



32<sup>nd</sup> Annual **INCOSE**  
international symposium  
hybrid event

Detroit, MI, USA  
June 25 - 30, 2022

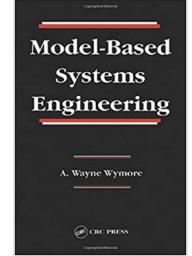
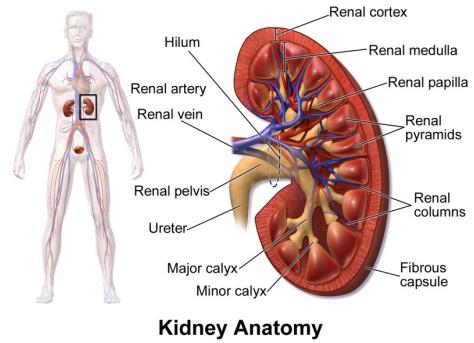
# Formalizing the Representativeness of Verification Models using Morphisms

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HUME CENTER FOR NATIONAL  
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# What do you think when you hear/read...?

Mass mock-up

Pedigree

Breadboard

Fidelity

Prototype

Final product

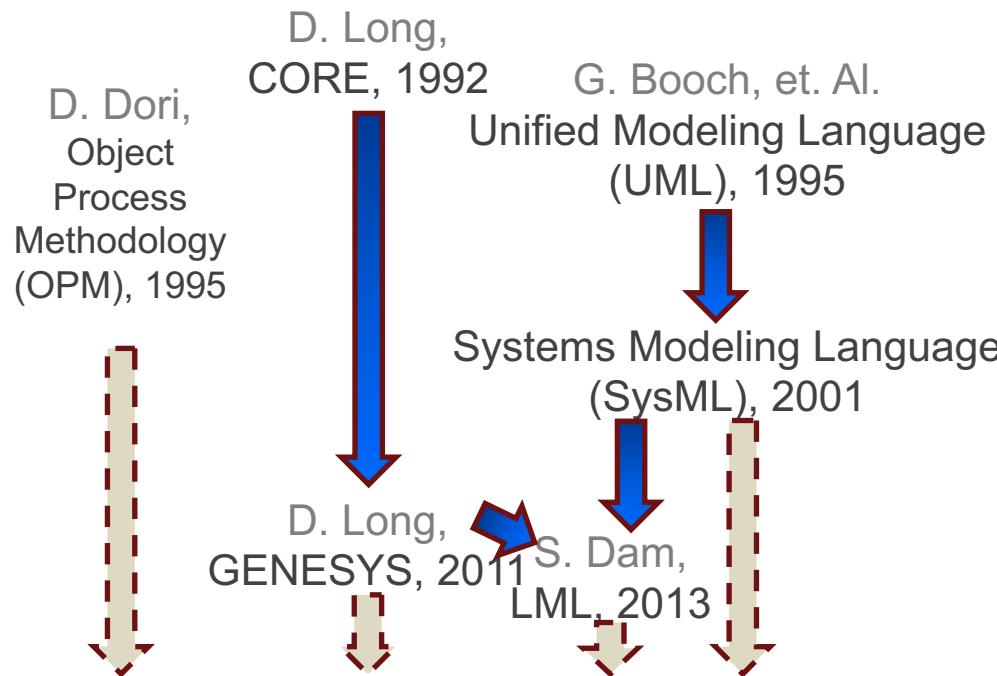
How do we determine validity of representativeness?

# Verification

- ...of adherence to system requirement
- ...activity using a verification model (VM)
- A VM is an (often) abstract representation of the system design (or final product)
- Awareness of the correspondence between the VM and the justification of the ascertain of the adherence of the system design to corresponding system requirements

# Systems Engineering Transformation

## Modern MBSE: Descriptive



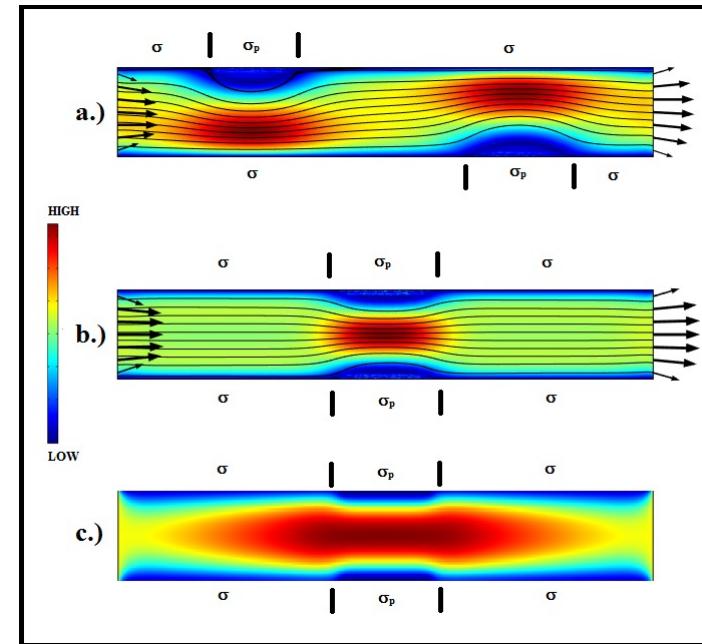
## Systems Engineering is in the midst of a transformation

- The practice still largely remains document-based (DBSE)
- Despite model-based (MBSE) tools and methods existing since the early 1990s
- A systematic literature review of ~1,300 articles suggests that MBSE is serving as a conduit to enable transformation to the digital paradigm (Digital Engineering/DE)

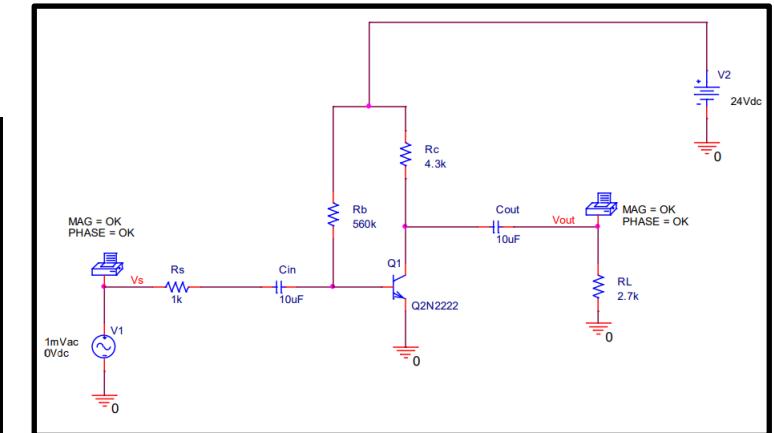
## Trajectory of MBSE: Keystone enabler to engineer systems within the digital paradigm

# Theory underpinning other domains

- Current forms of MBSE are descriptive and do not have theoretical foundations
- Other engineering domains have theoretical foundations upon which software platforms are implemented

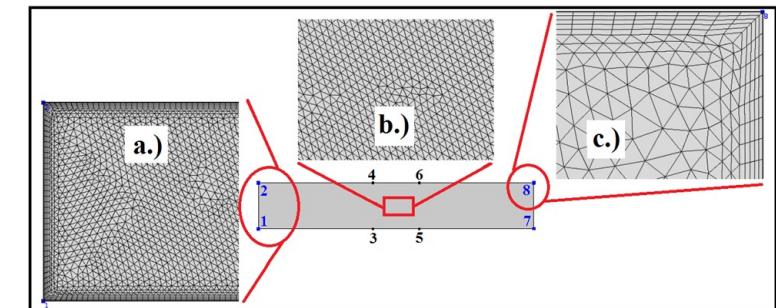


PSpice



[https://engineering.purdue.edu/~ee255/lecturesupp\\_files/PSpice-Tutorial.pdf](https://engineering.purdue.edu/~ee255/lecturesupp_files/PSpice-Tutorial.pdf)

<< Computational fluid dynamics

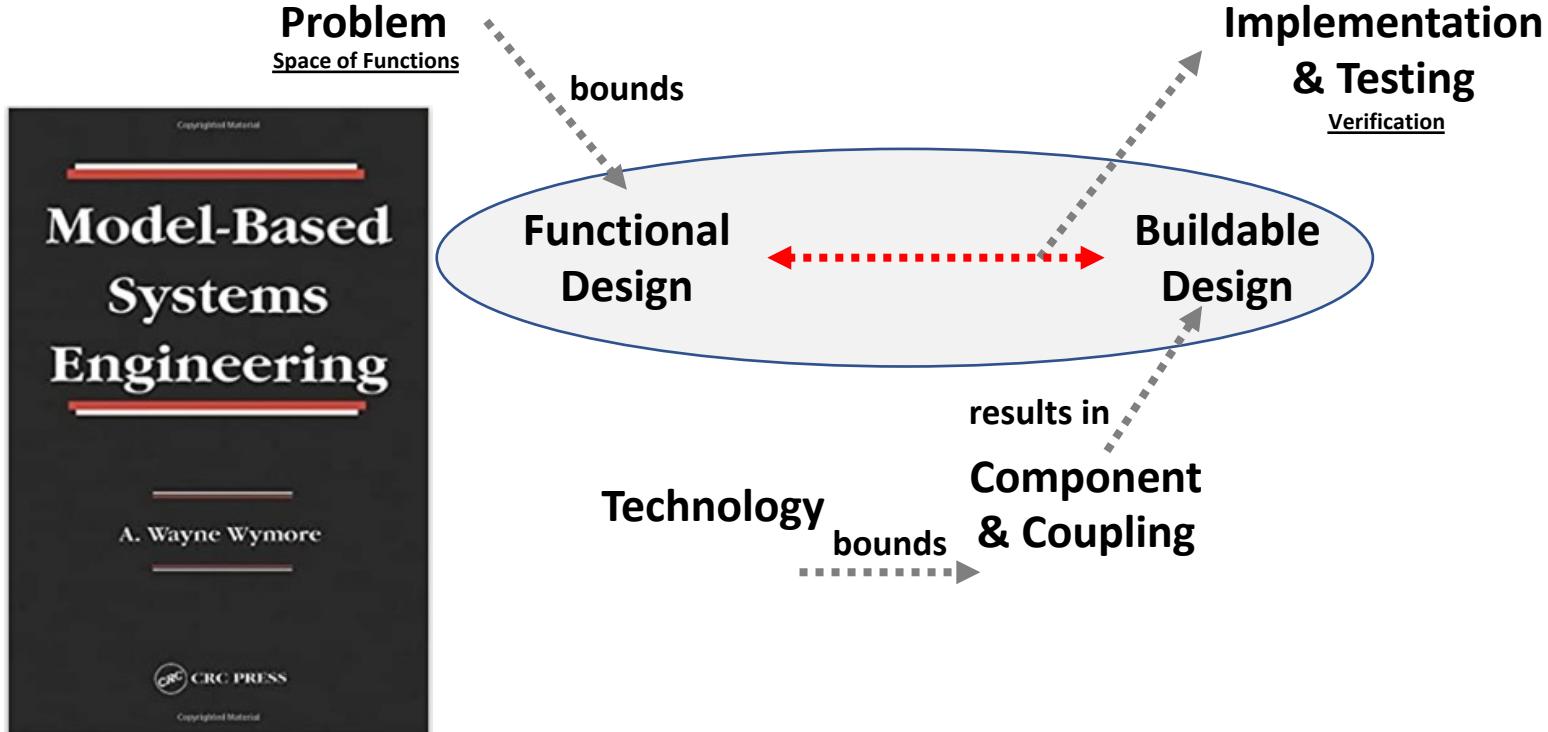


^ Finite element analysis ^

# A. Wayne Wymore



## ~Metamodel of T3SD



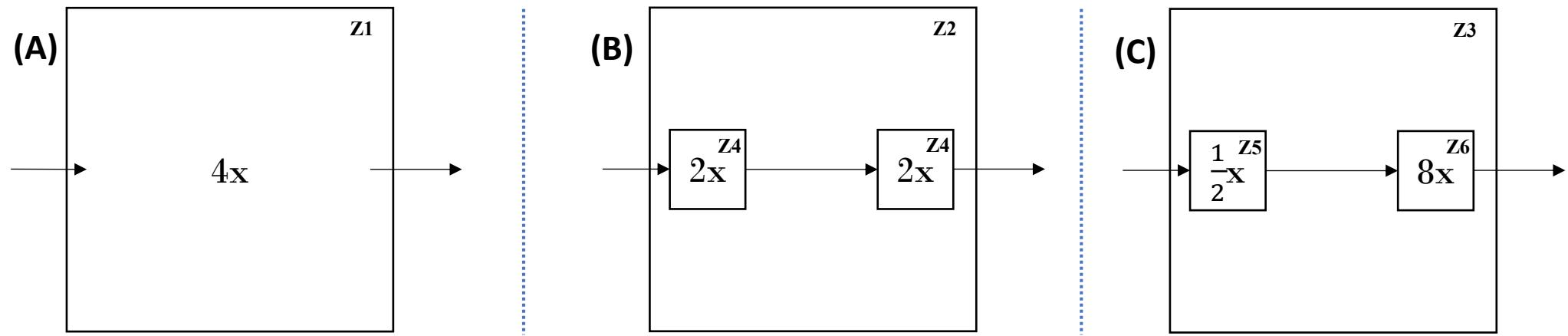
## Wymorian Systems Theory:

- Mathematical Theory of Systems Engineering
- Theory of Modeling and Simulation
- Tricotyledon Theory of System Design (T3SD) aka **theory of MBSE**
- Theory of problem (formulation) spaces

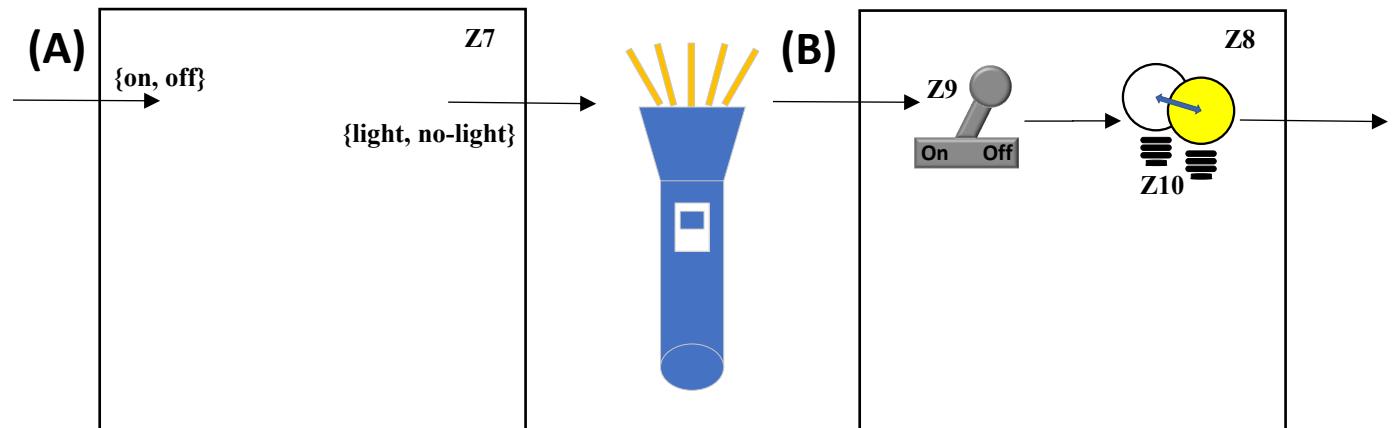
# For verification models...

**\*Start thinking in terms of morphisms**

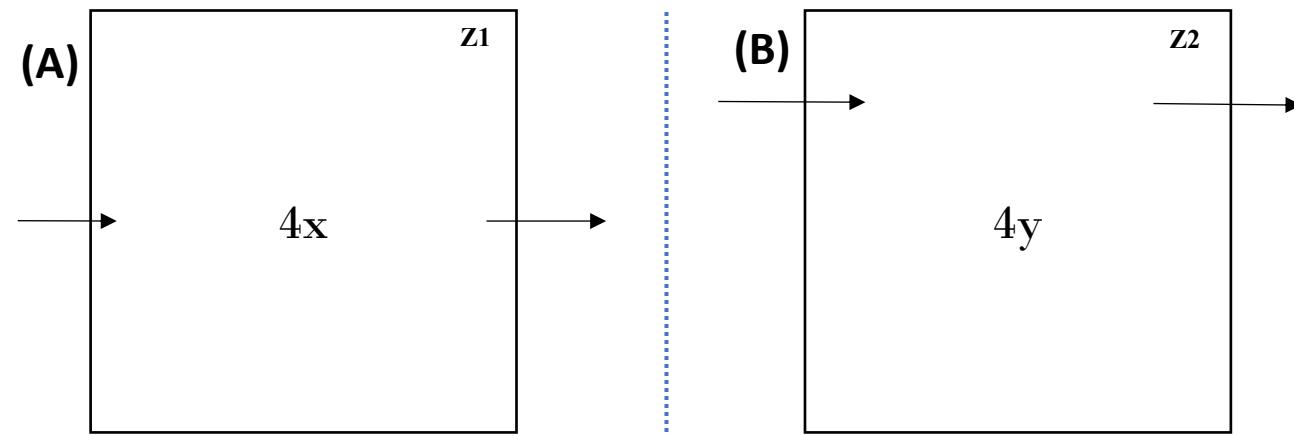
# Homomorphism



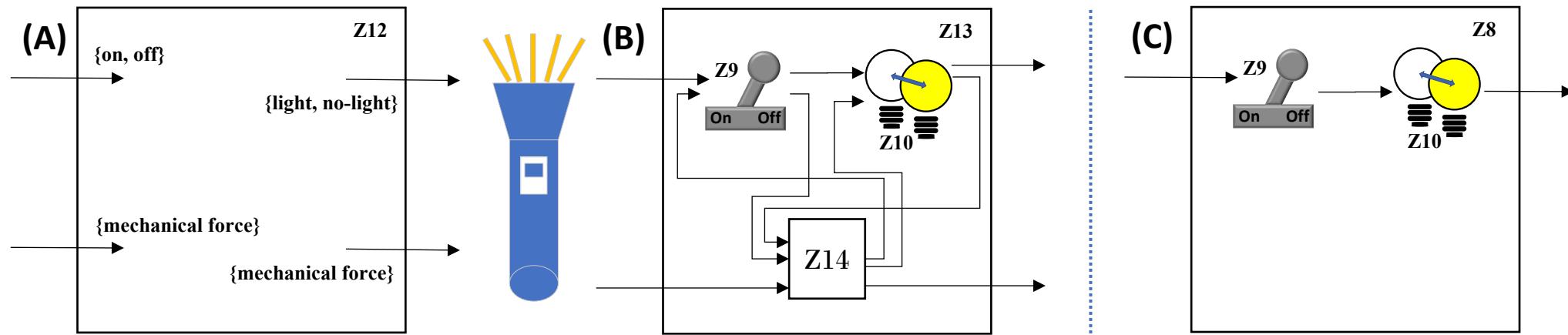
# Homomorphism



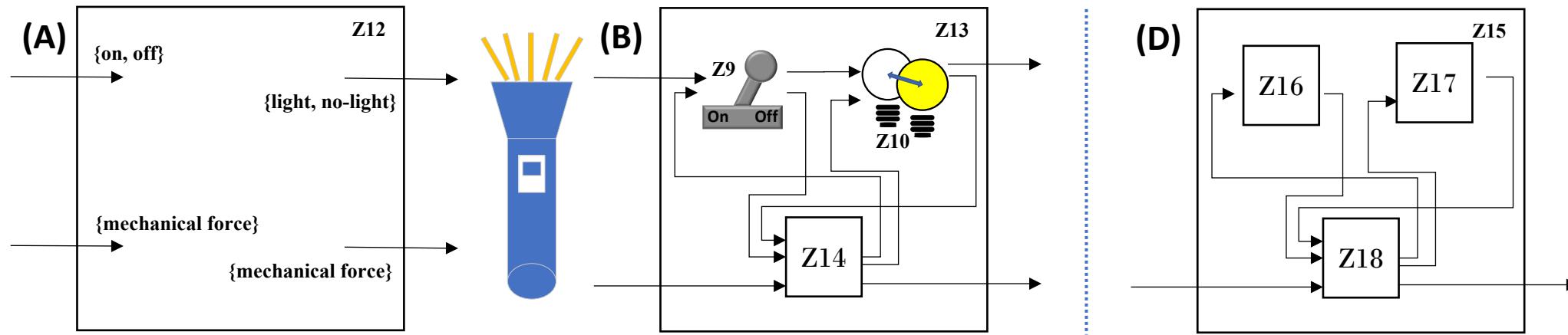
# Isomorphism



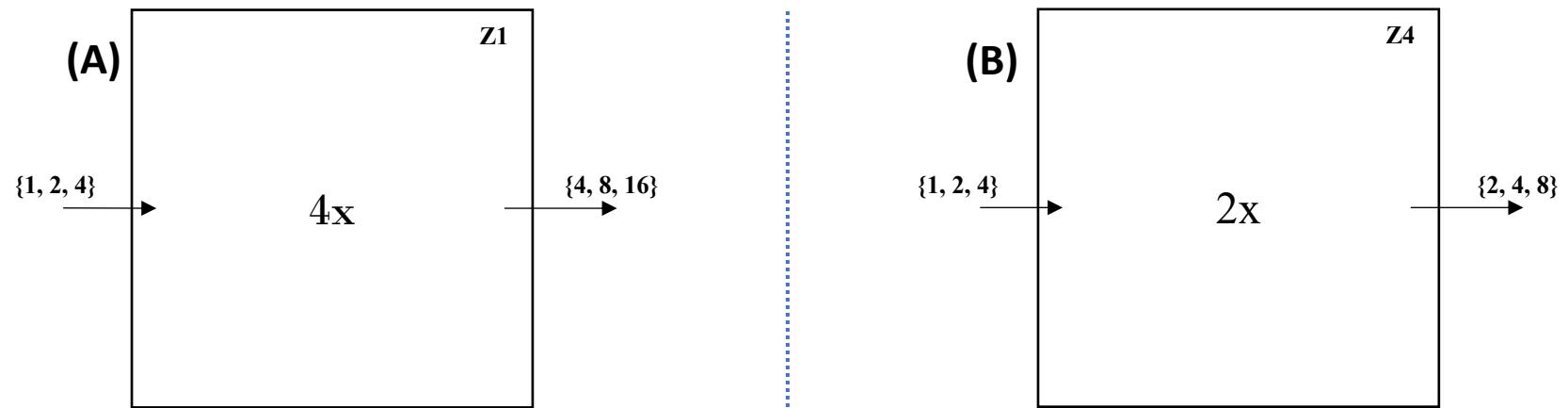
# Coupled system morphism



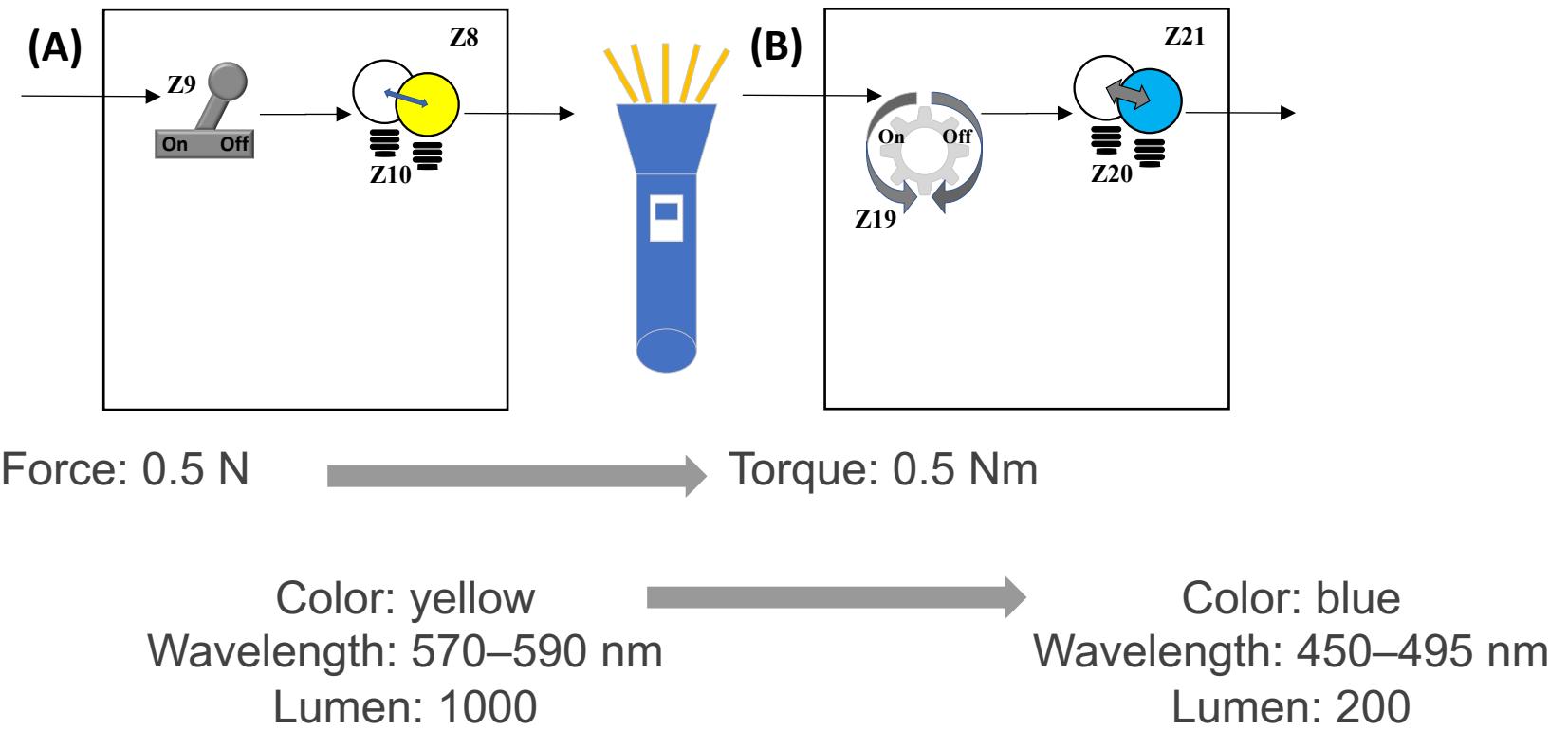
# Coupled system morphism



# Parameter morphism



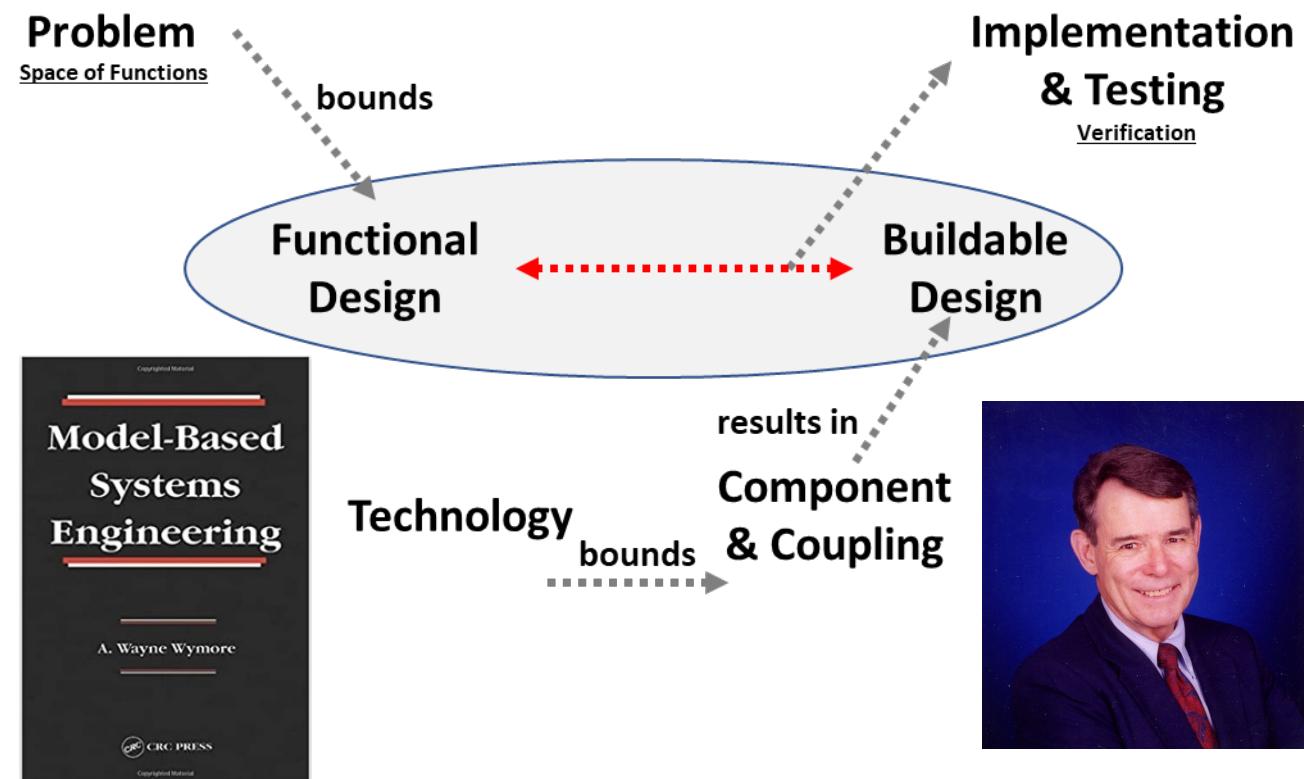
# Parameter morphism



# Start thinking in terms of morphisms

- ...for verification models
- Transition from implicit to explicit
- Verification is about confidence

## ~Metamodel of T3SD



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Thank You! Questions?



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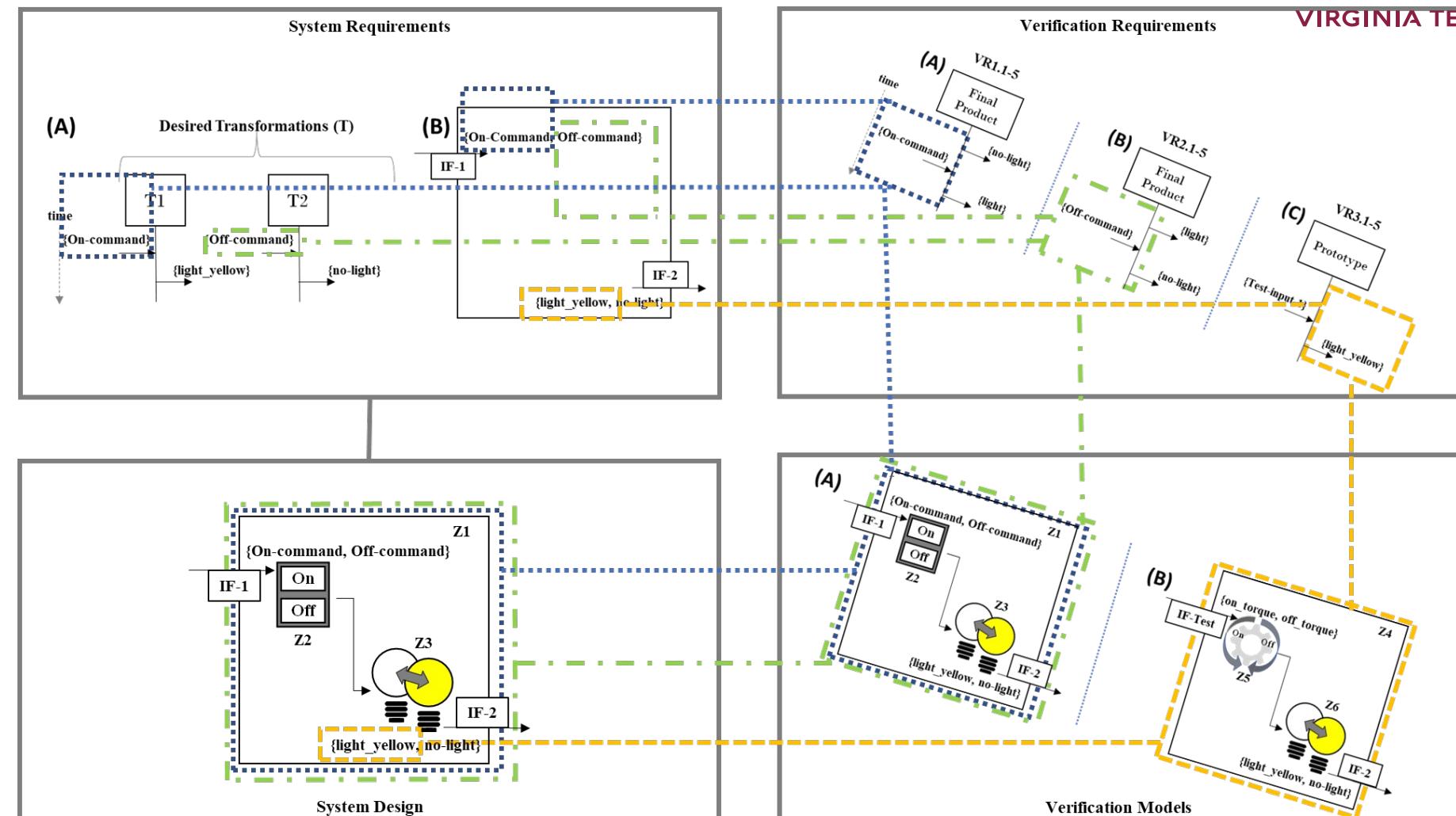
# Currently Exploring

- How “should” verification models be derived?
  - Currently exploring the framing of verification within the context of systems theoretic morphism

# Verification is about confidence

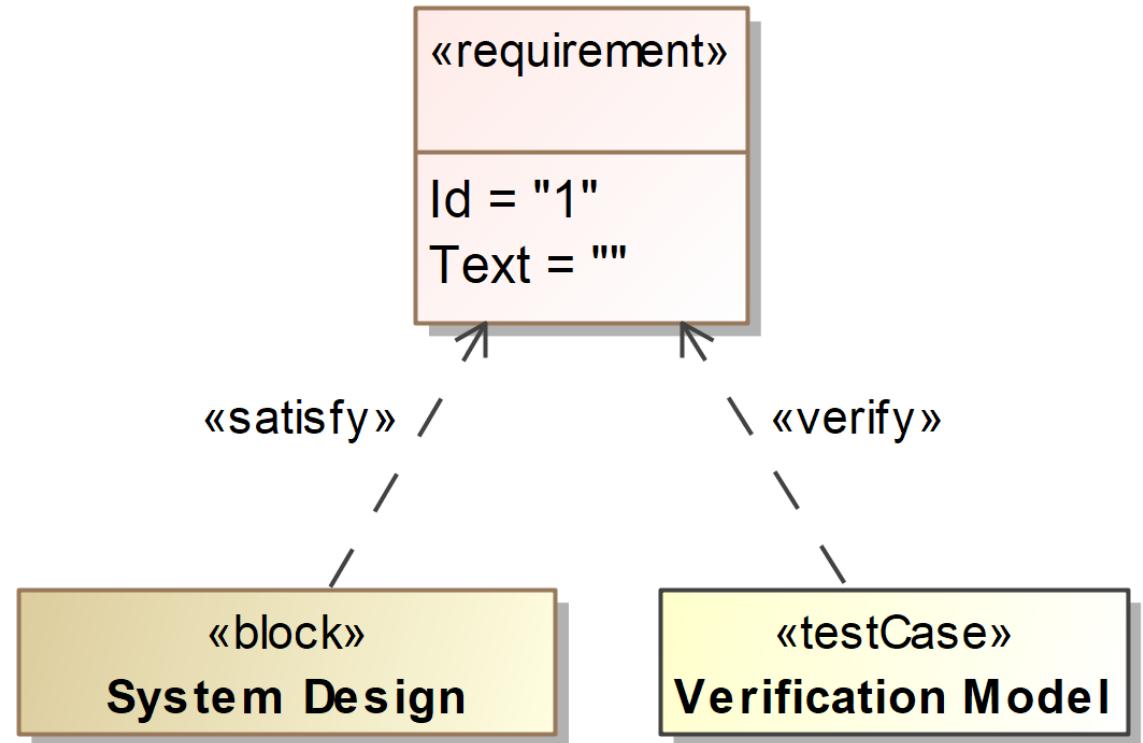
Research uses **systems theory** to frame the argument for confidence in the **systems design** adherence to **system requirements** through an **analogous verification model** observed within the context of the **verification requirements**.

\*Start thinking in terms of morphisms



# A look at SE model-based practice

- Does the “satisfy” relationship mean that the system design actually satisfies the requirement?
- Does the “verify” relationship provide exclusion criteria for acceptability of verification models?
- What is the theory underpinning these relationships?



# Systems Theory Perspective: System and System Requirements

- An **open system** is defined as a transformation of inputs into outputs transferred through interface(s)
- All system requirements can be modeled as **desired** transformations of inputs into outputs through **desired** interfaces
  1. Functional: what the system must do
  2. Performance: how well the system must perform its functions
  3. Resource: what the system may consume to perform its functions at the required performance
  4. Environment: settings or contexts in which the system must perform its functions

