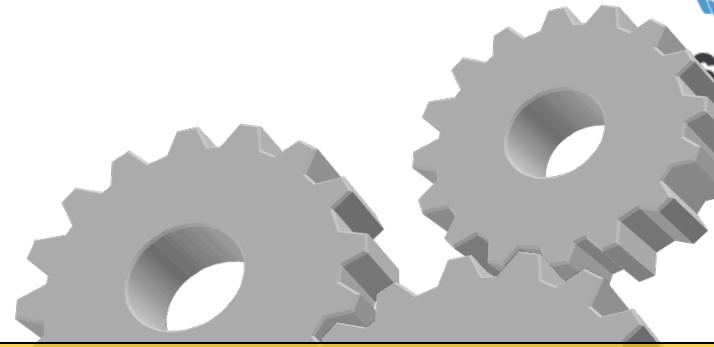
# Portfolio-Level Design



**System-level design methods do not effectively support the creation of specific portfolio-level properties**

- Multi-system acquisition of portfolios and operation of SoS present **higher order complexities** not addressed by system-level design techniques
- SoS engineering has developed approaches to consider the interactions of constituent systems and determine “satisficing” solutions<sup>(Keating et al. 2003)</sup>
- Some methods have also been adapted for portfolio design
  - Portfolio Theory application for SoS decision making<sup>(Davendralingam et. al, 2011)</sup>
  - Real options analysis for IT SoS acquisition strategies<sup>(Komoroski et. al, 2006)</sup>
  - Tradespace-based affordability analysis for complex systems<sup>(Wu et.al, 2014)</sup>

# Modern Portfolio Theory (MPT) for Engineering Portfolios



## Consistencies

- Value elicitation from stakeholders
- Modeling of asset value
- Founded in utility theory
- Identifies “efficient frontier” of potential alternatives

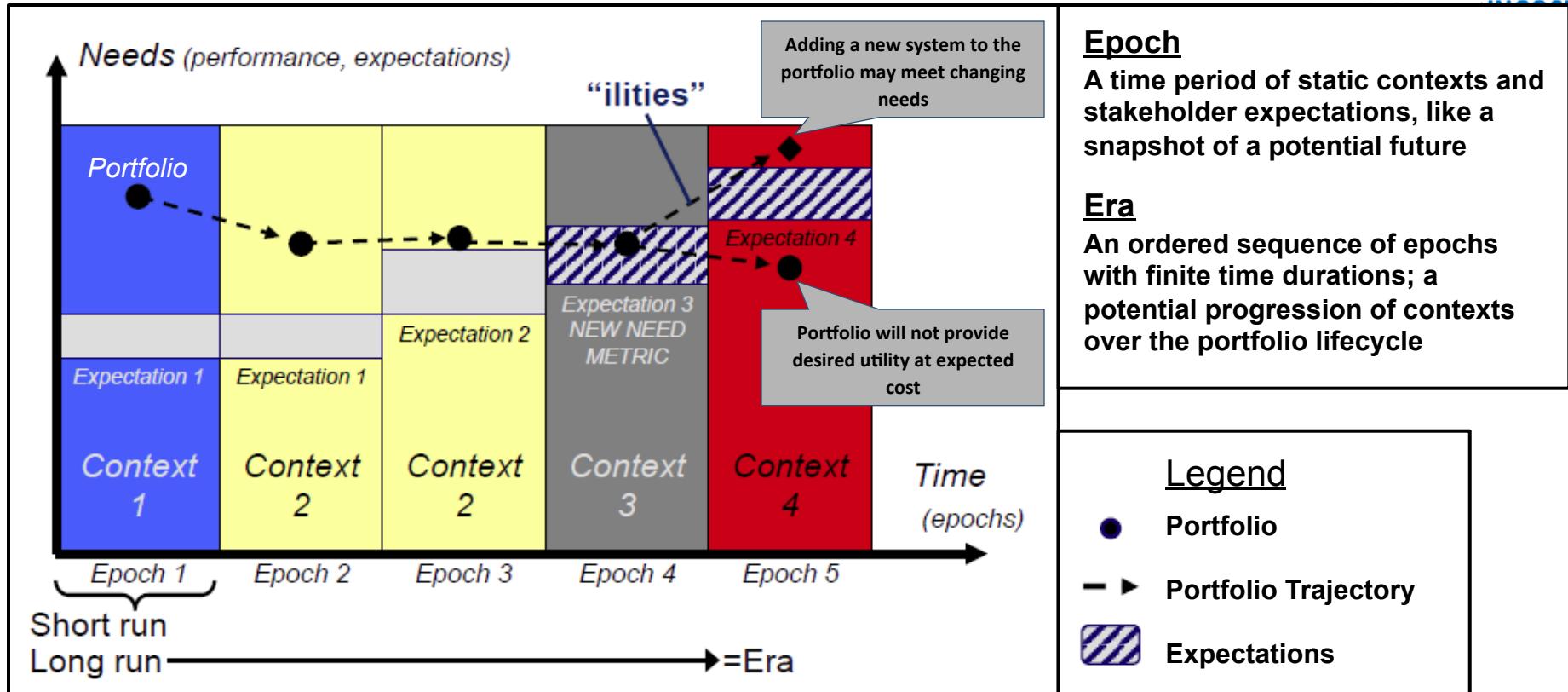
## Differences

- Asset performance is non-Gaussian
- Portfolio value is dictated by non-linear asset performance aggregation
- Covariance is insufficient to describe asset correlation
- Asset availability is dynamic
- Costs may accompany diversification

Select elements of Modern Portfolio Theory can improve the design and acquisition of engineering systems portfolios



# Epoch-Era Analysis

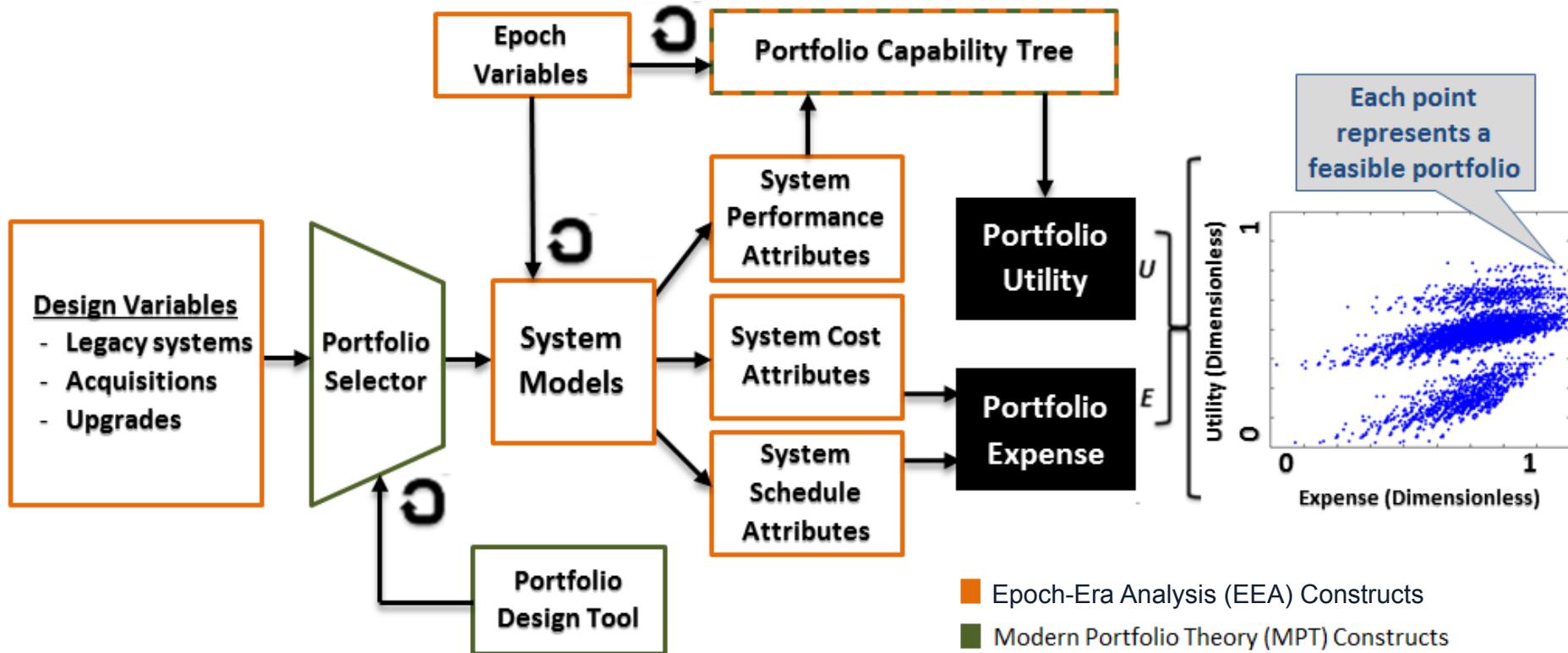


(Ross & Rhodes, 2008)

**EEA is an analytic method useful to assess potential portfolio performance over the dynamic environment in which it operates**

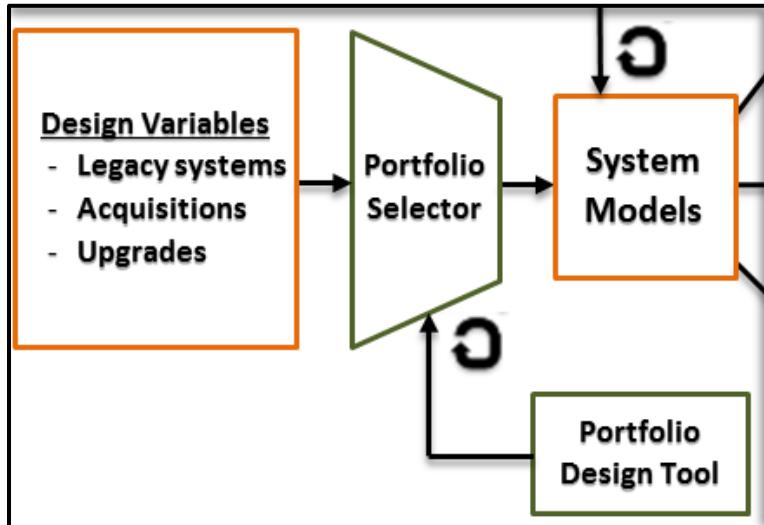
# JOINT EEA AND MPT METHOD TO SUPPORT DESIGN FOR AFFORDABILITY

# Portfolio-Level Epoch-Era Analysis for Affordability (PLEEAA)



Fuses elements of MPT with EEA through the framework of multi-attribute tradespace exploration

# Portfolio Enumeration



## Portfolio Design Tool

- Conducts **asset allocation**
- Applies portfolio **class constraints**
- Enumerates all possible portfolios

## Portfolio Selector

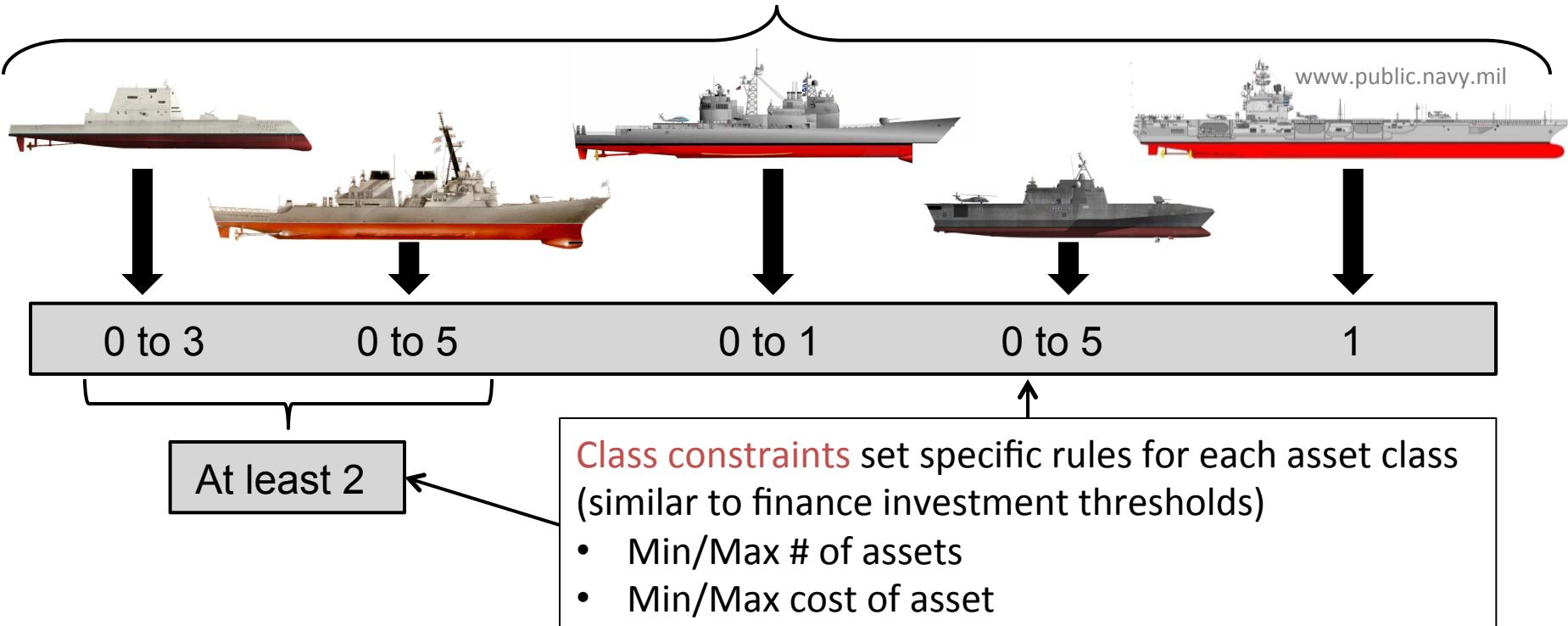
- Compiles a specific portfolio for modeling

An engineering portfolio may be represented by three primary **design variables**

- Legacy Systems – existing hardware available to the portfolio
- Acquisitions – new assets produced for the portfolio
- Upgrades – change options available for legacy systems

# Portfolio Design Tool

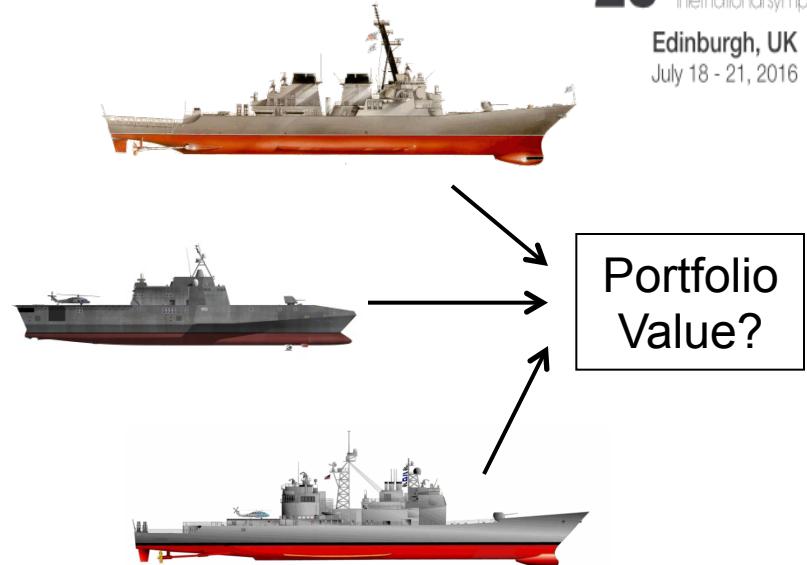
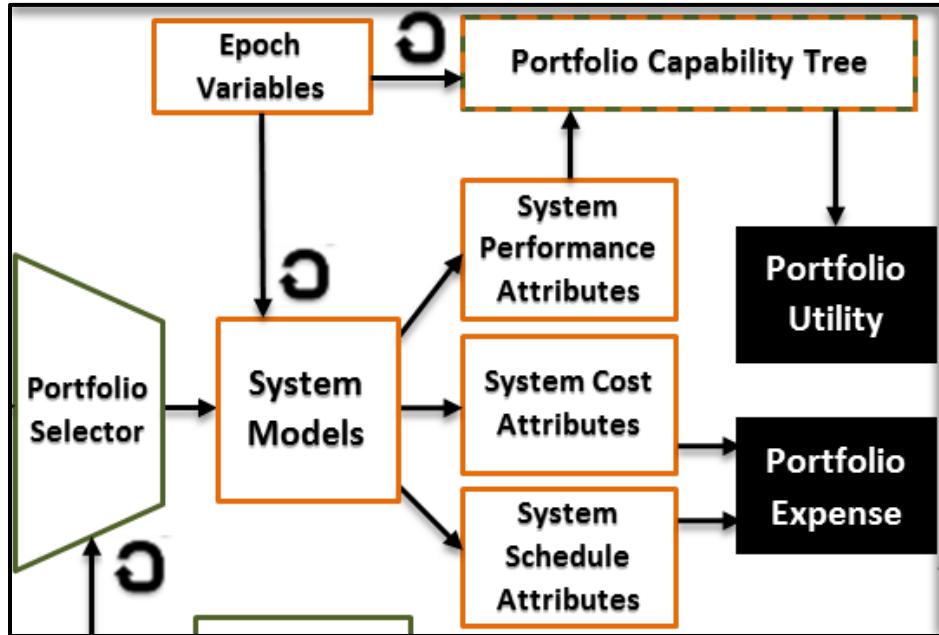
Fundamental to MPT, **asset allocation** identifies potential classes of assets which may constitute portfolio elements



# Constituent System Modeling

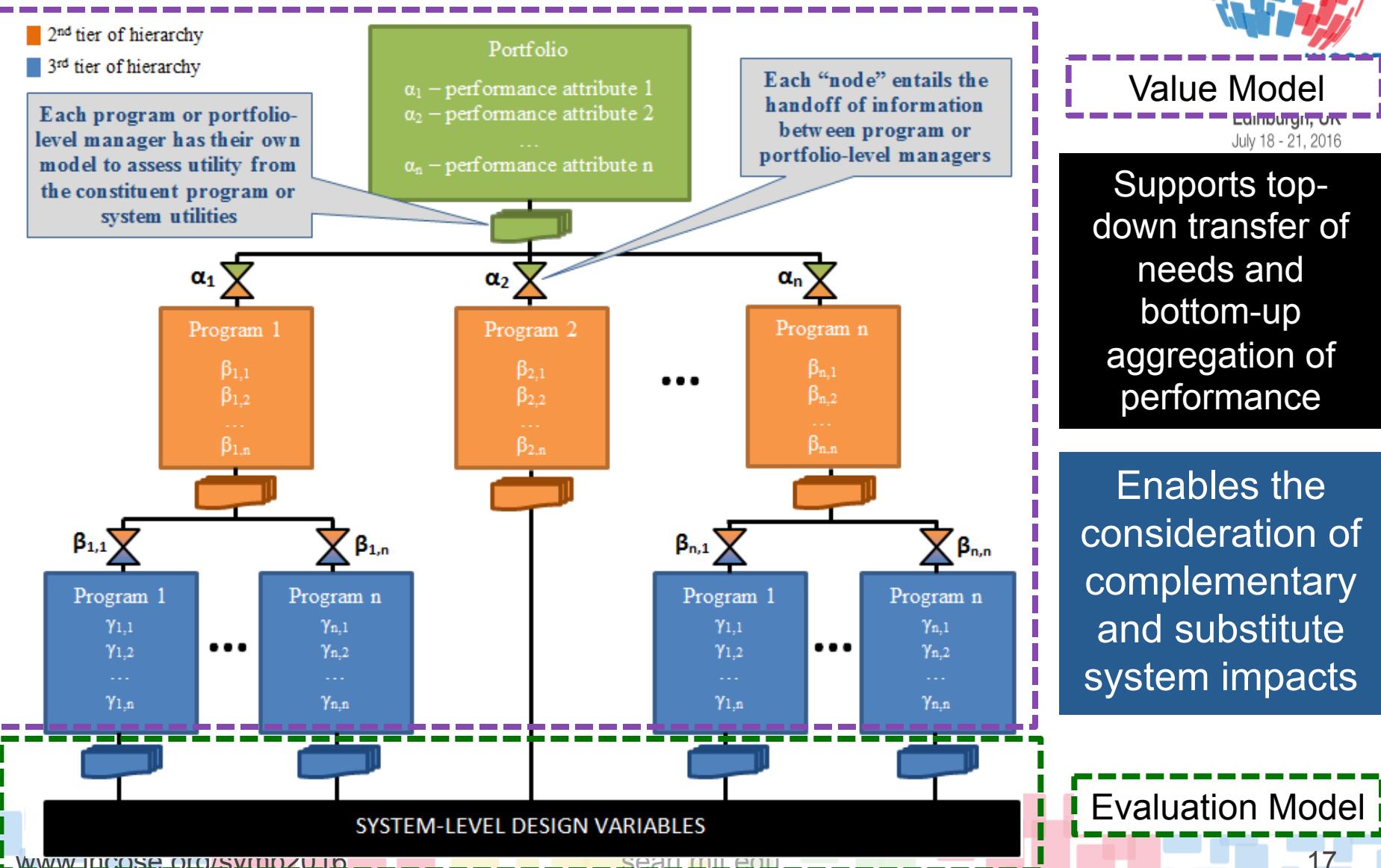


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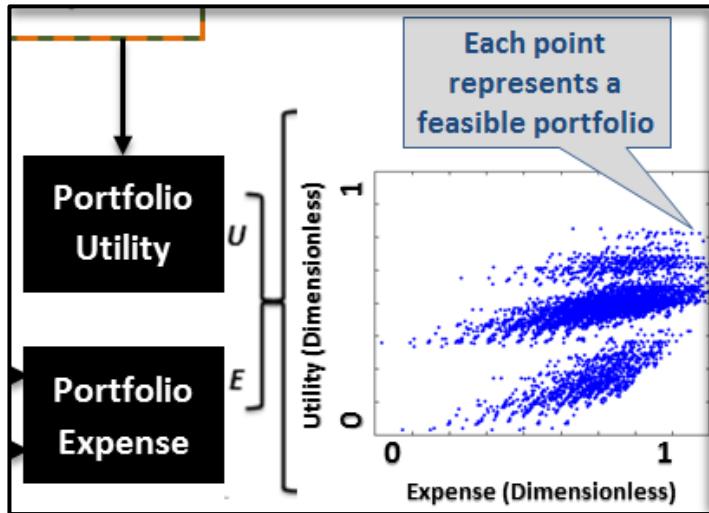


- System-level cost attributes are directly aggregated to portfolio expense
- The capability tree is a capability-based value mapping to aggregate system performance to determine portfolio utility

# Portfolio Capability Tree



# Multi-Attribute Tradespace Exploration with Epoch-Era Analysis



## Tradespace of Portfolios

- Utility and Expense axes
- Multi-attribute utility theory used to describe value of portfolio performance
- Hundreds of thousands of portfolios may be visualized

EEA provides several techniques to analyze the promising portfolio designs and conduct design tradeoffs with respect to value sustainment

- Single-Epoch Analysis: identification of “promising” portfolios in isolated epochs
- Multi-Epoch Analysis: exploration of the influence of contextual uncertainty on a set of promising portfolios
- Single-Era Analysis: identification of time-dependency of promising portfolio value delivery through multiple epochs
- Multi-Era Analysis: exploration of path-dependency of promising portfolio value delivery

# CASE APPLICATION: CARRIER STRIKE GROUP (CSG)

# Portfolio-Level Context Definition and Design Formulation



Identify the basic problem statement and design space for the proposed portfolio

## VALUE PROPOSITION

“responsive, flexible capability for sustained maritime power projection and combat survivability to shape the operation environment, respond to crisis, and protect the US and allied interest in any threat environment” – Chief of Naval Operations (2010)

## PERFORMANCE ATTRIBUTES

1. Electronic warfare capability
2. Defensive capability
3. Offensive capability
4. Power projection
5. Logistics

## Primary portfolio stakeholders

- Combatant commander (CCDR)
- Operational commander

## EXPENSE ATTRIBUTES

1. Acquisition cost
2. Influence cost
3. Operations cost
4. Schedule cost

## Potential Constituent Systems

### Legacy Systems

Arleigh Burke Flight I  
Arleigh Burke Flight II  
Arleigh Burke Flight IIA  
Ticonderoga

### Legacy Systems

Nimitz with Complement  
Los Angles  
Virginia  
Supply Class

### Acquisitions

Next Generation Combat Ship (NGCS) – 6 variants  
Arleigh Burke Flight IIA Restart  
Arleigh Burke Flight III  
Zumwalt

### Upgrades

Arleigh Burke Flight I upgrade  
Arleigh Burke Flight II upgrade

# CSG Capability Tree Formulation



Portfolio Level Capability Attributes
2nd Level SoS Capability Attributes
3rd Level SoS Capability Attributes
# of System Level Performance Attributes

} Levels of capability tree hierarchy

CSG Electronic Warfare Capability	Early Warning	6
	Weapon system detection	6
	Electromagnetic System	5

} Branch of capability tree

CSG Defensive Capability	Battlespace Defense Capability	Sea superiority	5
		Air Superiority	5
		Undersea Superiority	5
		Combat Search and Rescue	2
	Naval Asset Defense Capability	Anti-Ship Missile Defense	5
		Anti-Ship Kinetic Weapon	5
		Sea Mine Defense	5
		Torpedo Defense	5
		Crew Defense	4

CSG Offensive Capability	Missile Strike Capability	Naval Gun Fire Support	5
		Ballistic Missile Interception	5
		Cruise Missile Strike	5
		Torpedo Capability	5
		Sea Basing Capability	3
		Special Forces Insertion	4

Power Projection	2
CSG Logistics	4

# CSG Epoch Characterization



Seven epoch variables identified yielding a total of 2187 distinct epochs

EV Category	Epoch Variable	[Range]	Units
EV – Technology	Advanced Energy Weapons (AEW)	[0, 5, 40]	MW
EV – Technology	Unmanned Aerial Systems (UAS)	[0, 2, 5]	Berths
EV – Maintenance	Overhaul Event Costs	[0, 0.5e9, 2e9]	Billions \$
EV – Policy	Budget	[80, 100, 150]	%
EV – SoS management	Cooperation Costs	[80, 100, 150]	%
EV – Threats	Enemy Threat	[Low, Med, High]	Level
EV – Threats	Asymmetric Threat	[Low, Med, High]	Level

Five epochs initially selected for demonstration through the Carrier Strike Group case study

Epoch Names	Epoch Variables						
	AEW	UAS	Overhaul	Budget	Cooperation	Enemy	Asymmetric
Baseline	0	0	0	100	100	Low	Med
Small Navy	0	2	0	80	150	Low	Low
War on Terror	5	5	0	100	80	Low	High
Major Conflict	40	5	0	150	80	High	Med
Peacekeeping	5	0	0.5e9	100	100	Med	Med

# Design-Epoch-Era Tradespace Evaluation

- Based upon the 19 potential constituent systems
  - 53,108,336 unique portfolios were enumerated
  - 524,160 portfolios were evaluated
  - Between 220 and 477,916 portfolios were affordable, depending upon the epoch

Epoch	Valid Portfolios	Yield
Baseline	173,581	33.1%
Small Navy	220	0.04%
War on Terror	140,398	26.8%
Major Conflict	477,916	91.2%
Peacekeeping	191,558	36.5%

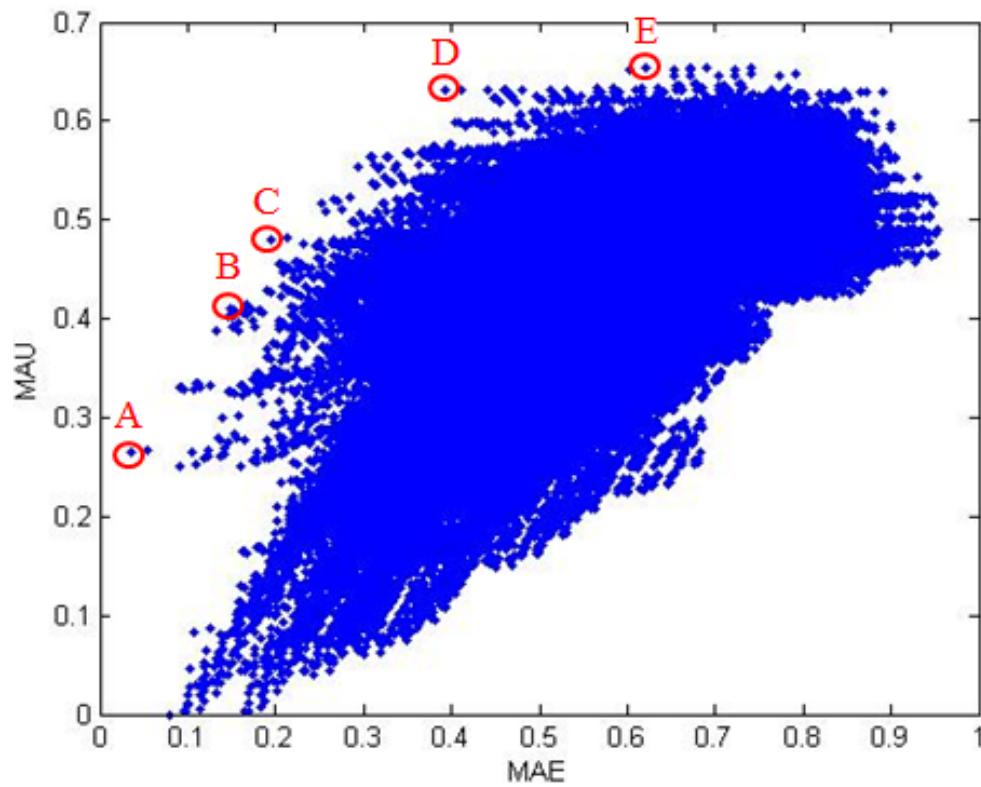
Severely limiting epoch due to a 20% budget cut and 50% rise in cooperation costs

**The PLEEA method enables a designer to consider far more alternatives, each in numerous potential future scenarios**

# Single-Epoch Analysis



Tradespace Exploration is conducted independently in each epoch



#	MAU	MAE	Portfolio Composition
A	0.2651	0.0352	1 Arleigh Burke Flight III 1 Nimitz with Complement 1 Los Angles
B	0.4109	0.1487	1 Arleigh Burke Flight I 1 Arleigh Burke Flight II 1 Arleigh Burke Flight III 1 Nimitz with Complement 1 Los Angles
C	0.4800	0.1953	2 Arleigh Burke Flight III 1 Nimitz with Complement 1 Los Angles
D	0.6305	0.3920	2 Arleigh B. Flight II Upgrade 2 Arleigh Burke Flight III 1 Nimitz with Complement 1 Los Angles
E	0.6532	0.6206	2 NGCS Variant 6 2 Arleigh B. Flight II Upgrade 2 Arleigh Burke Flight III 1 Nimitz with Complement 1 Virginia

Promising portfolios are identified on the efficient frontier of each epoch

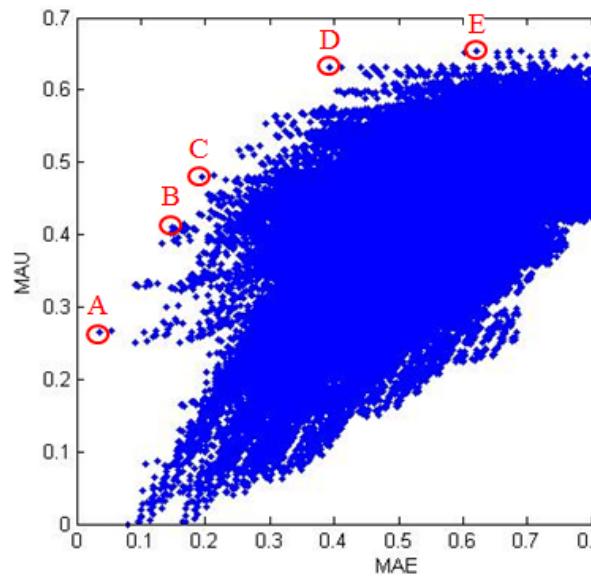
# Multi-Epoch Analysis



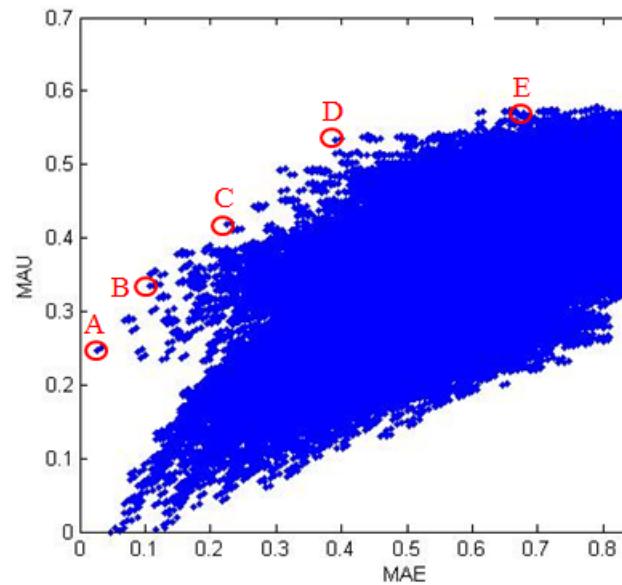
Promising portfolio designs are simultaneously explored in multiple epochs

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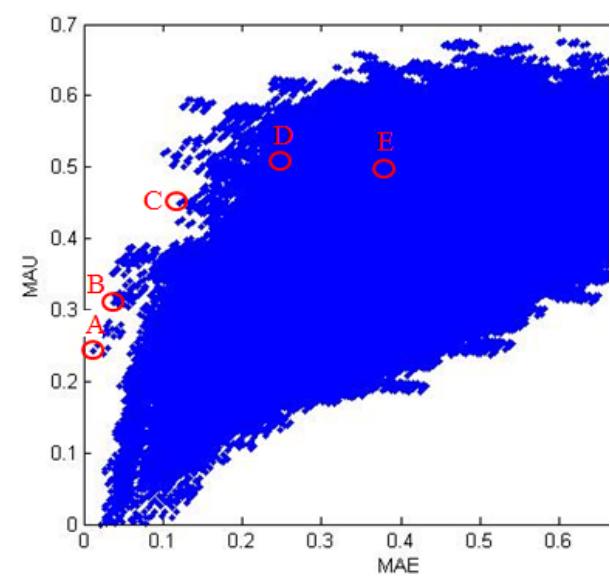
Baseline



War on Terror



Major Conflict



Multi-Epoch analysis illustrates the influence of contextual uncertainty on the utility of potential Carrier Strike Group portfolios

# Multi-Epoch Analysis

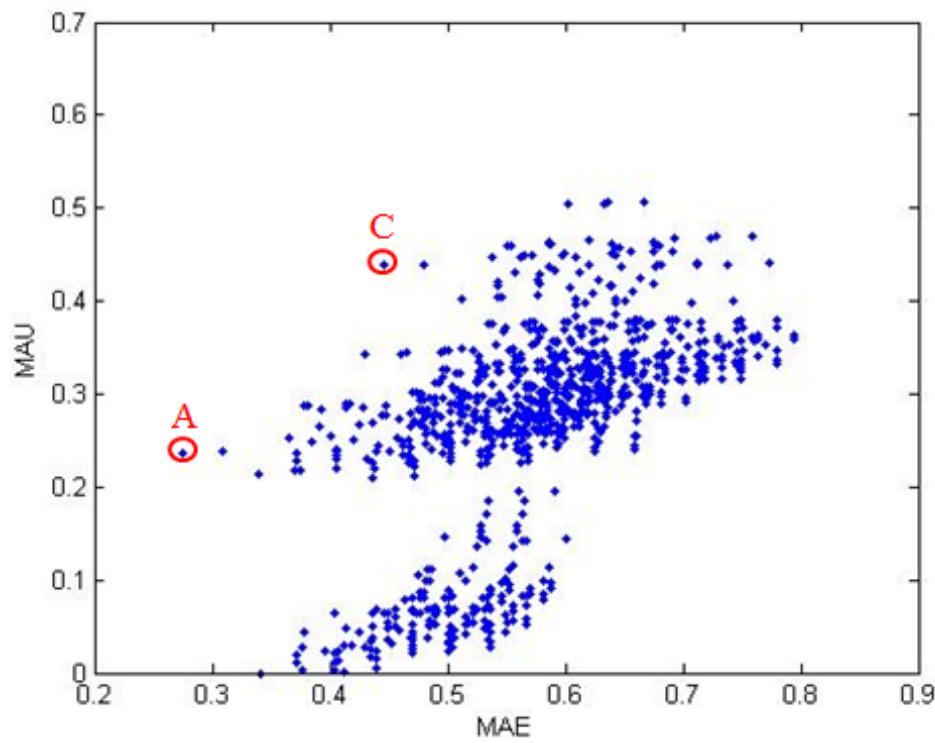
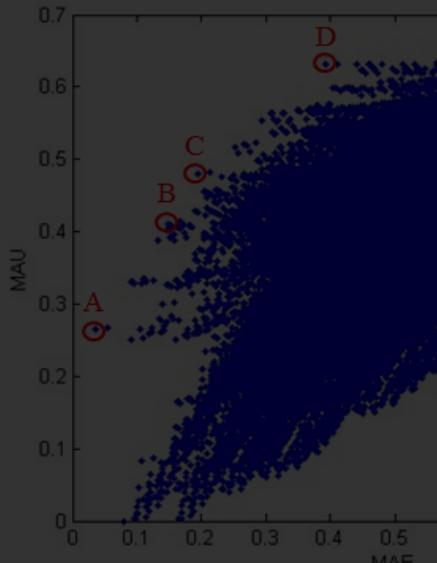


Promising portfolio designs are simultaneously explored in multiple epochs

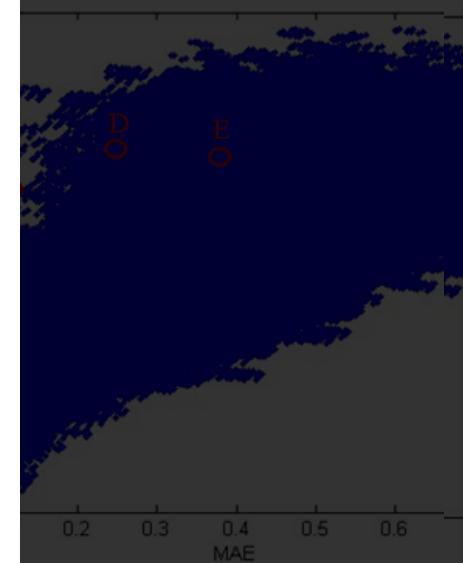
Small Navy Epoch

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Baseline



Major Conflict



Multi-Epoch analysis illustrates the influence of contextual uncertainty on the utility of potential Carrier Strike Group portfolios

# CSG Era Construction



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- An era is an ordered sequence of epochs
- Evaluating portfolio designs over an era illustrates the potential lifecycle value robustness of the portfolio
- Two eras were constructed from the five epochs through a narrative approach

## ERA 1

Baseline (5yr) → War on Terror (5yr) → Peacekeeping (10yr) → Baseline (3yr) → Small Navy (7yr)

TIME



## ERA 2

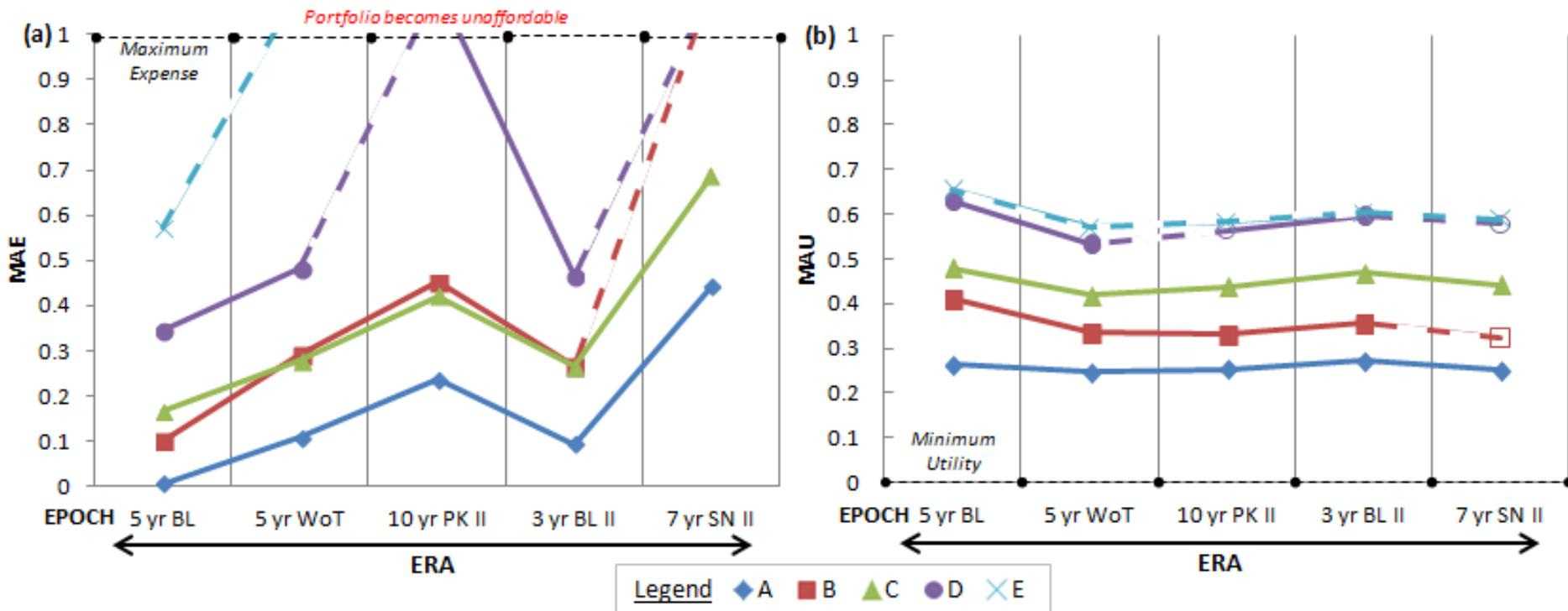
Peacekeep. (5yr) → Small Navy (5yr) → Major Conflict (5yr) → Peacekeep. (12yr) → Baseline (3yr)



# Single-Era Analysis

Promising portfolio designs independently explored in the constructed eras

Baseline (5yr) → War on Terror (5yr) → Peacekeeping (10yr) → Baseline (3yr) → Small Navy (7yr)



Single-Era Analysis enables exploration of the time-dependent affordability of promising CSG portfolios in one potential future

# Conclusion



Can aspects of MPT and EEA be combined to create sustained lifecycle *affordability* for engineering portfolios despite changing contexts?

- The PLEEAA method supports portfolio **design for affordability** during conceptual design
  - Considers new contexts before they arrive
  - Assesses lifecycle value sustainment of potential portfolios
- The case study displays how designers and acquisitions officers may explore promising CSG portfolio value in numerous potential futures
- The initial PLEEAA method accepts the following limitations:
  - Constituent system performance, costs and degradation uncertainties are not modeled
  - All performance attributes exhibit utility independence
  - Few portfolio stakeholders exist, or they may be represented in aggregate<sup>(Arrow, 1963)</sup>
  - The portfolio operates under *directed* management<sup>(Maier, 1998)</sup>

# Questions?

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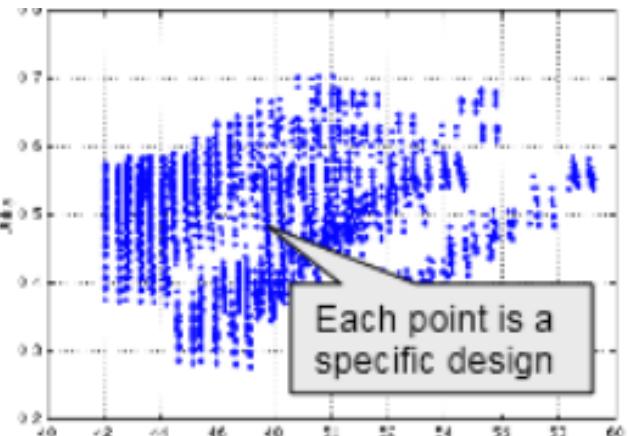
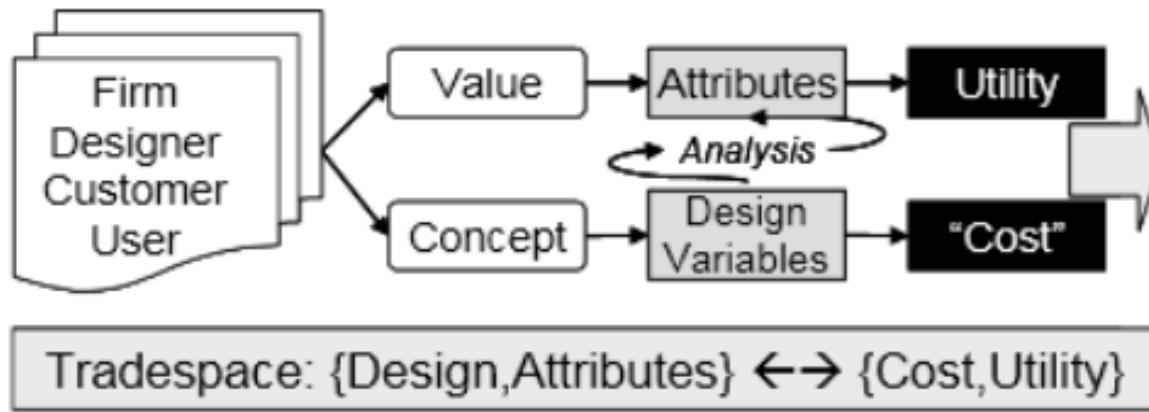
# Support Slides



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- [Multi-Attribute Utility Theory](#)
- [System, Program and Portfolio](#)
- [SoS and Portfolios](#)
- [Modern Portfolio Theory](#)
- [Wave Model](#)
- [Constituent Systems](#)
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- [Further Results](#)
- [Future Work](#)

# Multi-Attribute Tradespace Exploration

- Engineering portfolio design has traditionally revolved around Analysis of Alternatives studies concerning a few promising point designs
- Multi-Attribute Tradespace Exploration (MATE) enables designers to consider a far greater set of alternatives for affordability (Wu et.al, 2014)



# System, Program and Portfolio



Acquisition and development efforts face different challenges and opportunities contingent on the **scope** of the design abstraction

**System-Level:** Design that is inclusive of a singular major architectural element that is semi-independent from the remainder of the architecture



**Program-Level:** Design that requires joint consideration of multiple independent or semi-independent constituent elements such that each element fulfills a common set of capability requirements subject to identical stakeholder value metrics

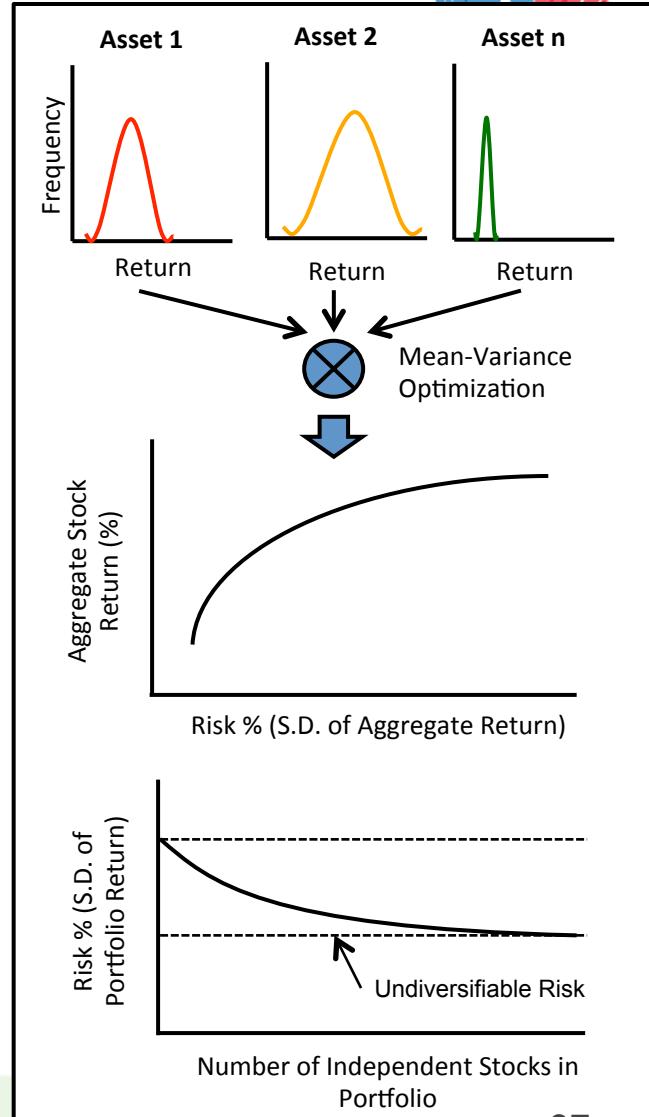


**Portfolio-Level:** Design that seeks to create a collection of heterogeneous assets, both from legacy and new sources, that can collectively provide a set of emergent capabilities through the aggregate performance of each constituent system

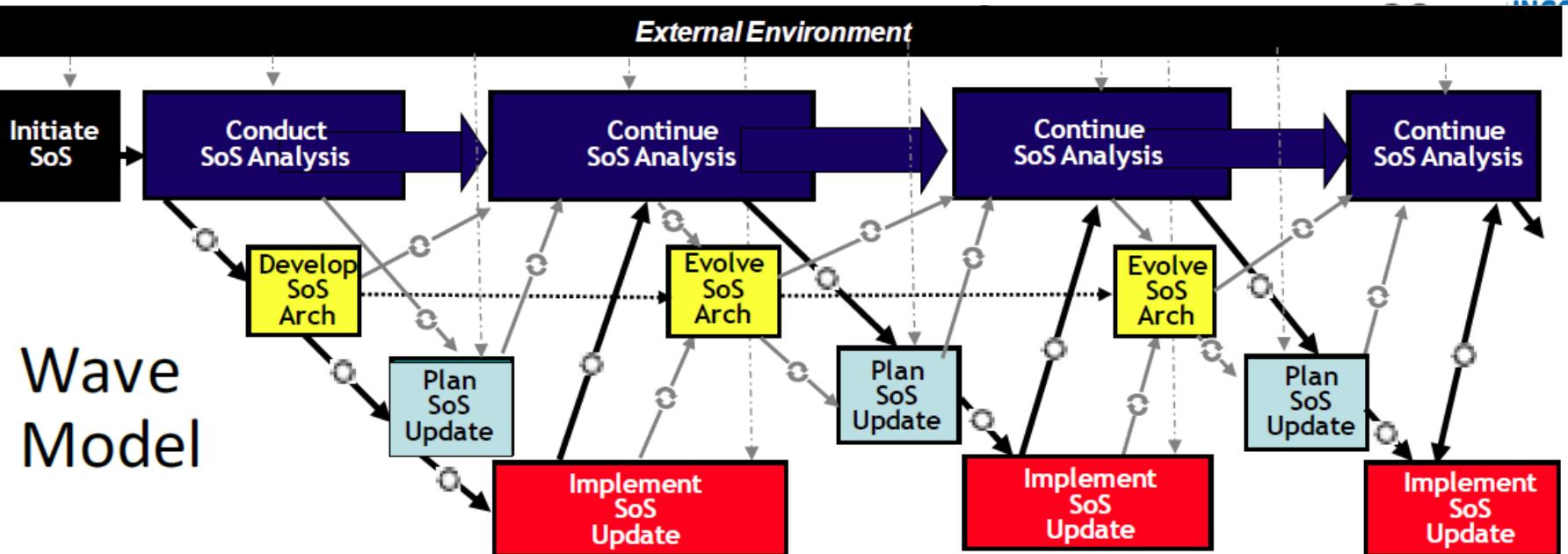


# Modern Portfolio Theory

- Utilized by financial institutions and operations research since the 1950's
- Constructs groupings of investments that maximize return (utility) subject to an acceptable threshold of risk (cost)
- Result in an "efficient frontier" of potential investment sets
- Relies upon **negative trending covariance** in diversified assets to reduce aggregate risk, or **mean-variance optimization**
- A variety of MPT derivatives exist that introduce non-normally distributed risks and semi-variance among assets



# Wave Model of SoS Design



(Baldwin, Dahmann , Rebovich, Lane, & Lowry, 2011)

- “Time-sequenced”, or adaptive approach to SoS construction
- Iterates to identify and respond to uncertainty/changes in context
- Risks requirement creep, spiraling design and rising costs



# Constituent Systems Considered

Potential Constituent System	Legacy Variants	New Variants	Upgrade Variants	Selected for Case Study
Next Generation Combat Ship (NGCS)	0	6	0	6 new variants
Arleigh Burke Class Destroyer	3	2	2	All 7 variants
Ticonderoga Class Cruiser	2	0	0	1 legacy variant
Zumwalt Class Destroyer	0	1	0	1 new variant
Nimitz Class Aircraft Carrier	1	0	0	1 legacy variant
Los Angles Class Submarine	1	0	0	1 legacy variant
Virginia Class Submarine	1	0	0	1 legacy variant
Supply Class fast combat support ship	1	0	0	1 legacy variant
F/A-18 Aircraft	4	0	0	None
F/A-35 Aircraft	2	0	0	None
E-2 Aircraft	2	0	0	None
EA-6B Aircraft	1	0	0	None
EA-18G Aircraft	1	0	0	None
SH-60 Helicopter	5	0	0	None
C-2A Helicopter	1	0	0	None

# Complementary and Substitute Systems



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## Complementary Systems

- Value delivery enhanced in at least one performance attribute
- Gain new capability in a performance attribute
- Often results from a change to the system's CONOPS

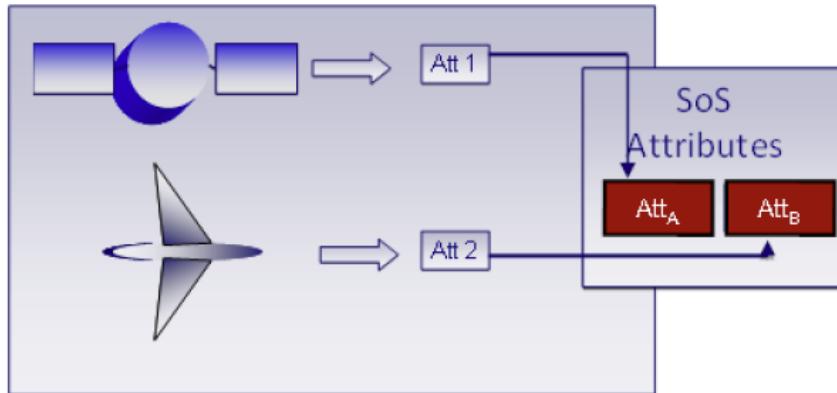
## Substitute Systems

- Simultaneous, overlapping value delivery in a performance attribute
- Often dependent upon the CONOPS
- Systems may be substitute in one performance attribute, but not necessarily in others

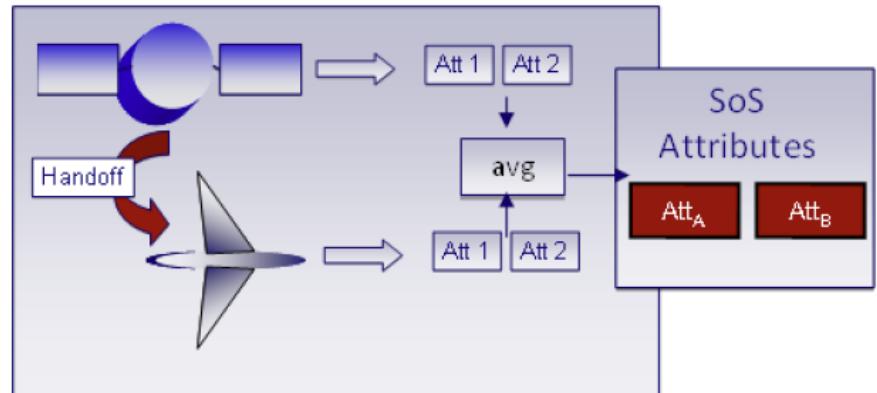
**PLEEAA, provides two mechanisms to address complementary and substitute systems through the capability tree architecture**

1. SME matching with potential interaction opportunities
2. Level of Combination Complexity adjustment factors (Chattopadhyay, 2009)

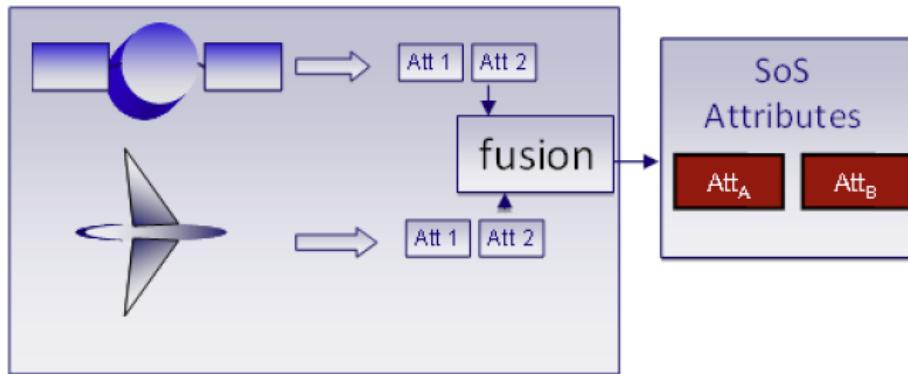
# Performance Aggregation Approaches for Constituent Systems



'Low' Level Combination



'Medium' Level Combination

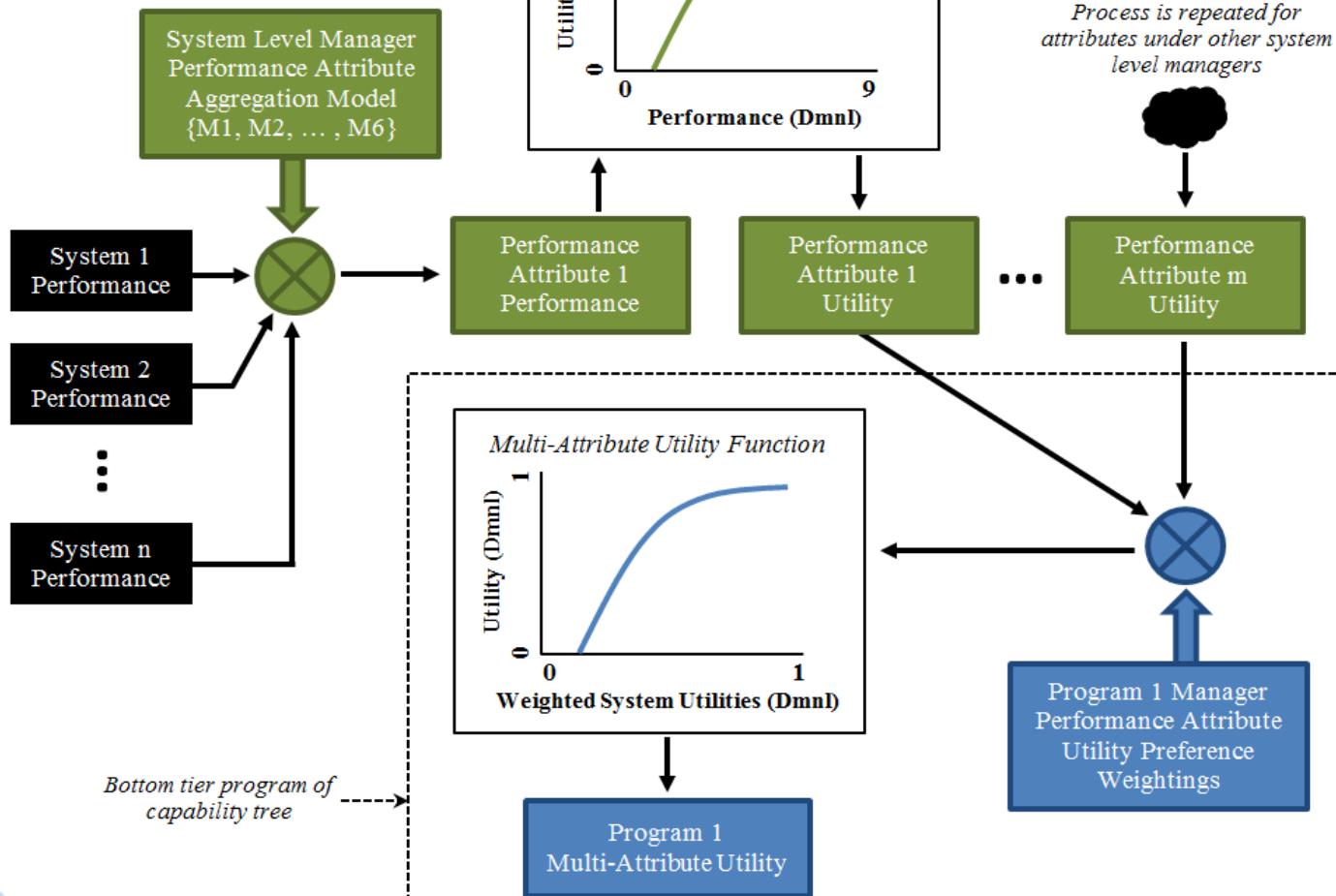


'High' Level Combination

(Chattopadhyay, 2009)

# Performance Aggregation and Utility Development

- system level tier of hierarchy
- 3<sup>rd</sup> tier of hierarchy





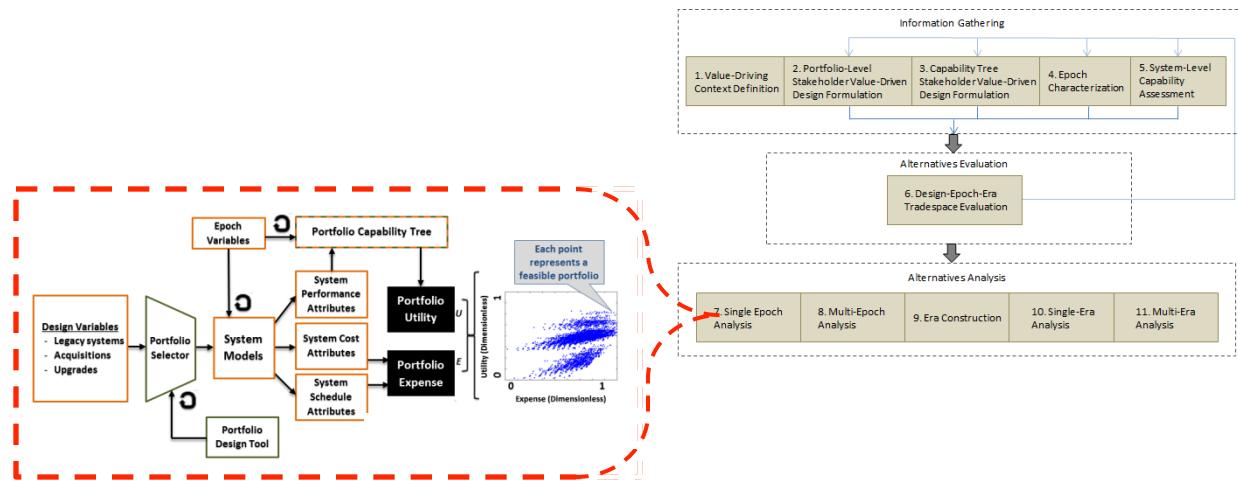
# Performance and Cost Aggregation Models for Constituent Systems

Model	Description of Approach
M1	<p>A summation of the average performance of each major system class:</p> $\Sigma[\Sigma[(v_{NGCS} * \varphi), (v_{AB,Tico} * \varphi), (v_{ABIII,Zmwlt} * \varphi)]/3, (v_{LA,VA} * \varphi), (v_{Nimitz} * \varphi), (v_{Supply} * \varphi)]$ <p><math>v</math> is the performance capability of the system for the attribute in consideration</p> <p><math>\bar{v}</math> represents the average performance capability of systems in that category</p> <p><math>\varphi</math> is a multiple unit function which adjusts performance if more than one unit of a system type is present: <math>\varphi = \sum_{i=1}^n \frac{1}{i}</math> where <math>n</math> is the number of units of a system type</p>
M2	<p>The mean of all non-zero constituent system performance capabilities:</p> $(\Sigma_{i=1}^s (v_i * \varphi > 0))/s$ <p><math>s</math> is the number of different potential systems (19 for the CSG case study)</p>
M3	<p>The maximum performance from any constituent system performance ranking:</p> $V_{i=1}^s (v_i * \varphi)$
M4	<p>A summation of the constituent system performance capabilities, weighted by the relative contribution of the constituent system to the highest preferred program manager attribute:</p> $\Sigma_{i=1}^s \left( v_i * \varphi * \frac{x_i}{x_p} \right)$ <p><math>x</math> is the system performance capability for the most desired program manager attribute</p> <p><math>x_p</math> is the portfolio performance capability for the most desired program manager attribute</p>
M5	<p>The mean of all constituent system performance capabilities:</p> $(\Sigma_{i=1}^s (v_i * \varphi))/s$
M6	<p>The summation of all constituent system performance capabilities:</p> $\Sigma_{i=1}^s (v_i * \varphi)$

# Responsive Systems Comparison Augmentation with PLEEAA



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# Promising Portfolio Constituent System Investment Comparisons

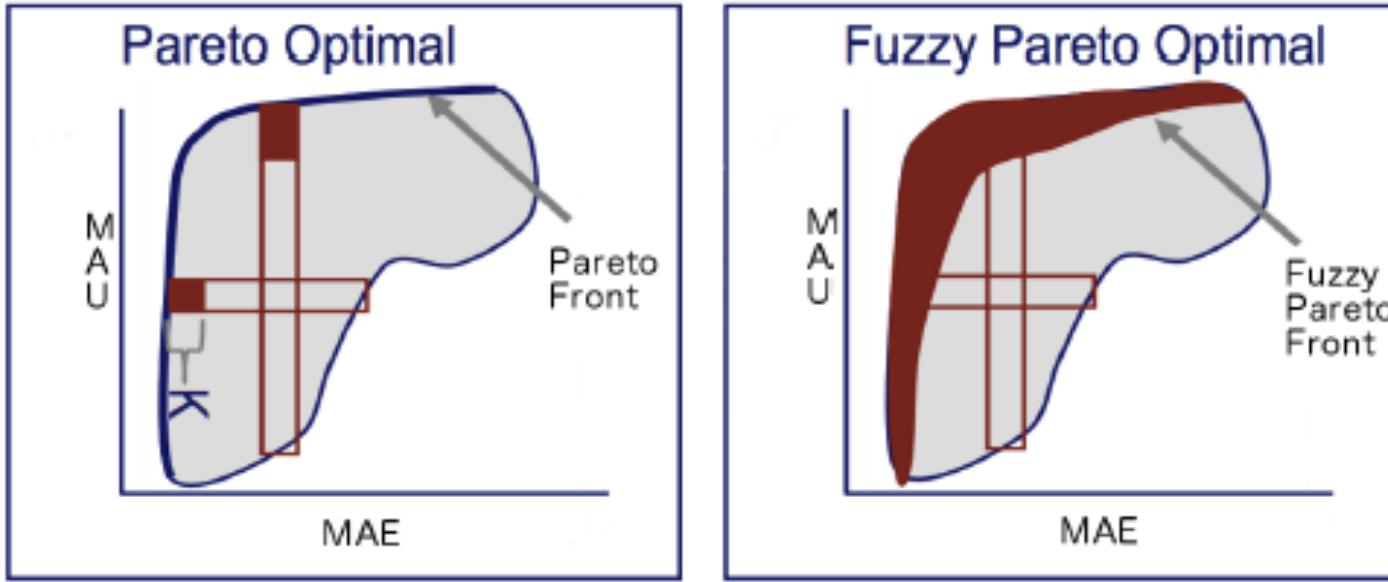


		Potential Constituent Systems																	
		Different Systems																	
Promising Portfolios	A	0	reference portfolio	reference portfolio	reference portfolio	reference portfolio	reference portfolio	reference portfolio	reference portfolio	reference portfolio	reference portfolio	reference portfolio	reference portfolio	reference portfolio	reference portfolio	reference portfolio	reference portfolio	reference portfolio	reference portfolio
	B	2	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio			
	C	0	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio			
	D	1	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio			
	E	2	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio	similar to reference portfolio			
			system in current portfolio	reference portfolio	similar to reference portfolio	different than reference portfolio													

- Portfolios A and C are contain the identical constituent systems, albeit varying numbers of each system
- Well performing portfolios with similar composition may identify complementary constituent system interaction or latent value robustness



# Fuzzy Normalized Pareto Trace



- Describes the percent of epochs for which a design is within a certain threshold of the efficient front
- Width of threshold defined by a constant, K

Useful concept to assess portfolio performance  
across multiple epochs and reveal *passive robust solutions*

# Fuzzy Normalized Pareto Trace

Portfolio	NPT	5% fNPT	10% fNPT	20% fNPT
A	1	1	1	1
B	0.8	0.8	0.8	0.8
C	0.6	0.8	1	1
D	0.8	0.8	0.8	0.8
E	0.4	0.8	0.8	0.8

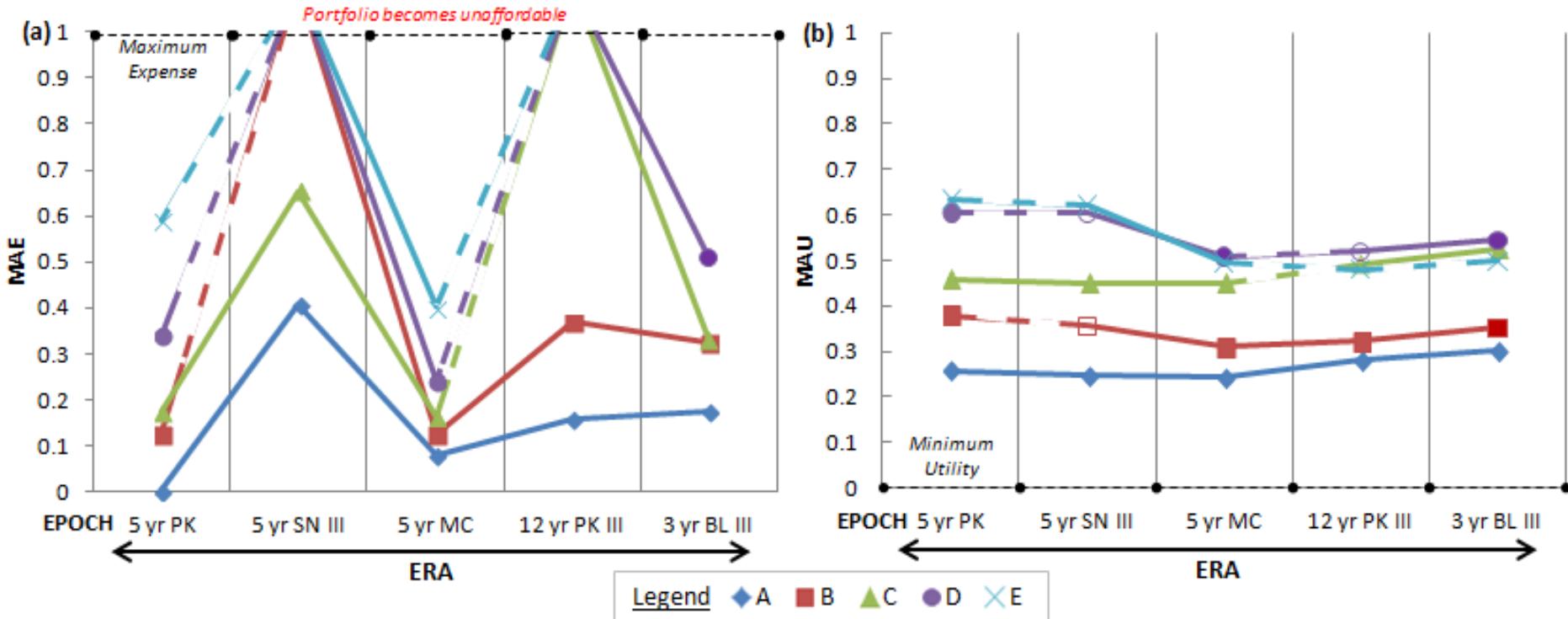
- Portfolio A is on efficient front in all epochs considered
- While Portfolio C is only on the efficient front in 60% of the epochs, it lays within 10% of the Pareto front for all five epochs
- Not other portfolios are within 20% of the efficient front for all epochs indicating significantly increased cost or reduced performance



# Single-Era Analysis

Promising portfolio designs independently explored in the constructed eras

Baseline (5yr) → War on Terror (5yr) → Peacekeeping (10yr) → Baseline (3yr) → Small Navy (7yr)



Single-Era Analysis enables exploration of the time-dependent affordability of promising CSG portfolios in one potential future

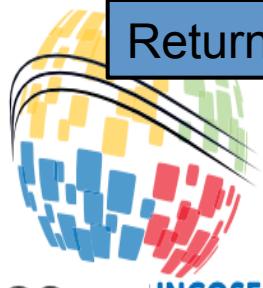


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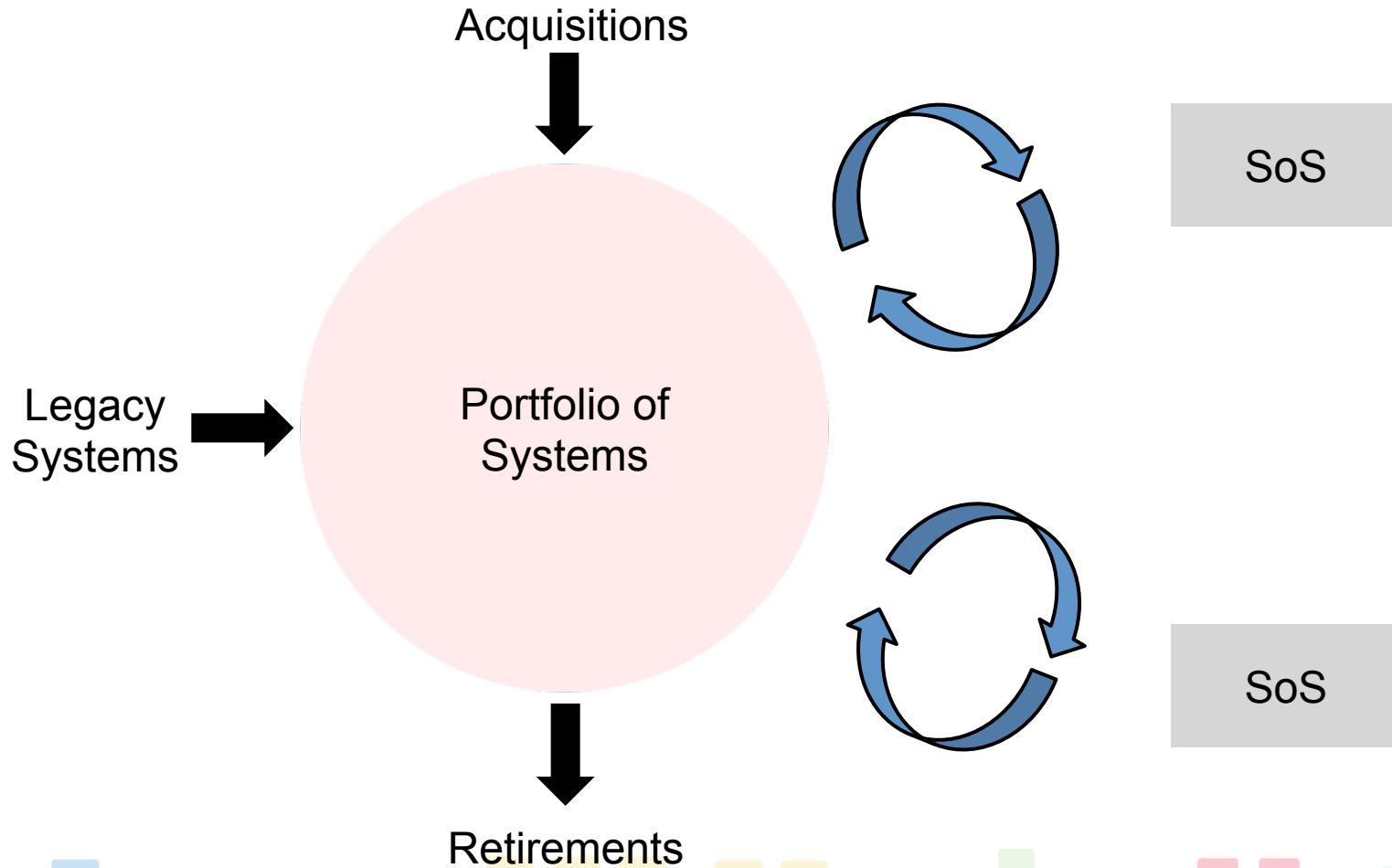
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# SoS Relation to Portfolios

- A **System of Systems** is a dynamic network of constituent systems that exhibit varying levels of operational and managerial independence, but operationally interact so as to achieve mutually desired, oftentimes emergent, capabilities (Maier, 1998)
- A **Portfolio** is a construct that describes a collection of assets, acquisition programs, and research programs that are jointly invested in to exploit qualities of the set, regardless of whether the assets are operationalized independently or participate in a SoS



# SoS Relation to Portfolios





# Value-Centric Design Methodologies

- A **Value-Centric Design Methodology**, as opposed to a requirements or cost-related design approach, link together **physics** and **cost-based** system models with a **valuation** model to provide system selection criteria based on *derived system value* (Ross et al., 2010a)
- Value-Centric Design Methodologies include
  - Net Present Value
  - Cost-Benefit Analysis
  - Multi-Attribute Utility Theory
  - Cumulative Prospect Theory
  - Value Functions
  - Analytic Hierarchy Process
  - Technique for Order Preference by Similarity to Ideal Solution



# Value-Centric Design Methodologies

- Ross et al. 2010a presents a framework for assessing how well the conditions and assumptions of an analysis meet the needs and limitations of the various VCDM techniques
- MAUT was deemed the most appropriate VCDM for engineering portfolio design
  - Value is an aggregation of a set of benefits relative to their net cost; it is **difficult to monetize**
  - Value is derived from **multiple benefits and costs**, not simply profits
  - Mutual Utility Independence versus Mutual Additive Independence (preferential independence) enables **consideration of substitution and complementary affects** among attributes



# Multi-Attribute Utility Theory (MAUT)

Governing Equation:

$$K * U(\hat{X}) + 1 = \prod_{i=1}^n (K * k_i * U(X_i) + 1)$$

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Normalization Constant:

$$K = -1 + \prod_{i=1}^n (K * k_i + 1)$$

If the performance attribute swing weights sum to one (i.e. preferential independence of attributes),  $K = 0$

Additive Utility Function:

$$U(\hat{X}) = \sum_{i=1}^n k_i * U(X_i)$$

# Future Work



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- The work conducted in this research represent initial efforts to extend EEA to the portfolio-level of design
- Numerous opportunities exist to improve the PLEAA method and expand the set of problems to which it may be applied:
  - Stochastic/probabilistic modeling for system-inherent uncertainty
  - Dynamic entry and exit of systems from portfolios (technology infusion)
  - Usage of multiplicative utility equation to consider utility dependent attributes
  - Enhanced collaboration costs and “likelihood of participation” factors (Shah, 2013)
  - Design for “graceful degradation” capability
  - Co-design features to identify system-level design requirements to complement portfolio
  - Expanded schedule cost factors
- A regime of validation tests also need to be conducted