



**32**<sup>nd</sup> Annual **INCOSE**  
international symposium  
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# **How to faithfully model systems composed of millions of parts?**

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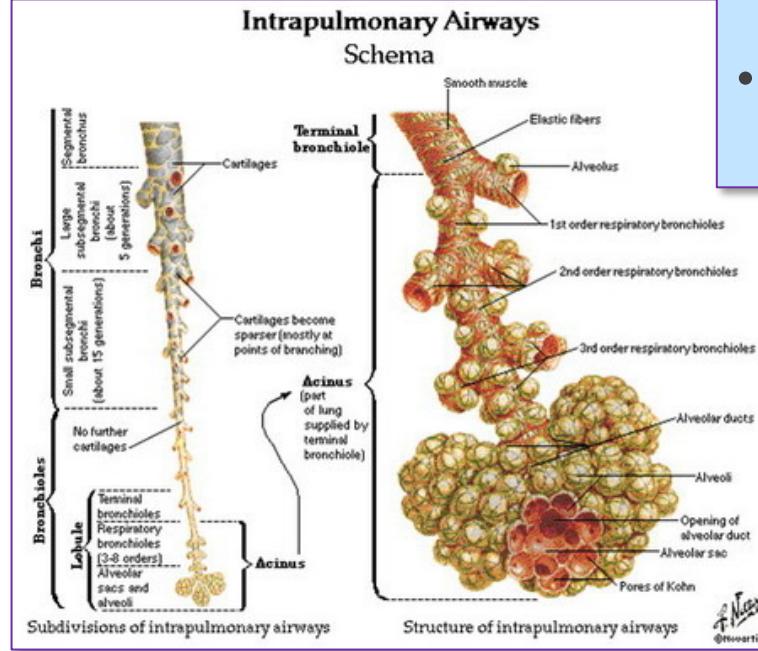
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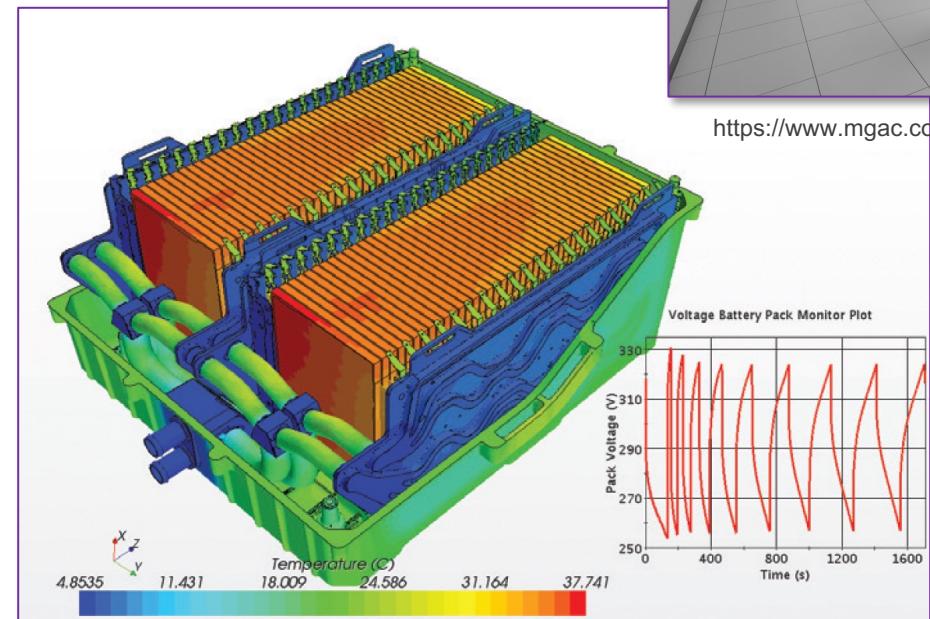
# The Challenge – Modeling Ultra Complex Systems



- Critical systems in our world
- Thousands or millions of elements
- Impossible to model directly by hand



<https://web.as.uky.edu/Biology/faculty/cooper/KMA/lungs%20pdf.pdf>



Siemens-SW-Designing-tomorrows-Li-ion-battery-White-Paper\_tcm27-101035.pdf



<https://www.mgac.com/blog/6-models-of-the-modern-data-center/>



Suppose we need to model the behavior of a single user session of an application in a data center.

## Example 1 – Data Center



# Example: User Session in a Data Center



Consider the problem of modeling a single user session of an enterprise software application hosted somewhere in a data center.

The data center consists of many rows of 24 inch / 42 U equipment racks.



# Example: User Session in a Data Center

A standard equipment rack is 24 inches (~600mm) wide and has 42 evenly spaced mounting holes on each side.



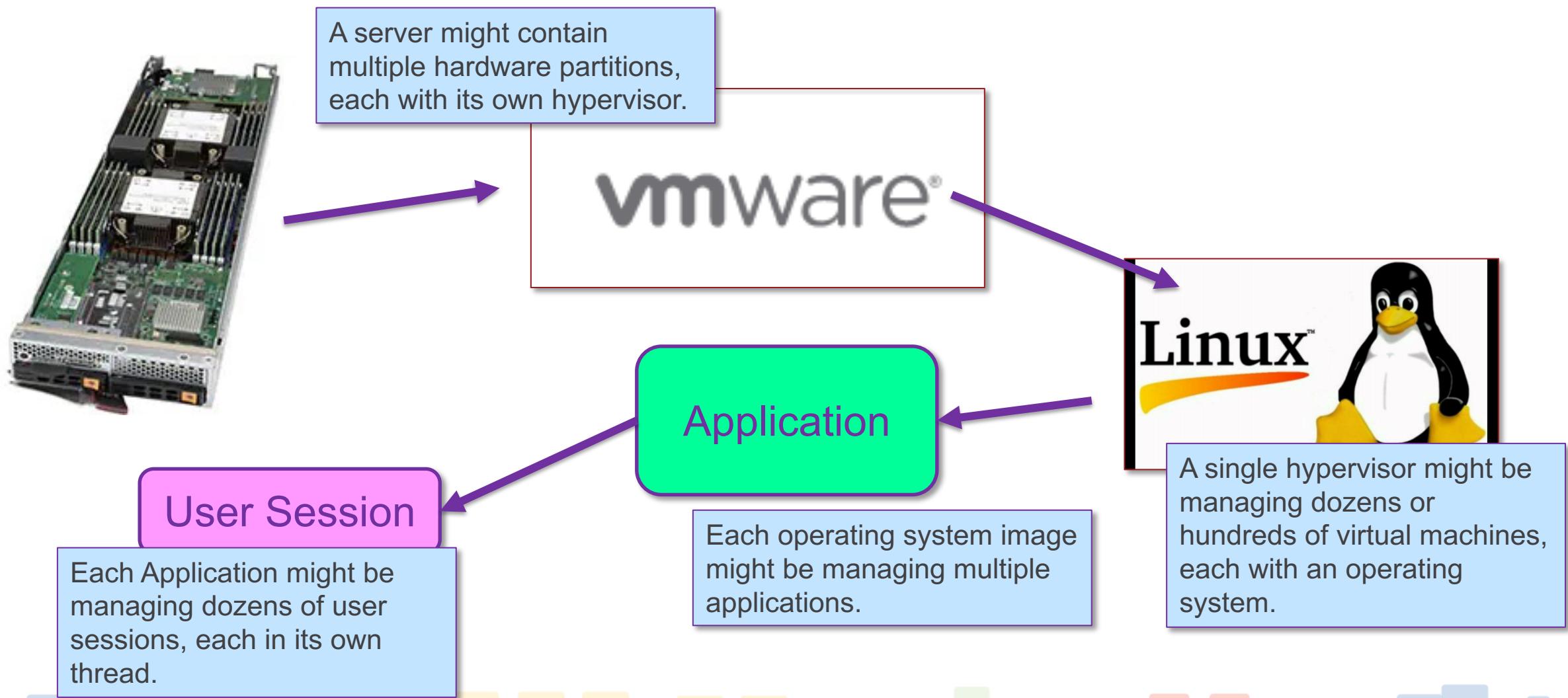
IT equipment comes in multiples of "U" vertical width. Here is a typical "6U" blade server chassis with a number of slots.



Each slot in the blade chassis contains a server blade with 1 to 4 server-class microprocessors, each with as many as 40 cores.

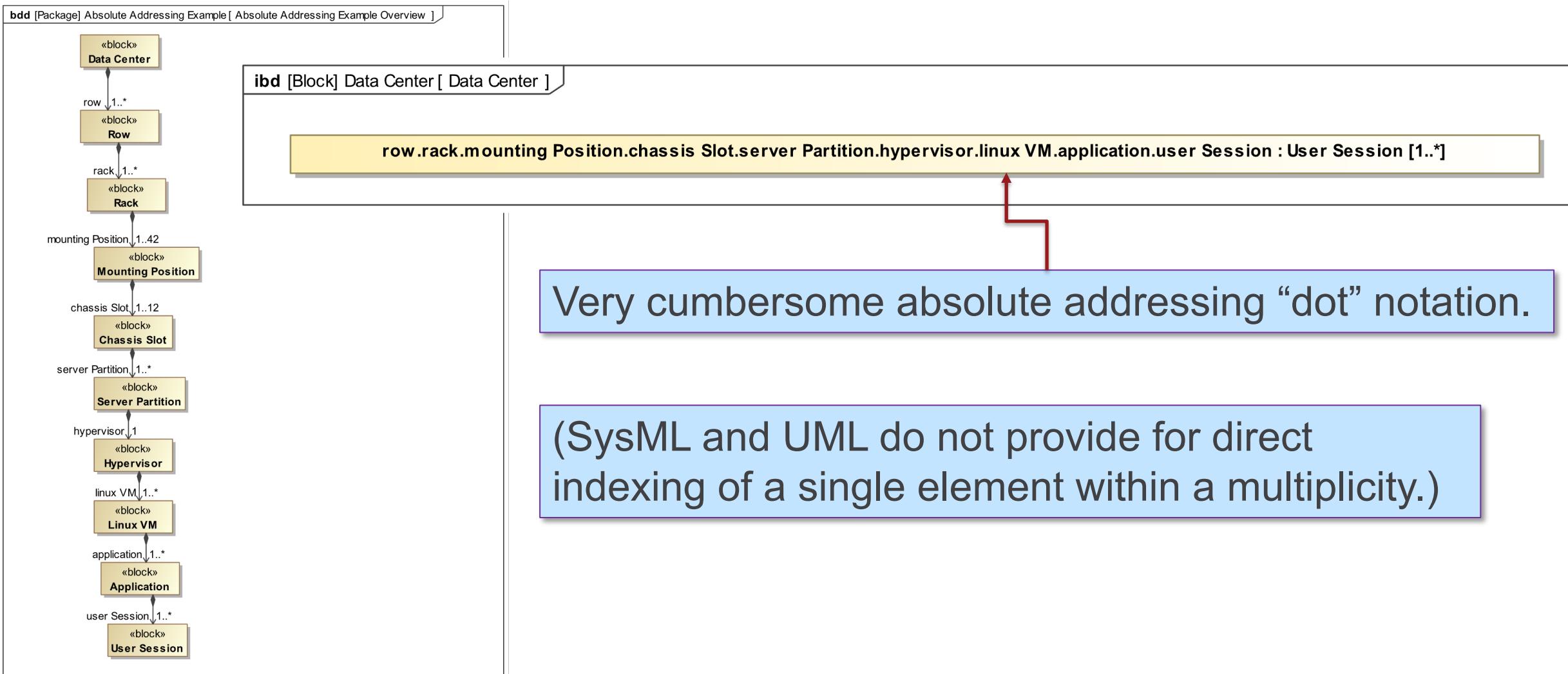


# Example: User Session in a Data Center





# Example: SysML Approach

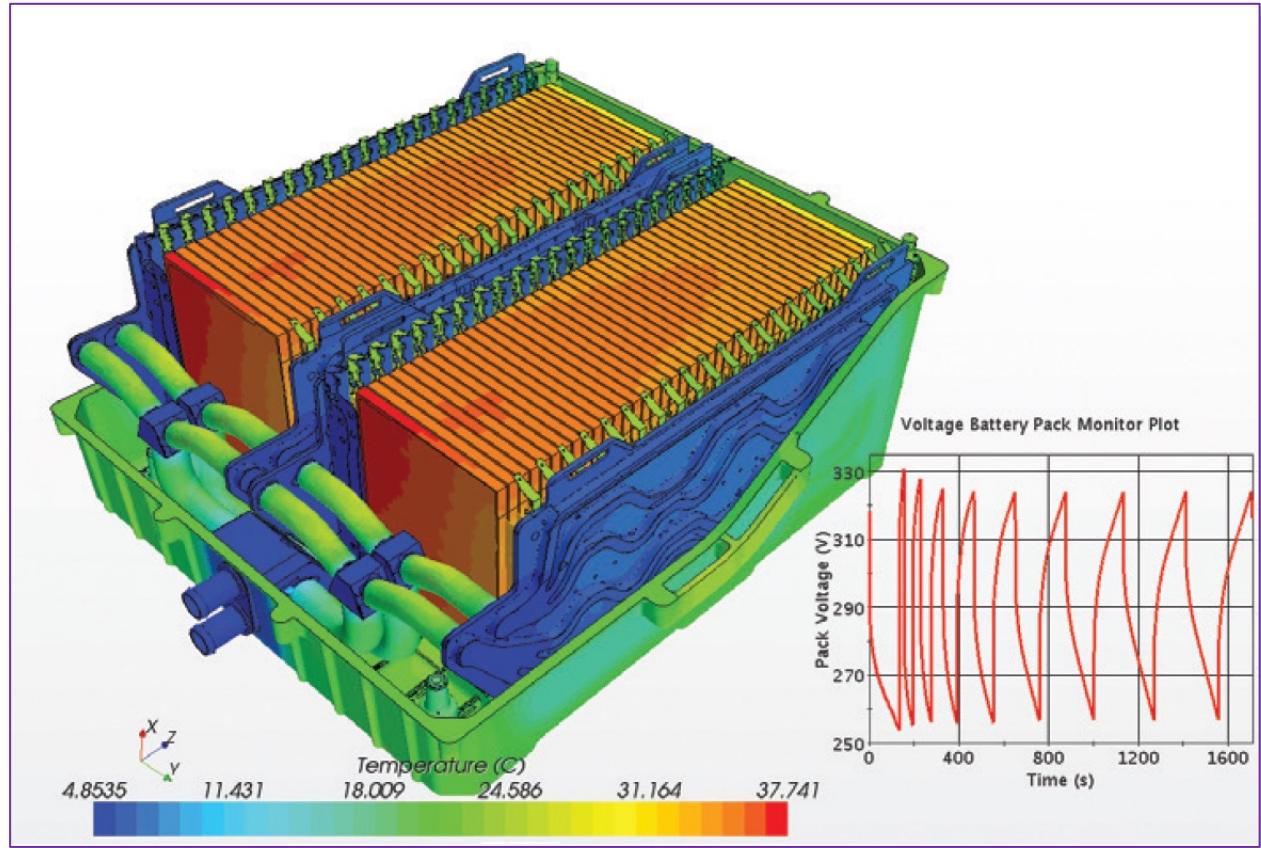




What if we need to directly model an automotive battery pack?

## Example 2 – Battery Pack

# Battery Pack

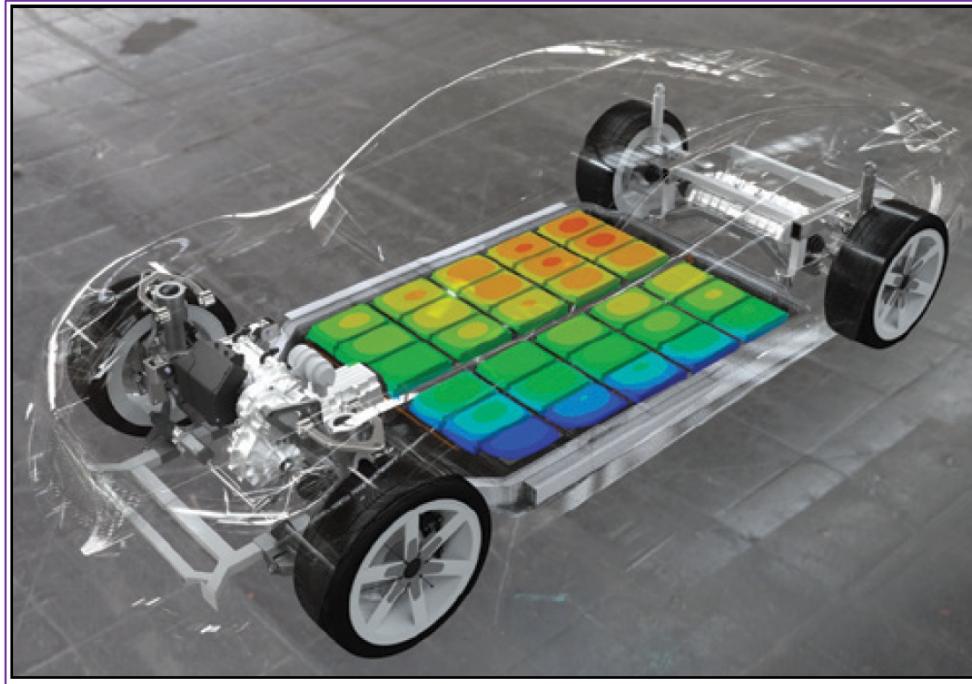


Siemens-SW-Designing-tomorrows-Li-ion-battery-White-Paper\_tcm27-101035.pdf

- Thousands (not millions) of elements.
- However, the “interfaces” to the elements depend heavily on where the specific element is in the physical structure of the pack.



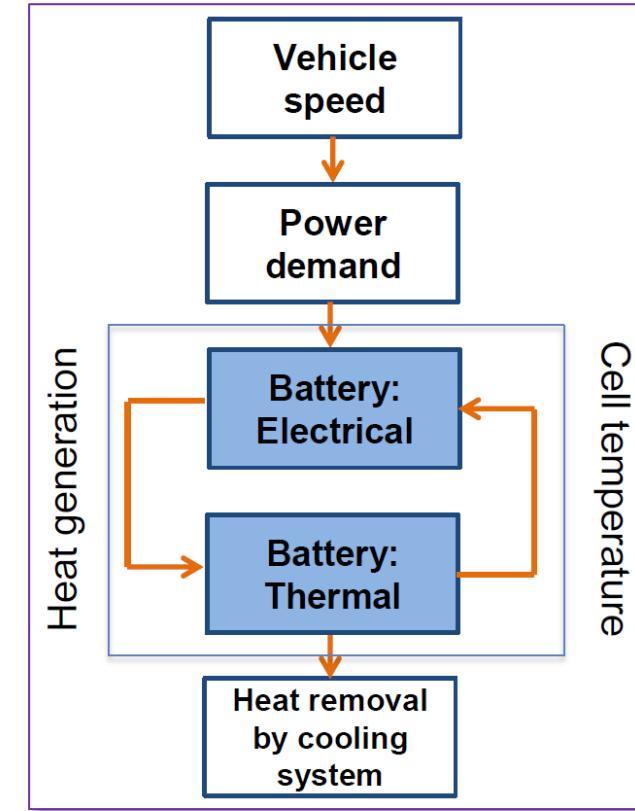
# Battery Simulation



SAE Battery & Electrification Technology, May 2022

- Although cells may be identical, hot and cold areas in a battery will depend on the location of the cells

- Electrical and thermal performance are tightly coupled.



Development and Application of Liquid-cooled Lithium-ion Battery Pack Thermal Model, Model based approach by using GT-SUITE - North American GT Conference 2017, Fiat Chrysler Automobiles



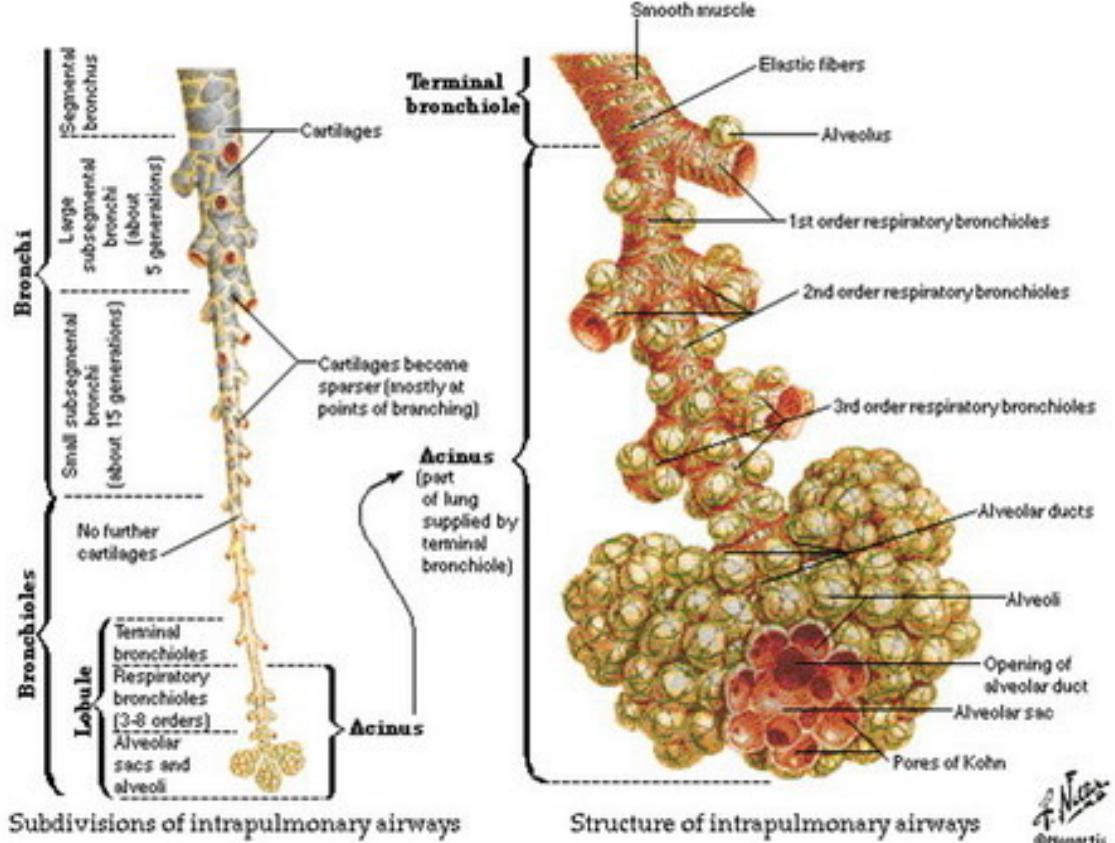
Modeling the gas exchanges in a human lung would be complicated as well.

## Example 3 – Human Lung

# Human Lung



## Intrapulmonary Airways Schema

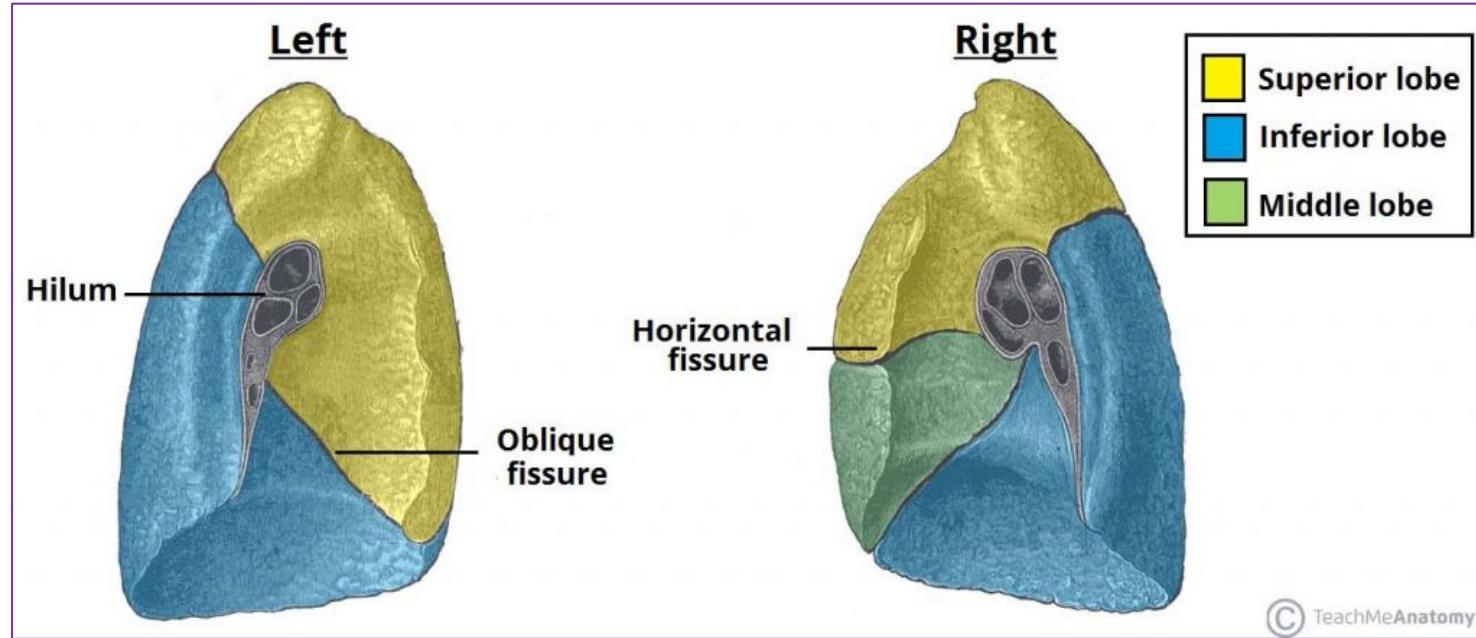


- About 28 orders of division in the tracheo-bronchial tree.
- Estimated 200-400 million alveoli with 40-80 square meters of surface area.

<https://web.as.uky.edu/Biology/faculty/cooper/KMA/lungs%20pdf.pdf>



# Human Lung Structural Patterns



<https://teachmeanatomy.info/thorax/organs/lungs/>

- Although the lungs appear to be uniformly structured, actually they aren't
  - Right and left lungs are different.
  - The lobes within each lung are different.
  - A straight multiplicity model will not be sufficient.



First and foremost, the model has to help the users understand the system.

## Challenges of Modeling



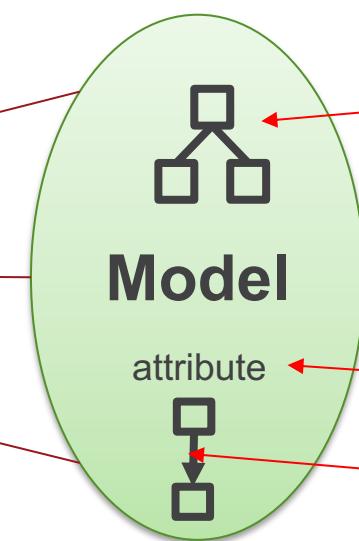
# Expectation about Models

Human complexity

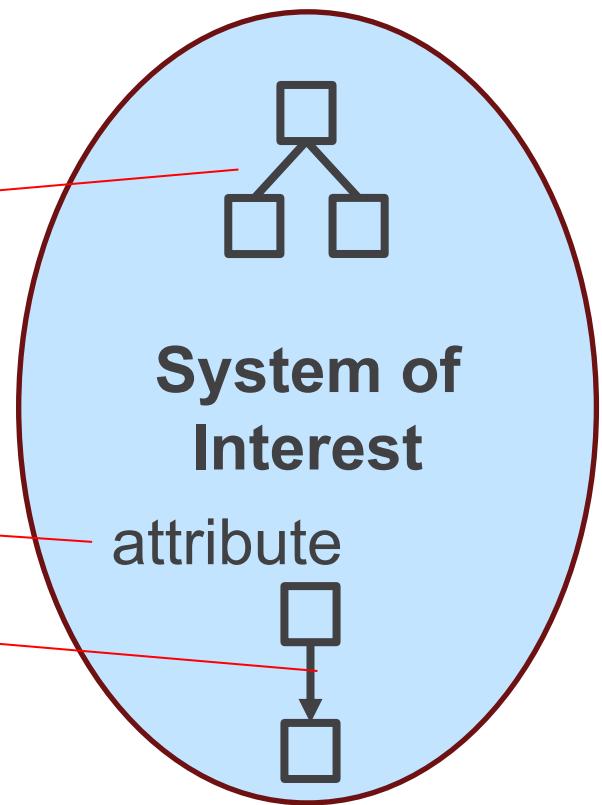


**Analyst**  
« Users »

**Accessible**



System complexity

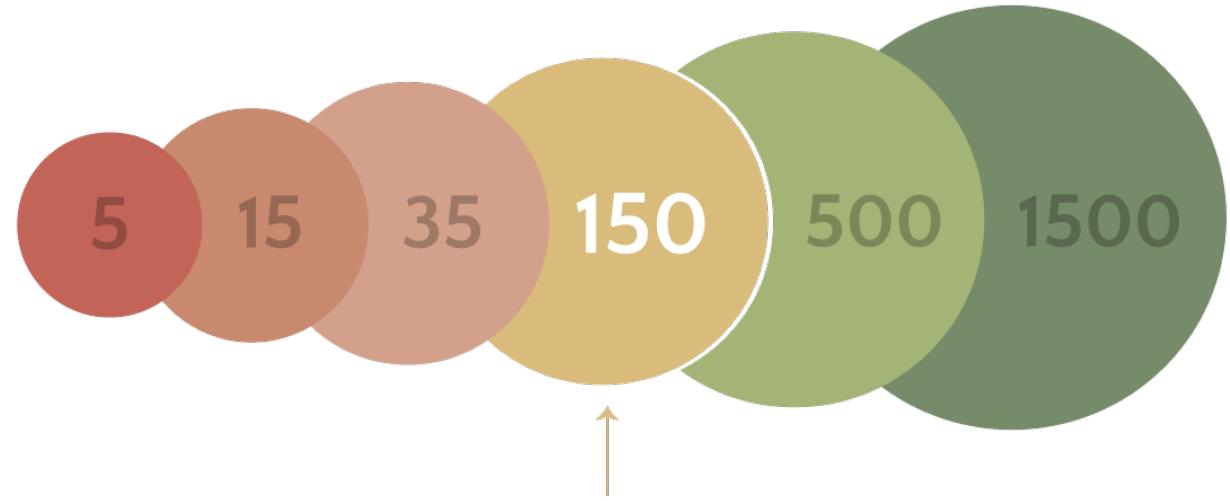


**Faithful**



# Dunbar's Number

- Widely discussed in studies of social media
- Exact number is hard to nail down, but general effect is well understood.
- Many examples of military and corporate structures organized around 200.
- **Assertion:** Although usually thought of as related to human relationships, *there is similar limit of the number of elements in a model that a human can think about before becoming overwhelmed.*



## Dunbar's Number

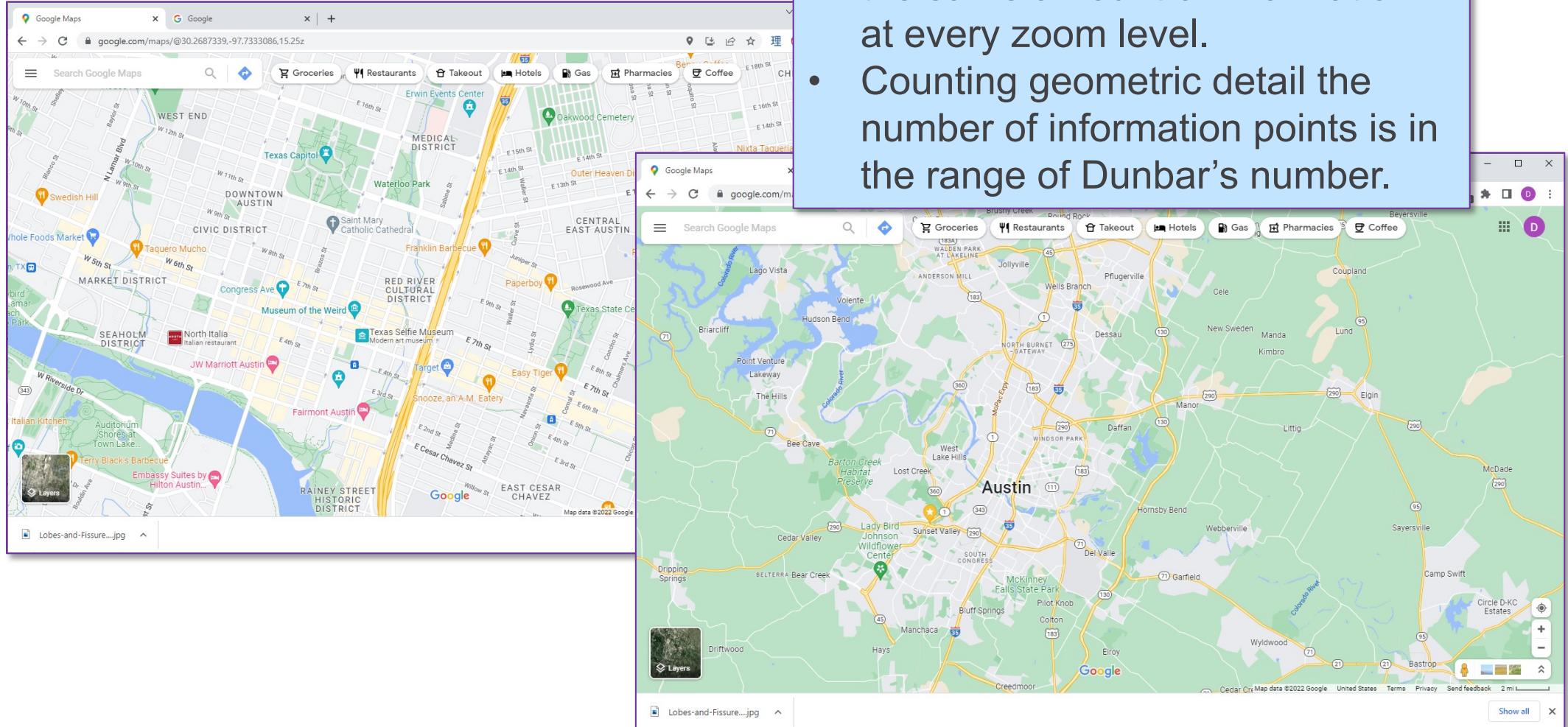
*the max number of relationships a person can maintain*

[https://en.wikipedia.org/wiki/Dunbar%27s\\_number](https://en.wikipedia.org/wiki/Dunbar%27s_number)

# Google Maps



- Google Maps presents roughly the same amount of information at every zoom level.
- Counting geometric detail the number of information points is in the range of Dunbar's number.





# Miller's Law

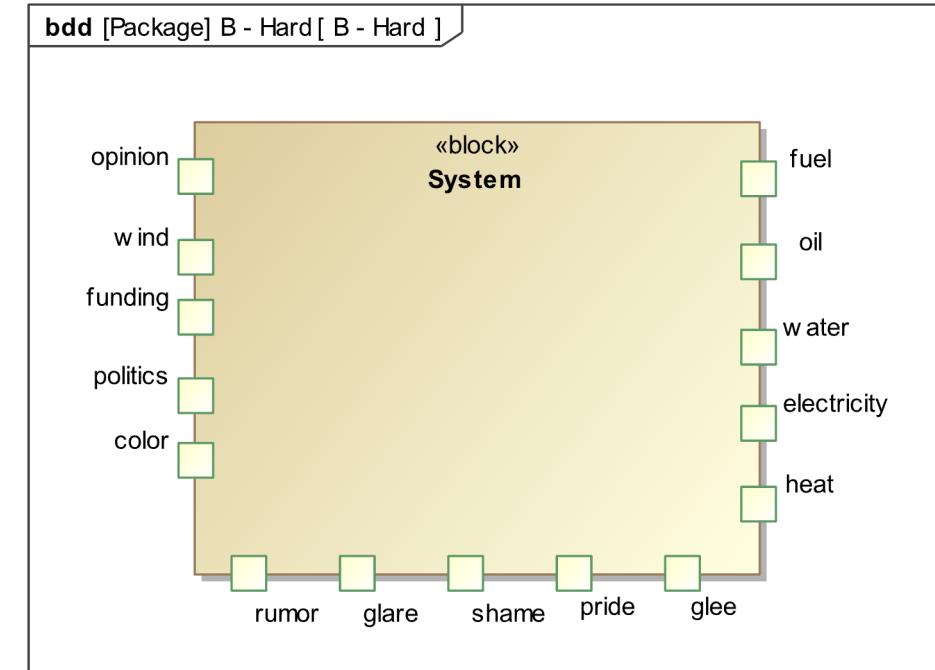
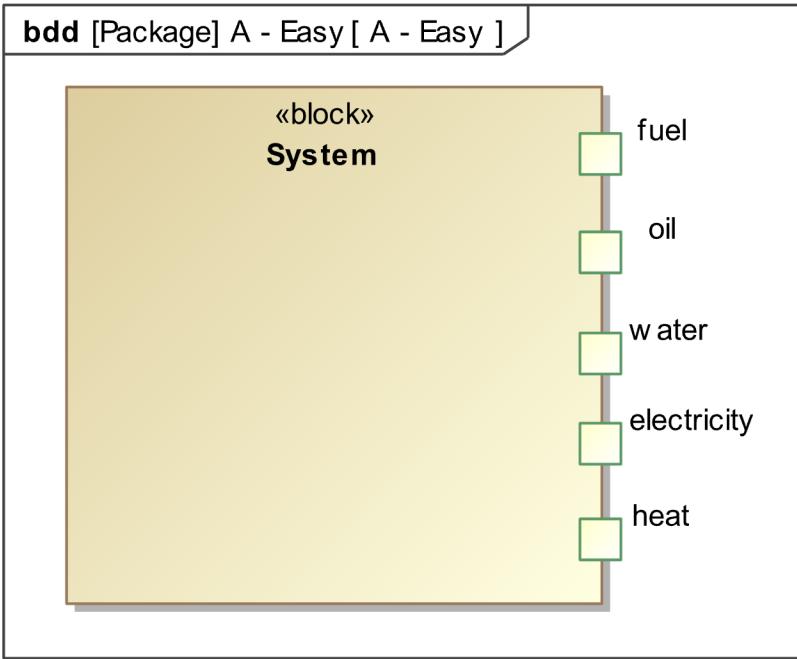
- 1956 article in Psychology Review by George Miller of the Harvard University Department of Psychology
- Limits of short-term memory
- **Assertion:** Although usually thought of as related to human short term memory, *there is similar limit of the number of similar elements in a model diagram before users start having difficulty comprehending the diagram*

“Seven plus or minus two”

[https://en.wikipedia.org/wiki/The\\_Magical\\_Number\\_Seven,\\_Plus\\_or\\_Minus\\_Two](https://en.wikipedia.org/wiki/The_Magical_Number_Seven,_Plus_or_Minus_Two)



# Ports Example



- The system with 5 ports is easy to think about

- The system with 15 ports requires a lot more concentration to understand.

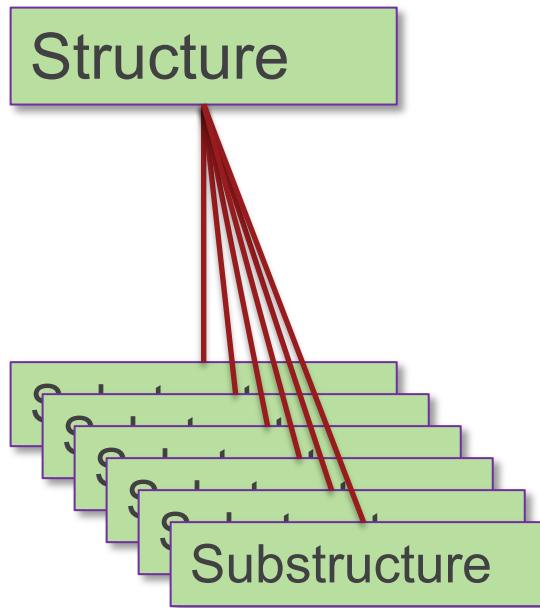


Clearly, a modular approach will be needed

## Complexity Reduction Strategy

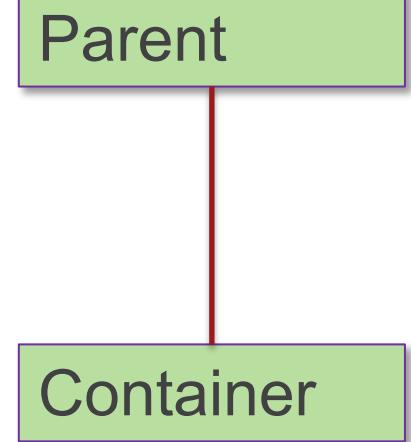


# Approach: Simplifying Hierarchical Relationships



The real system is like this.

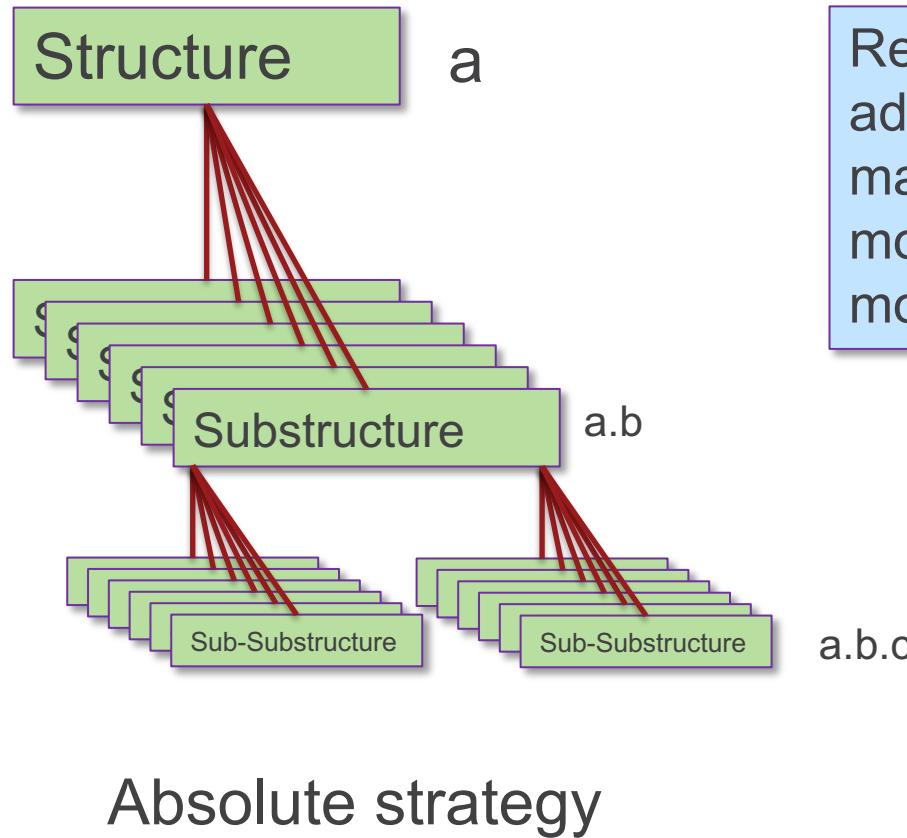
The simpler modeling helps us with the Dunbar Number and Miller's Law problem



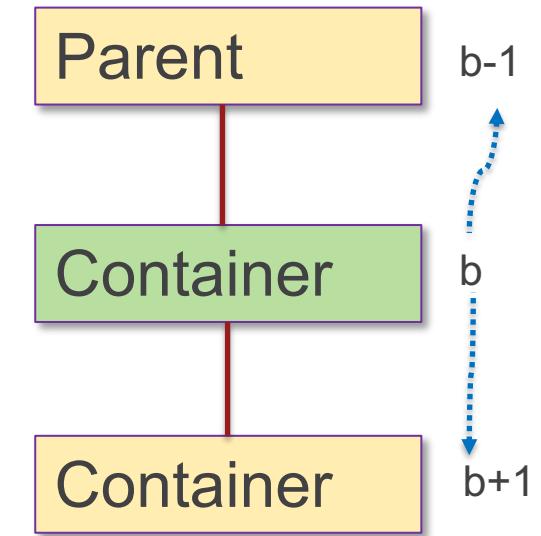
We model this.



# Approach: Absolute versus Relative References



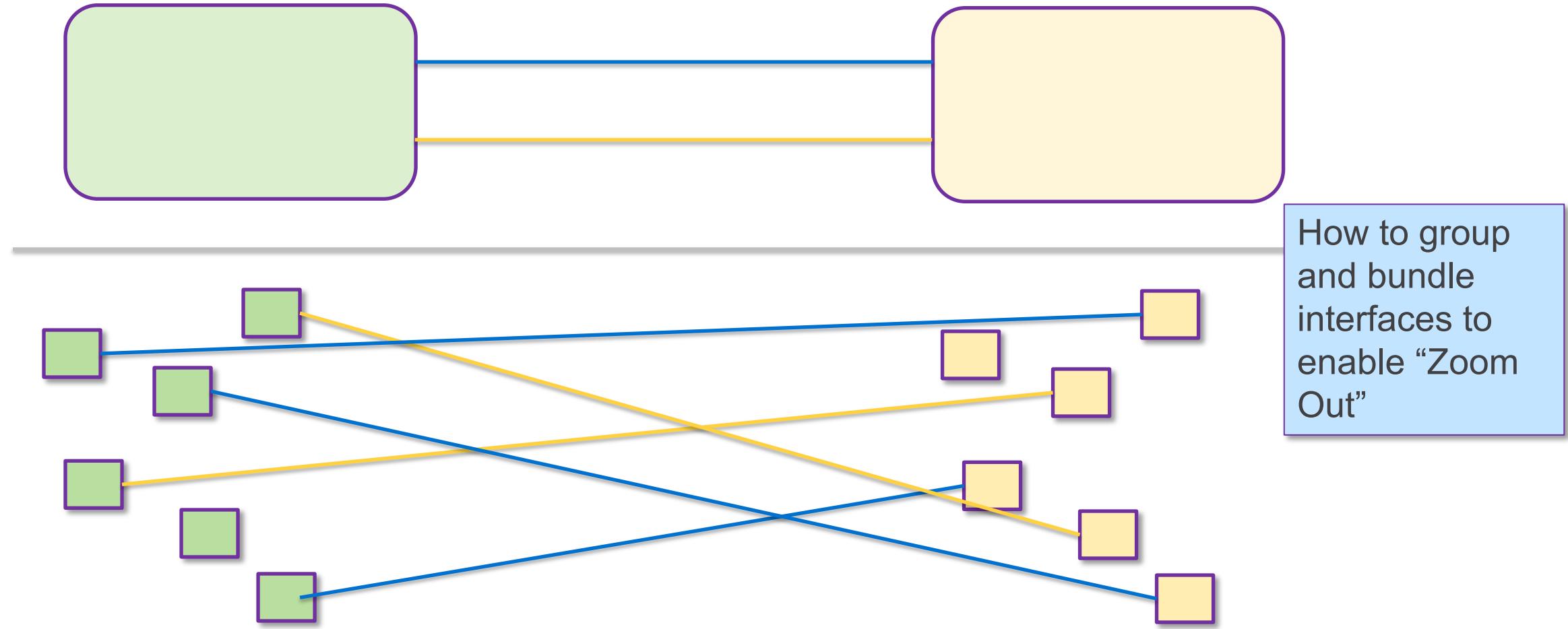
Relative addressing makes our model more modular.



**Relative strategy**



# Approach: Reducing Interface Complexity





Although the cells seem similar, their thermal interfaces depend on their location in the structure.

## Modeling the Battery Pack



# Parametric Models an Example

## Case of a battery structure:

We present an example.

Here parameters are lists of integers

`m = [1..6] several modules [m]`

sl = [1..3] number of slavemodules[sl] per [m]

cp = [1..32] number of cell packs [cp per [s]] [Link in /mmin](#)

c = [1..30] number of cells[c] per [cp]

### 8.1.1.1

Some syntactic rules are needed:

« link[m][s]min»

if:  $sl \equiv slmin$

iii.  $Si = Si_{min}$

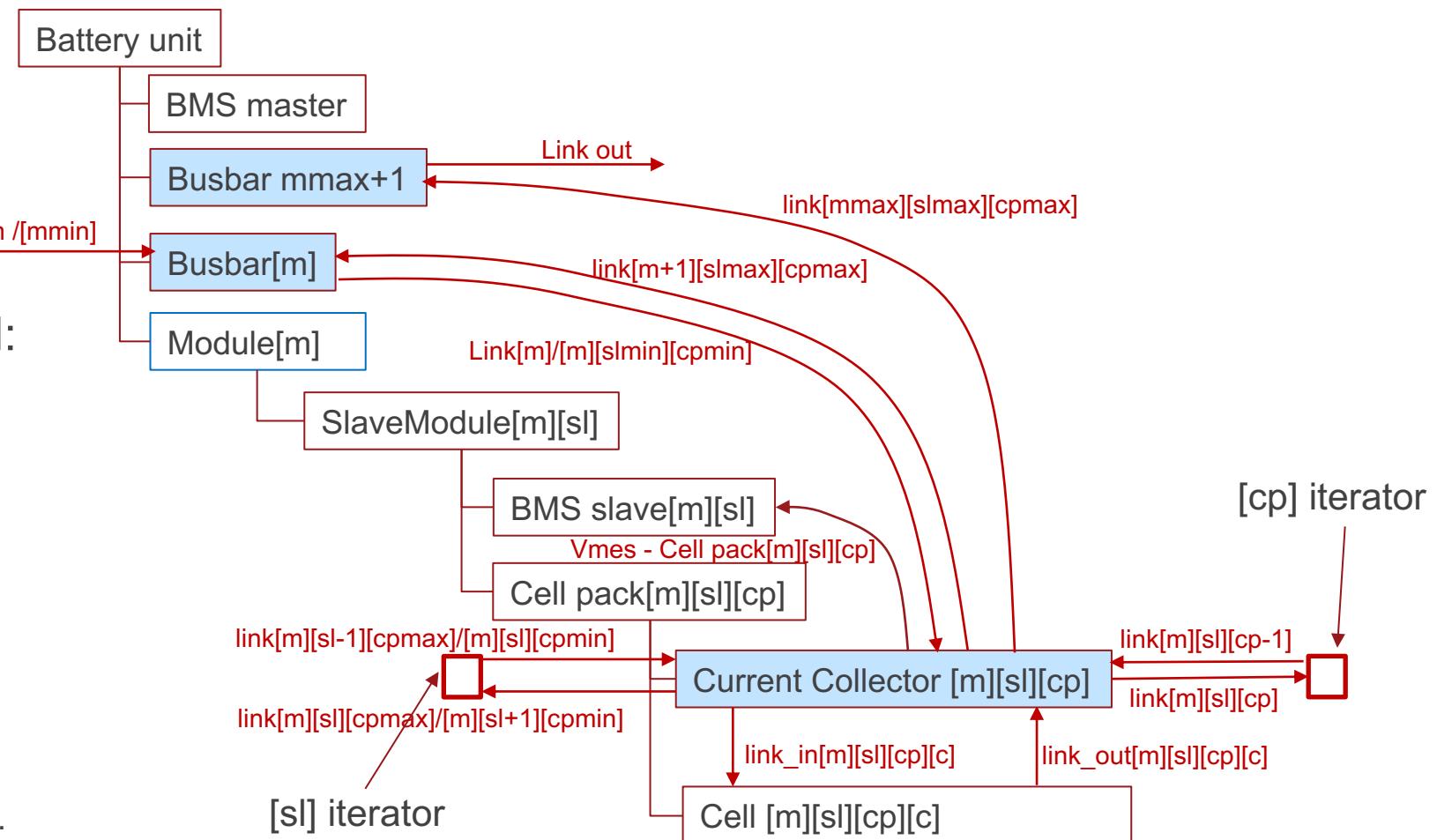
« `link[m][s][cp, 1]` » does exist if and only if

« *lik[li][si][cp-1]* » due  
aujourd’hui à un 1er commis

« link A/B » is a link from an object with parameter configuration A to an object with parameter configuration B

Iterator means the input and output flows correspond to each other w.r.t some parameter.

The interest here is to check that every produced flow is consumed and conversely.





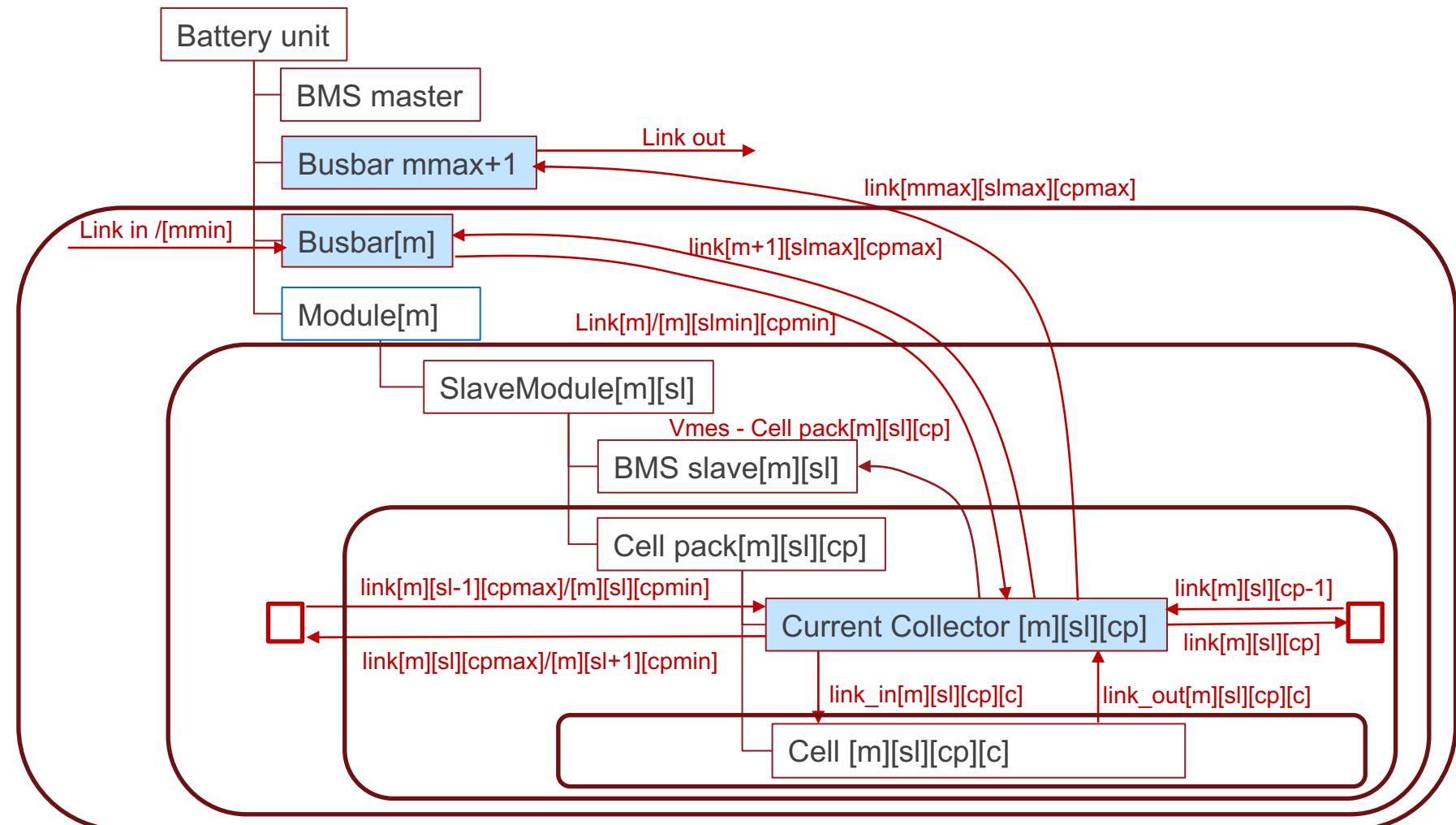
# Limits of Absolute Indexing

- Objects and flow identifiers get complex
    - Many parameters
    - Cumbersome naming
  - Difficult to manage for highly complex systems
    - Lung model should cope with more than 20 bronchial splits leading to more than 20 parameters.
- e.g for a tree structure:
- ```
graph LR; Root[Root] --> S1[S[s1]]; S1 --> S1S2[S[s1][s2]]; S1S2 --> S1S2S3[S[s1][s2][s3]]; S1S2S3 --> Dots[.....]
```

Can we find a more powerful syntax? We think so

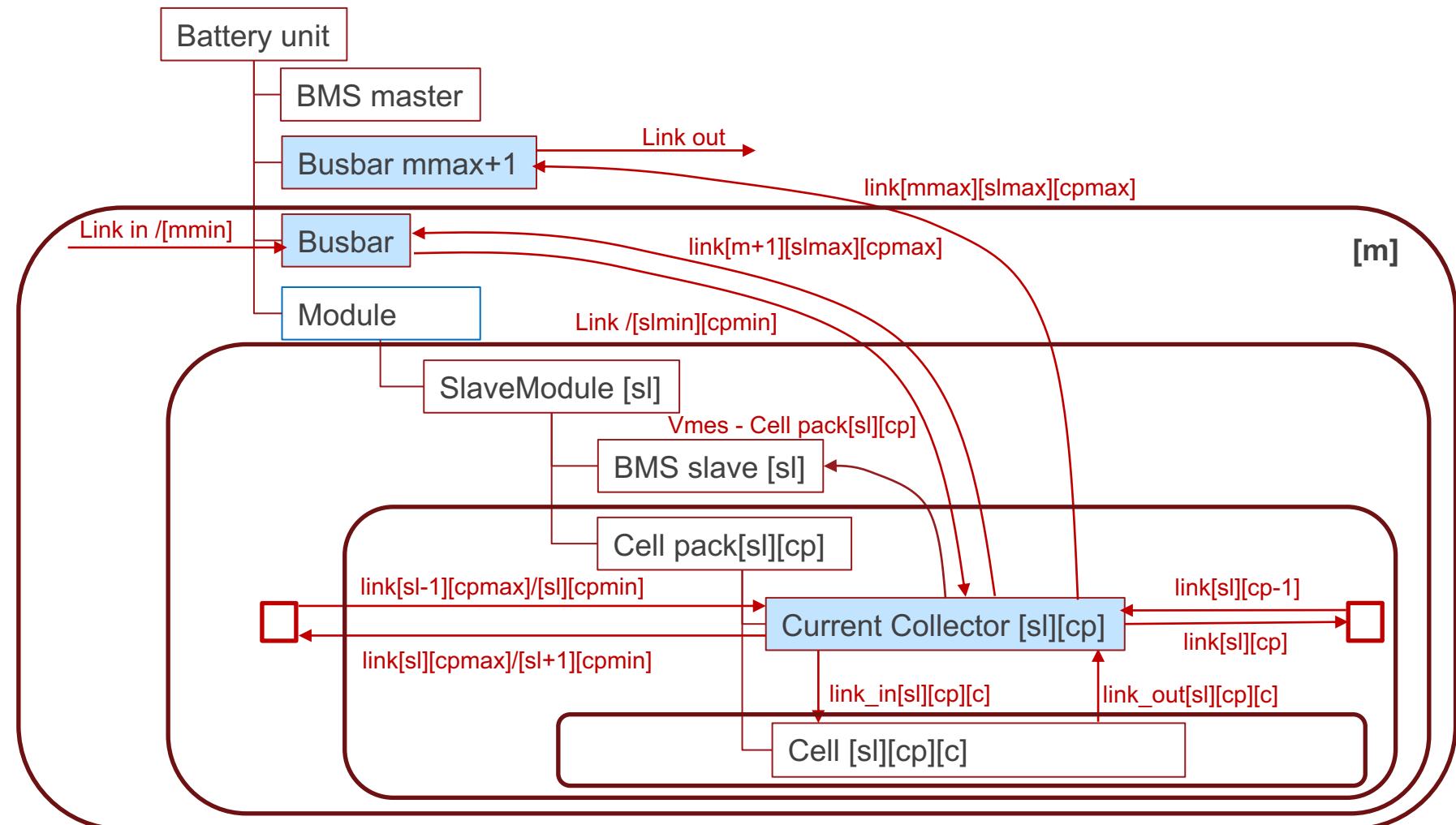


# Introducing Parametric Containers



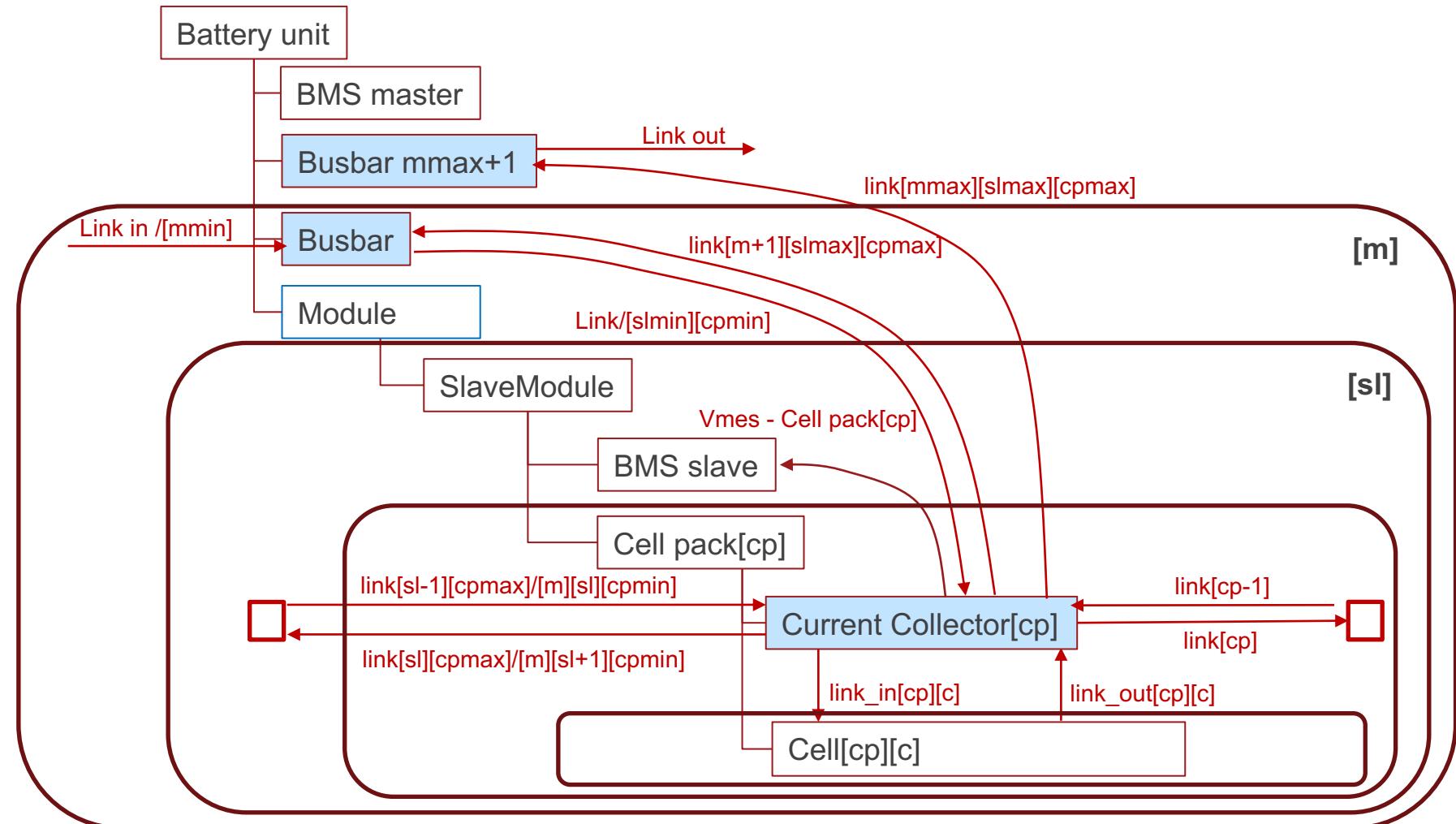


# Introducing Parametric Containers





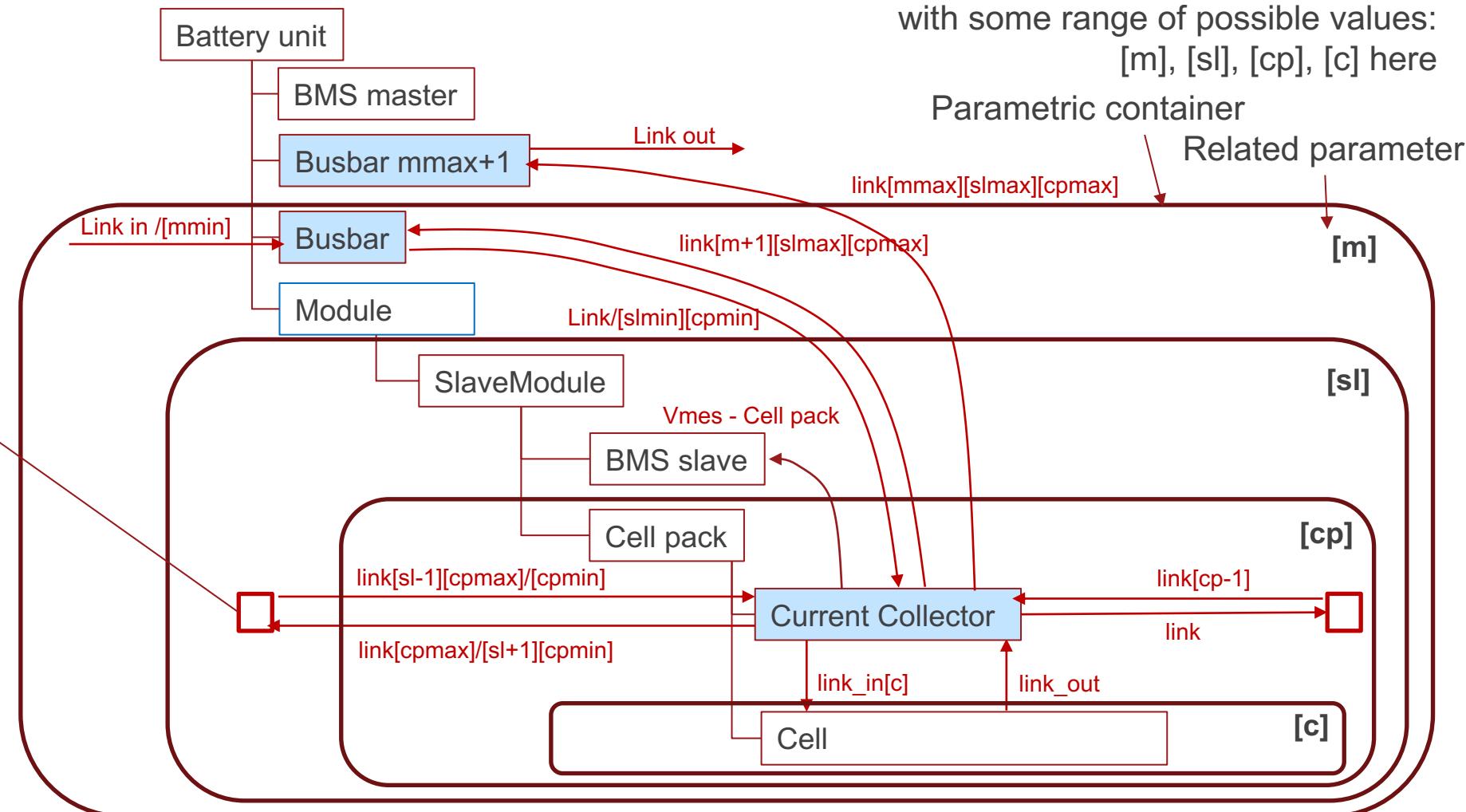
# Introducing Parametric Containers



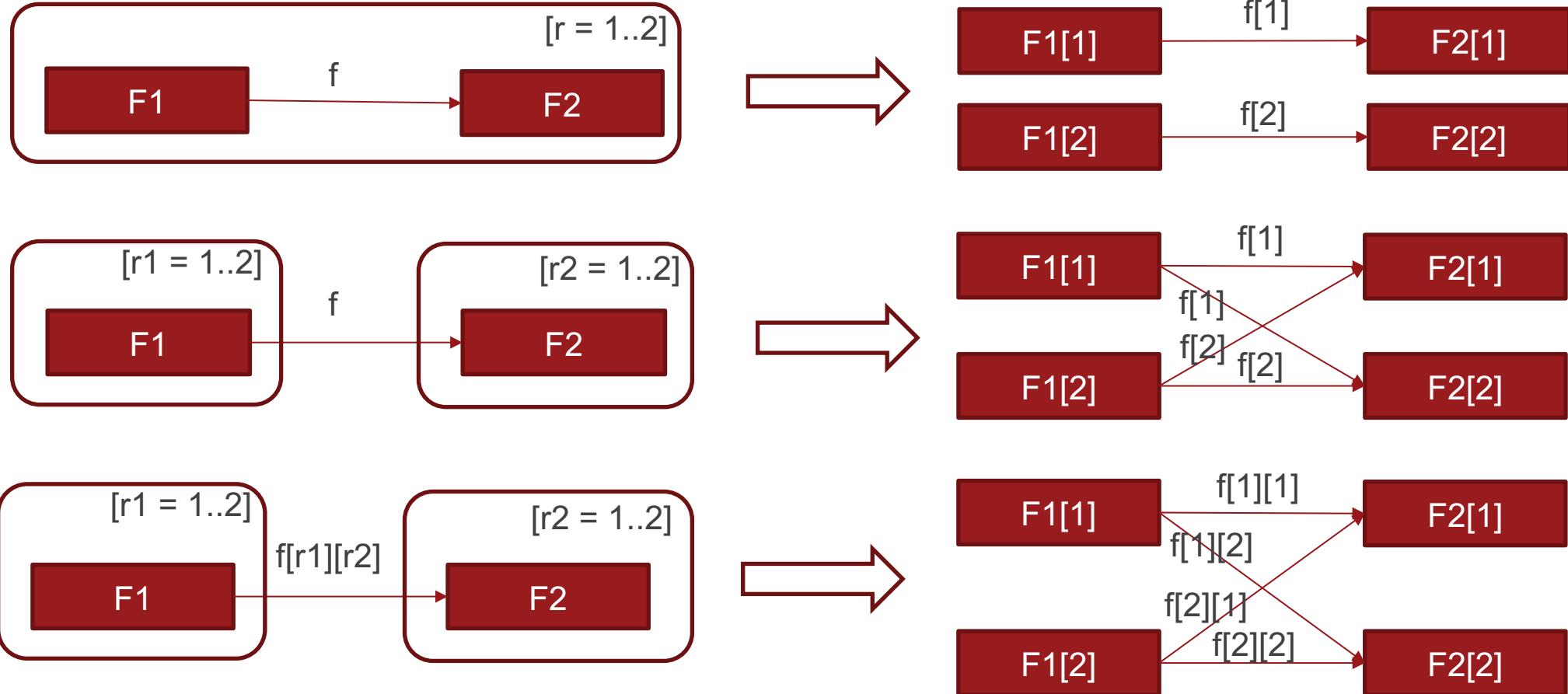


# Introducing Parametric Containers

Each container relates to a parameter with some range of possible values:  
[m], [sl], [cp], [c] here

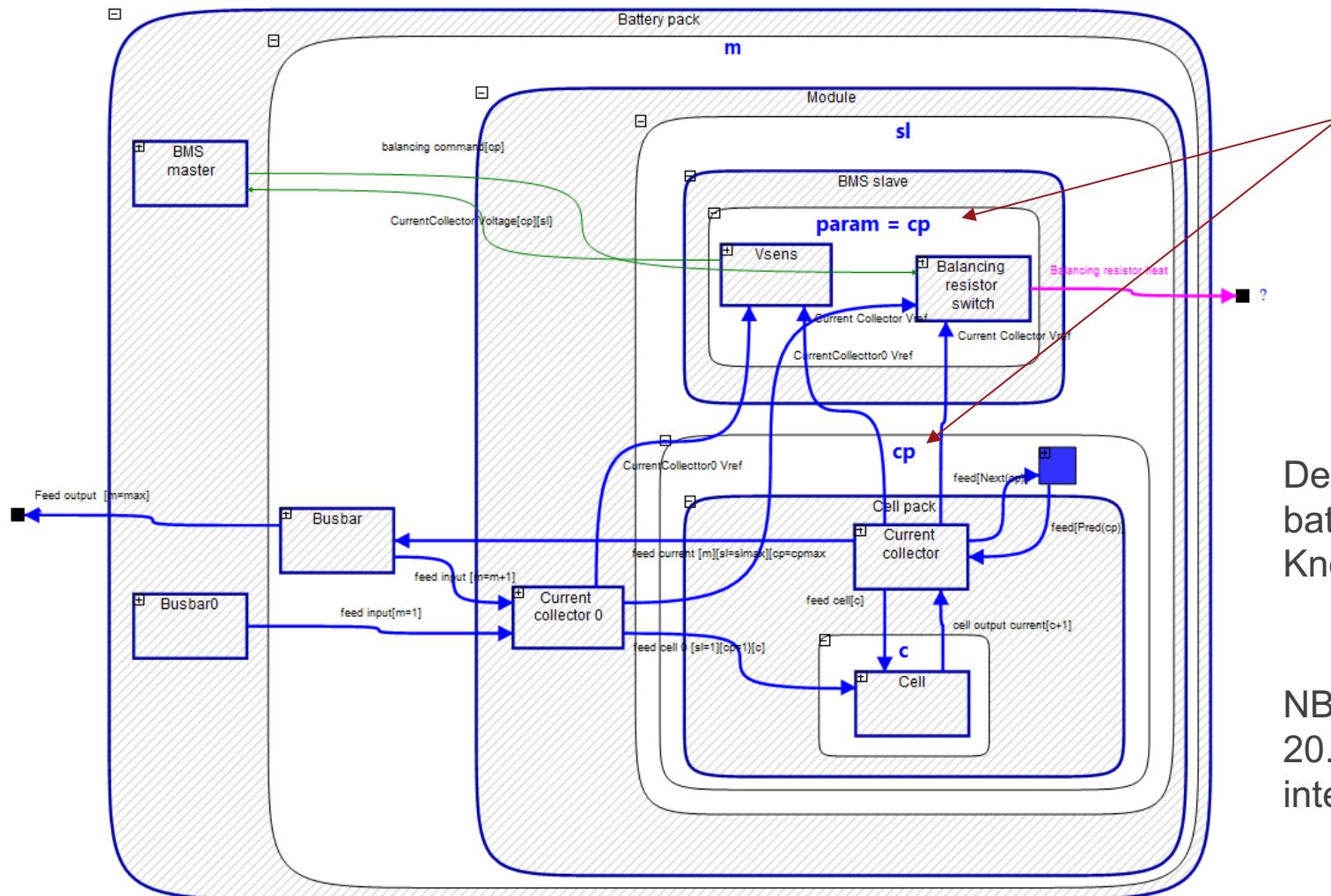


# Learnings: Applying Notation to Redundancy Strategies





# Learning: Parametric Containers with Flows



Nothing prevents from finding the same parameter container with several occurrences

Developing a data model for our battery example with arKtect<sup>©</sup> by Knowledge Inside SAS

NB: This model is supposed to be 20.000 objects and 100.000 interfaces large

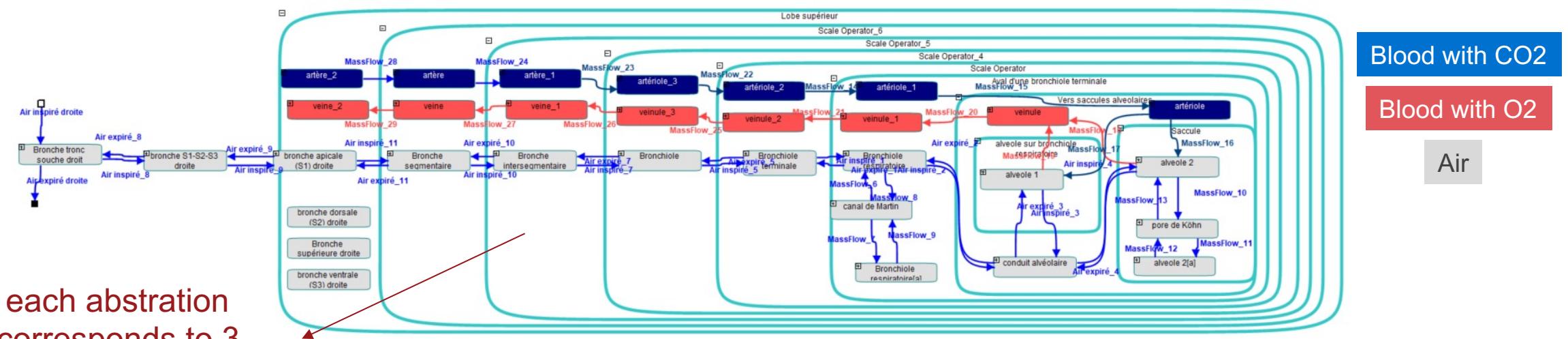
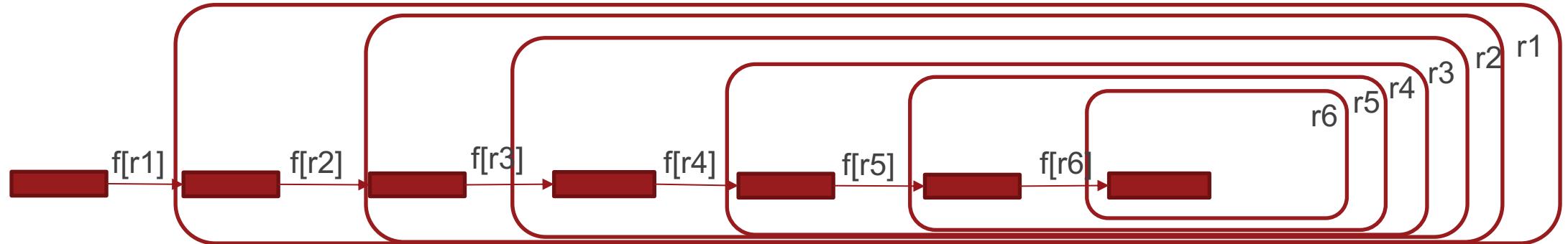


The number of layers and total number of avioli is daunting

## Modeling the Human Lung



# Learnings: Applying to Tree Structures



Here each abstraction step corresponds to 3 decompositions layers

Partial model of a lung modelled with arKtect© by Knowledge Inside SAS



In this presentation, we have merely started to formulate the problem.

## Conclusion and Path Forward



# Parametric Containers and SE Artefacts

- The Parametric containers are part of the system view or solution view. By system here we mean both a functional and organic concept.
- Requirements may apply to a particular instance or to a set of instances.
- Usually we think of having at least two distinct views:
  - Architecture view – the one we discussed previously
  - Requirements breakdowns structure – mainly for the purpose of traceability between requirements applied at different system levels including traceability w.r.t external requirements.
- Requirements should probably inherit parameters of the systems on which they are allocated. They possibly should be allocated with specific(conditional) parameter values as well.



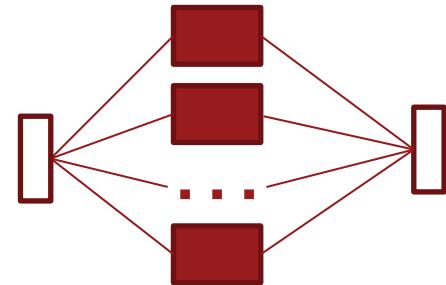
# Conclusion

- Parametric Container seem to be a pretty aesthetic approach for modeling faithfully systems with a recursive structure using only a logarithmic number of objects in the model.
- We tested this approach on different case studies. It allows lowering the complexity of the system for the system architect and allows to present a very compact holistic system view.
- Minimizing the number of views for a system description is for us a very strong indicator as it simplifies the topic both for the author and for every user of the result.
- The concept of solution may introduce geometric concepts (which is very natural). The concept of neighbourhood of a parameter instance depends on the geometric concept.
- The approach fits very well with a modeler. We simply introduce a new category of pervasive containers w.r.t. a classical Systems Engineering data model. Instantiation of parameters in functional chains is a must.
- It's clear how to specify a generation from the system model toward domain specific modeling tools afterward: e.g based on matlab, modelica....

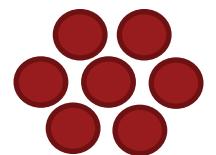


# Ongoing and Further Works

- A parameter angle may depend on it's parent parameter values.
- Available functions on parameters instances need to be clarified, min and max may not exist in case parameter range is not ordered  
**This is where geometric concept is needed and part of the concept of a solution**
- Possibly, we could imagine patterns of patterns: in the case of the lung, some levels of decomposition can be gathered because « they decompose the same way ». This leads to a higher complexity (parameters as patterns of subparameters) but more compact representation
- In the modeling approach, it is possible and important to generate automatically chains unfolding the parametric model for some sets of parameters values. e.g. you are interested to see what happens at the border of two modules of the battery, want to check side effects
- This approach allows defining an unambiguous naming of all objects in the product.



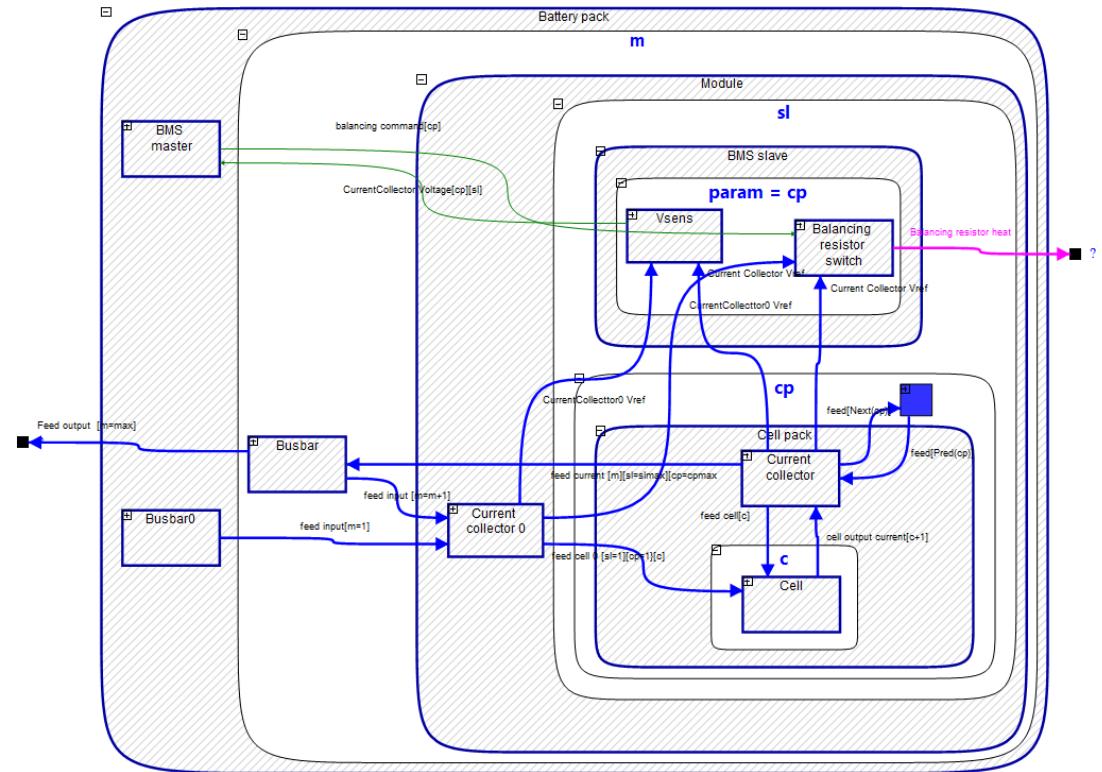
List of cells in parallel:  
**Min, max, +1, -1**



Set of tubes in a  
cooling  
exchanger  
**Numbering rules  
and functions**  
tbd



# Thank You



# Q&A



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