

# On a Recursive Methodology for the Analysis of System Requirement Tolerances



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Part I

# Introduction & Overview

# Author Role

- Systems Engineer at Raytheon
- Supported requirement traceability, statistical analyses, and failure investigations
  - Supported AI/ML methods through development of verification techniques

- Statistical Tools
- Systems Theory
- Program Implementation

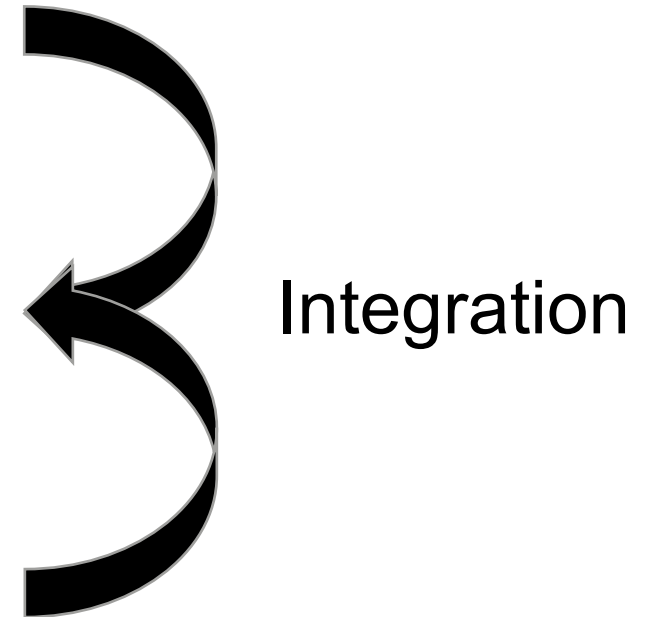
Author Responsibility

- AI/ML methods

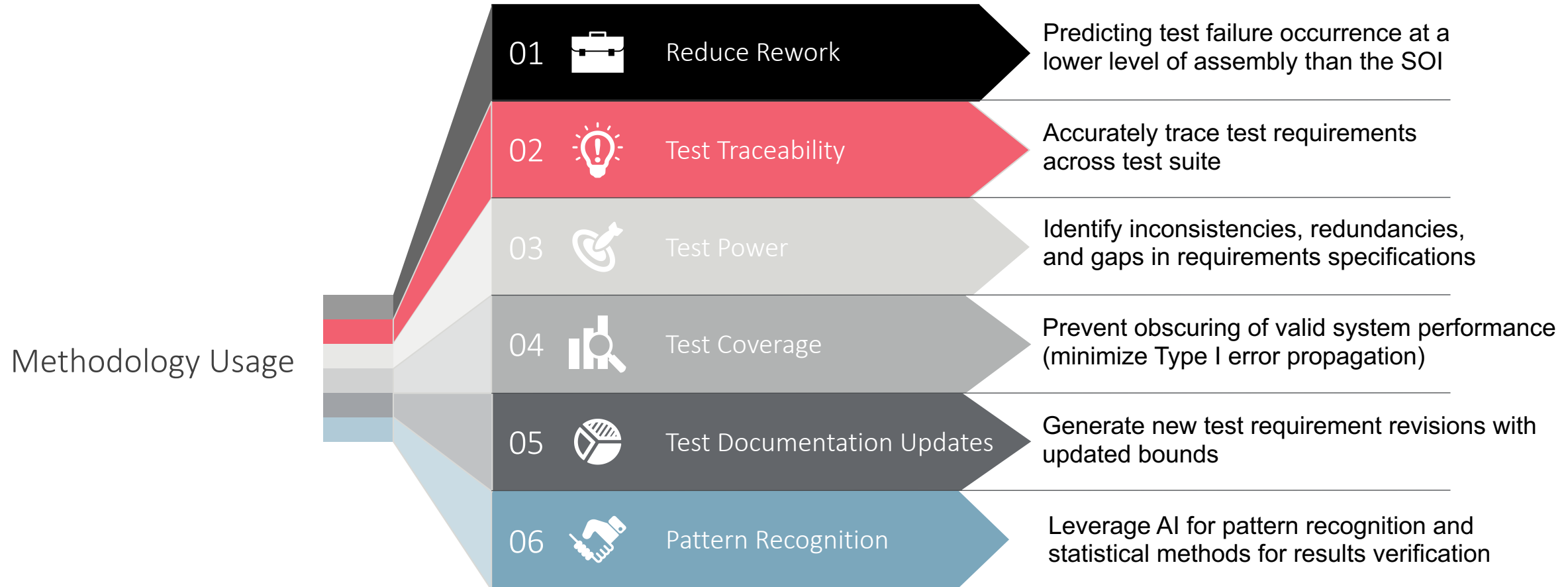
Software Team

- Subject-Matter-Expert (SME) interactions

Program Personnel



# Methodology Objectives

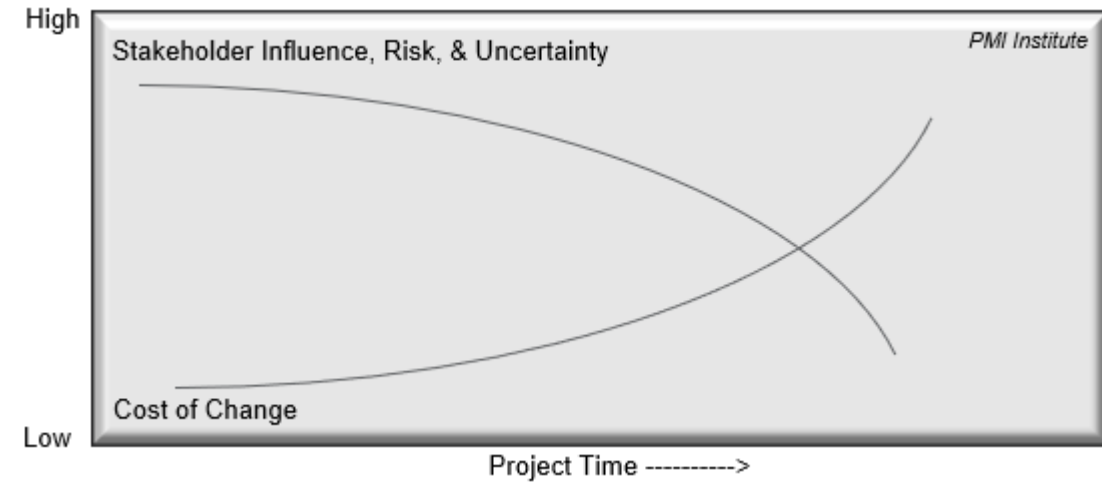
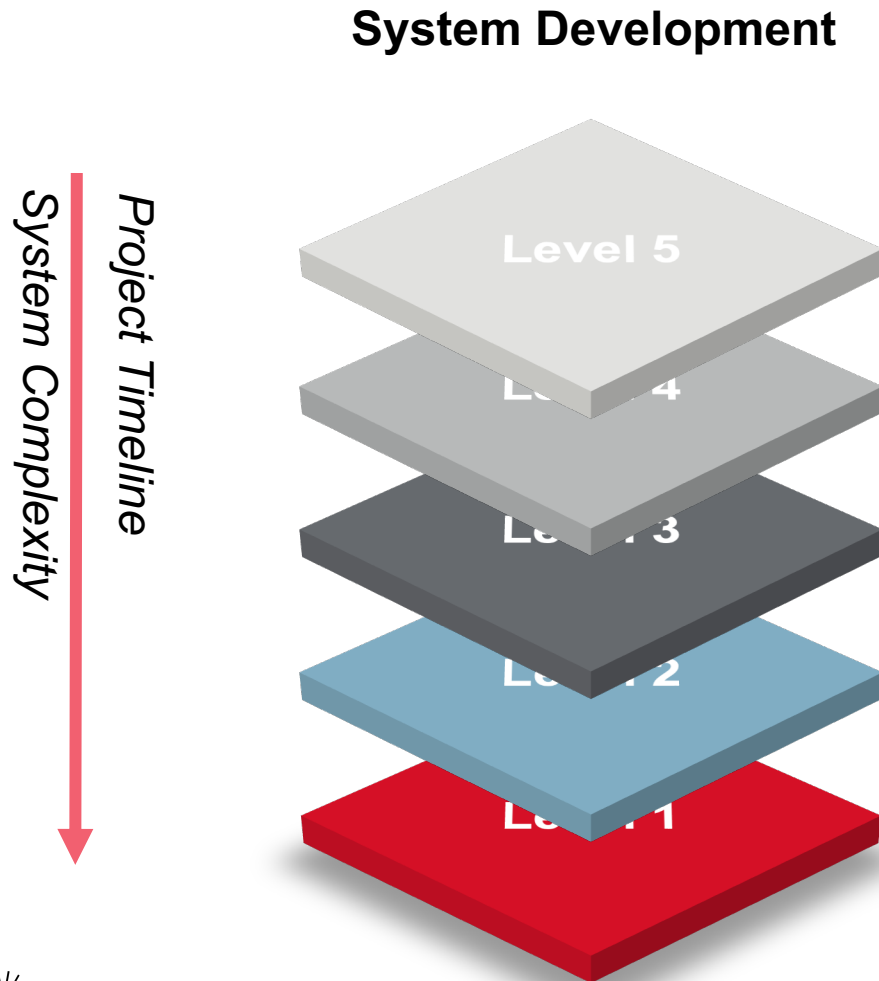


# Project Lifecycle



Source: PMI Institute  
Project close is omitted

# Rework Implications



*CCA Level Build Structures*

*Subsystems*

*Final System Build*

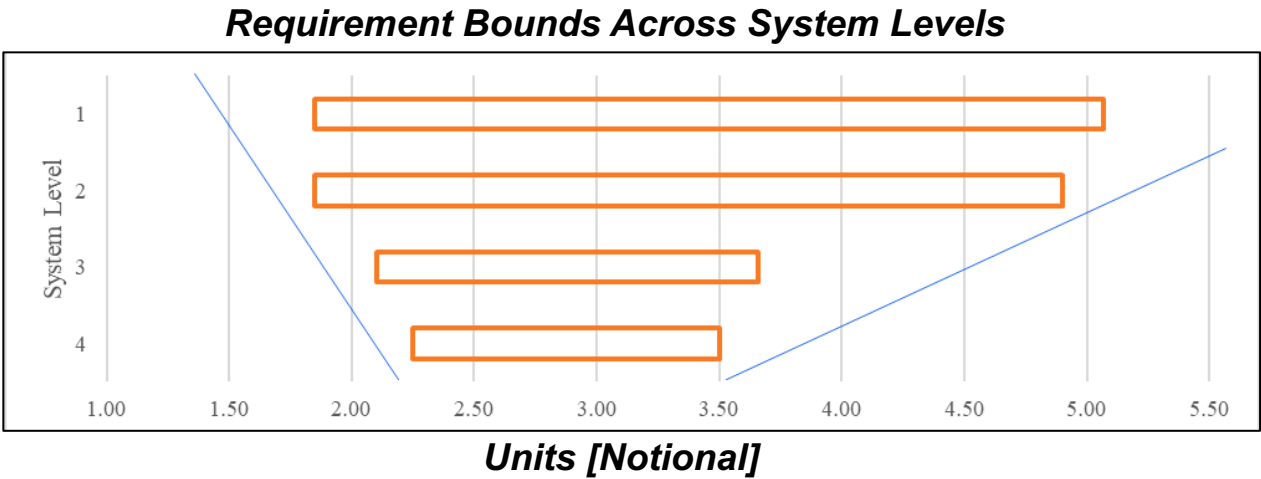
## Part II

# Methodology

Test ID	Function	Port Start	Port End	Lower Limit	Upper Limit	Units
Test #X	What does it do?	Port #Y	Port #Z	A	B	[units]

- Lower-level requirement bounds can be truncated to mitigate potential future failures
- Increase test precision
- Lower-level UUT changes are more cost-effective
  - Absence of confounding & system-system coupling effects

Funnel relationships amongst requirements with high correlation or derived traceability is desirable to capture **true** system performance

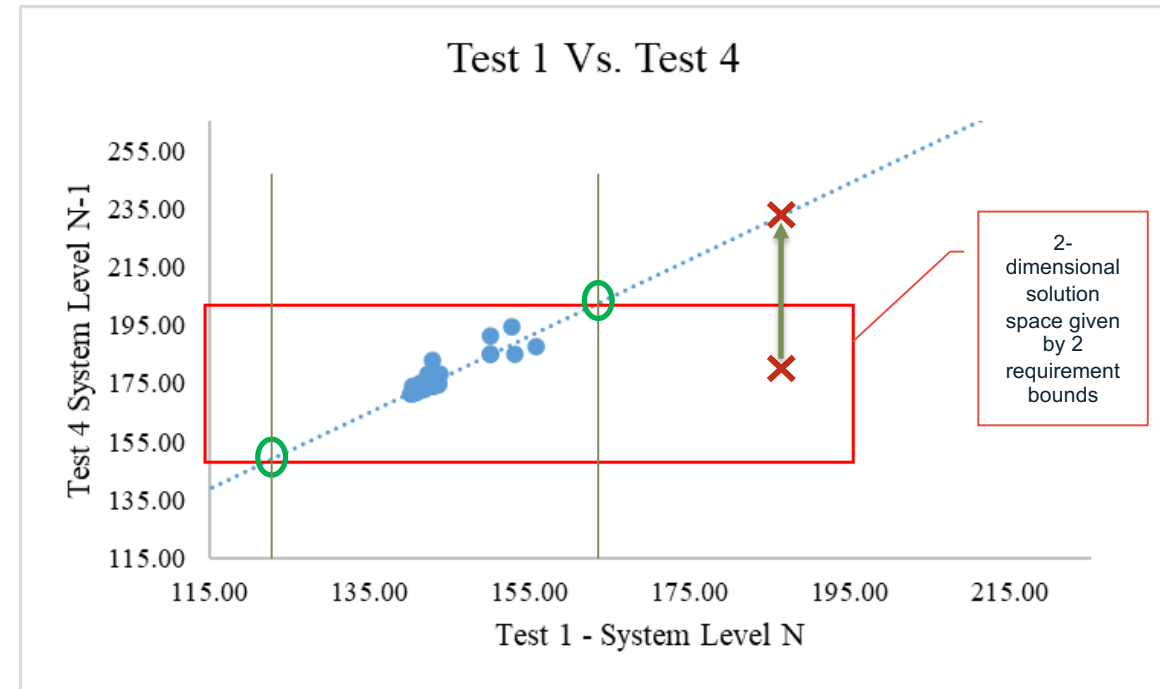


UUT – Unit Under Test



# Requirement Bound Truncation I

- Given a function describing the two data sets and the requirement bounds with some degree of correlation:
  - Truncate bounds along the regression line to limit allowable variation
  - Maintain funnel relationship
- Implication:
  - Allowing 2-dimensional solution space can lead to future test failures (see 'X' data point)
  - Requirement bound construction can yield inadvertent failures
- Post-Truncation:
  - Requirement bound truncation can prevent future test error propagation



# One-To-One Relationships

- Test relationships of the form:  $F(\text{Test } x_1) = F(\text{Test } x_2)$

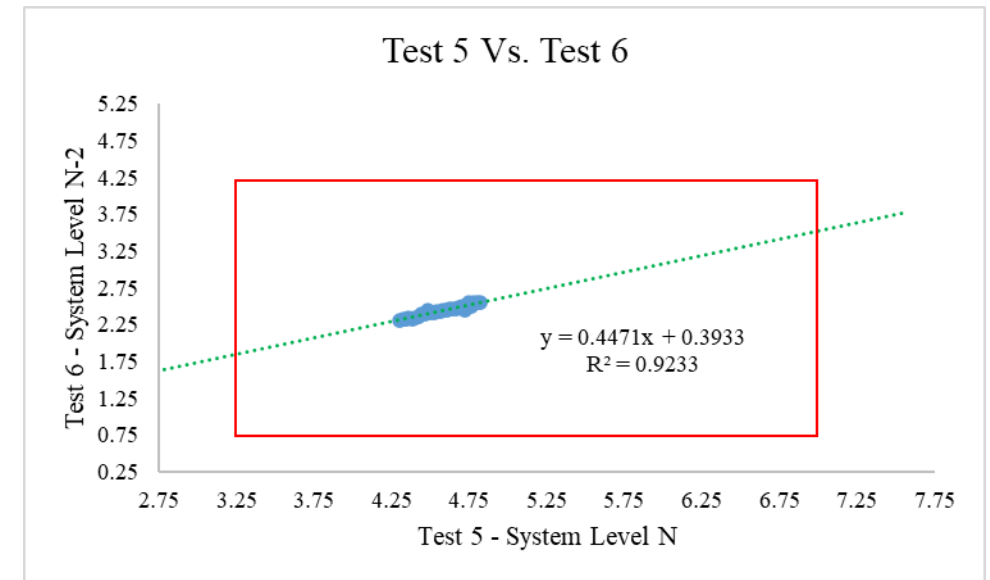
*Where Test Suite =  $[x_1, x_2, x_3, \dots, x_n]$*

- Test Criteria:
  - If tests are similar  $\rightarrow$  Can the data (samples) from  $x_1$  and  $x_2$  be shown to be from the same population?
  - If so, there is strong evidence to allocate the same lower & upper limits
    - Maintains funnel structure
  - ANOVA, Welch Z-Test as diagnostic tools
- Indicates incorrect bounds on requirements across test requirements

One-to-One Relationships can maintain funnel relationship if they can be shown to come from the same population

# Linear Relationships

- Test relationships of the form:  $F(x_1) = m \cdot x_2 + b$ 
  - Exists where SOS interactions/coupling effects influence test behavior
- Test Criteria:
  - Truncate bounds based on the intersection of the trendline, and requirement bounds (see slide 9)
  - Truncate bounds at some point and calculate the Type I Error Propagation for the proposed new bounds.



Linear Relationships may not always violate the funnel relationship, but allows for improving test coverage

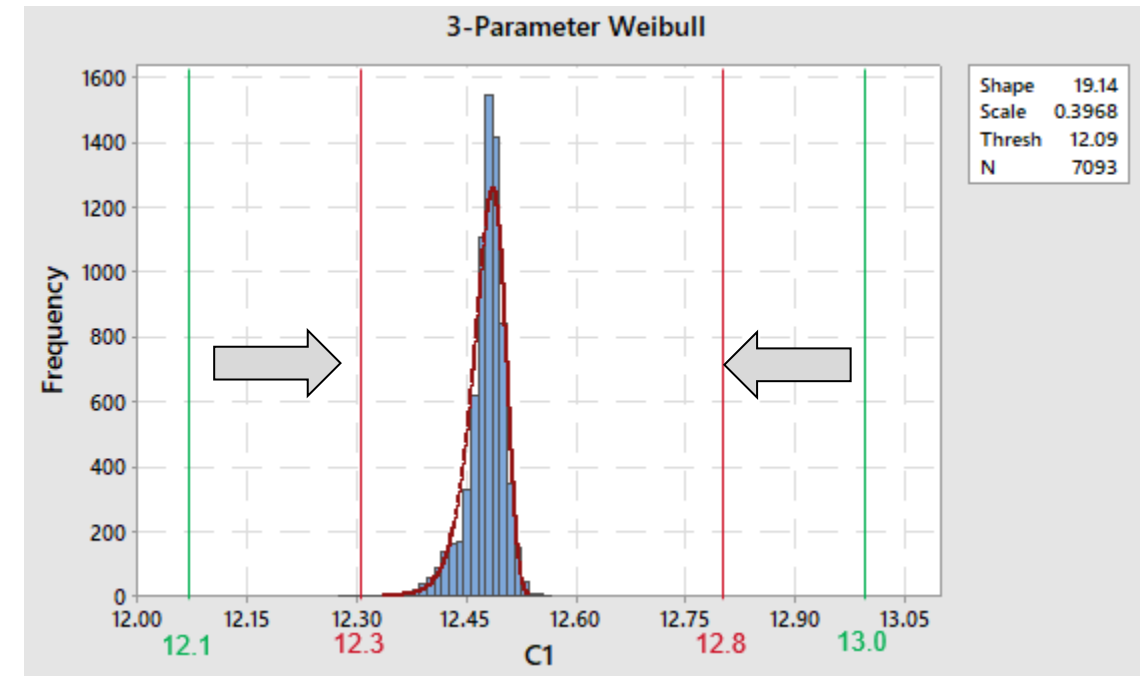
# Type I Error Propagation

- Determine best distribution to fit to test data
  - KS, AD statistics used as criteria using statistical software
- [Test 7] has the following distribution based on AD statistic
- Green bounds → Requirement bounds
- Red bounds → Truncated bounds

$$\text{Type I Error} = \int_{12.1}^{12.3} P(x)dx + \int_{12.8}^{13.0} P(x)dx \leq \eta$$

Where  $P(x) \sim \text{Weibull}(19.14, 0.3968, 12.09)$

Test 7 Distribution



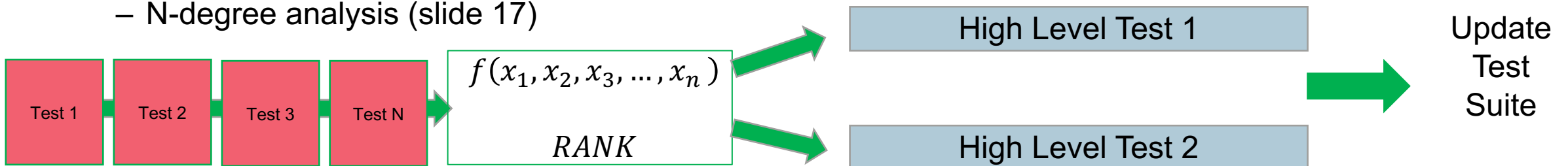
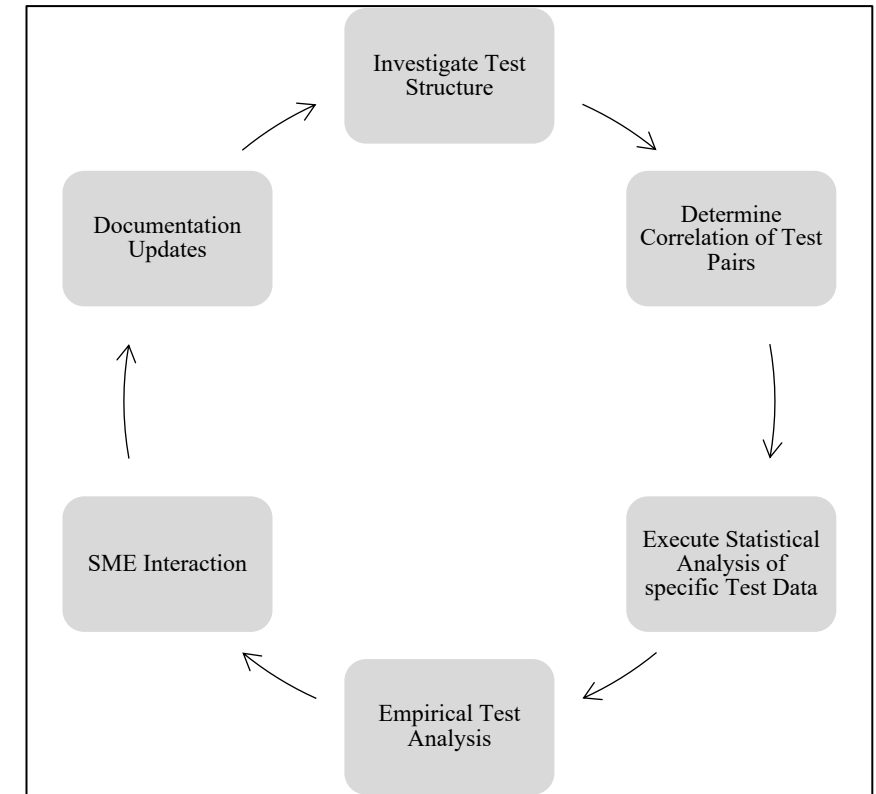
Given a change to requirement bounds, the resulting Type I Error probability must remain below a threshold value,  $\eta$

## Part III

# Results

# Overall Findings

- 30+ unique tests across 7+ requirement sets identified as valid changes
  - Highly correlated pairs selected for analysis
  - Test execution investigated to understand test conduct
  - Type I error propagation minimized ( $\eta \leq 0.1\%$ )
  - SME interaction to validate & verify changes reinforced findings
- More complex relationships discovered
  - Nonlinear relationships
- Greater inter-test dependency discovered
  - N-degree analysis (slide 17)



Requirement changes were approved by program document change authorities and new bounds were implemented

# Analysis Set

Part/Level	Test	Function	Part/Level	Corr.	LL (ms)	UL (ms)
CCA/3	Switch Close Time	Measure close time from specific Voltage	Battery Assembly/2	0.85	100	155
Aft Wing Assembly/1	Position Control	Measure deflection of wing following command	Test 1 (level 2 – wing assy.) Test 3 (level 4 – squib circuit 1) Test 7 (level 4 – tank release valve)	See slide 17	Multiple	Multiple

Let's investigate 2 examples

# Analysis Set Example I

*Bound truncation at higher system level from to lower-level tests*

## CCA Test

Part/ Level	Test	Function
CCA/ 3	Switch_Close_Time	Measure close time from specific voltage

$$R^2 = 0.921$$



## Battery Assembly Test

Part/Level	Test	Function
Batt Assembly/2	Voltage Steady State	Record time battery reaches steady state (41 V for time duration)

Lower Limit: 80 ms  
Upper Limit: 140 ms

Lower Limit: 70 ms  
Upper Limit: 225 ms

- Highest correlated pairs from the full factorial design investigated first
- Lower limit on level 2 violates funnel relationship; investigate truncation



# Analysis Set Example II

*Test suite investigation for opaque predictive relationships – generalized linear model*

## Test Set with High correlation to Final Assembly Build

- Test 1 (level 2 – wing assy.)
- Test 3 (level 4 – squib circuit 1)
- Test 7 (level 4 – tank release valve)

## Check-Out Test at Final Build Phase

- Test 44A – Aft Assembly wing switch position control

Units: mrad, tolerance of wing position

Multiple Linear Regression between Tests 1, 3, & 7 to Test 44A

Generate generalized linear model to determine failure modes on the independent var.

*Given by general form:*

$$Y_i = \beta_0 + \beta_1 X_{i1} + \beta_2 X_{i2} + \cdots + \beta_p X_{ip} + \epsilon_i$$

*for each observation  $i = 1, \dots, n$ .*

*The parameters  $\beta_{1...p}$  can be estimated to determine the effect of each sub – test to a test of interest at the higher system level*

## Part IV

# Concluding Remarks

# Conclusion

## Type I Error Propagation

New bounds showed no increase in false alarms

## Efficacy on High Failure Rate Components

Greatest cost savings on high failure rate components

- Touch Time
- Rework Operations



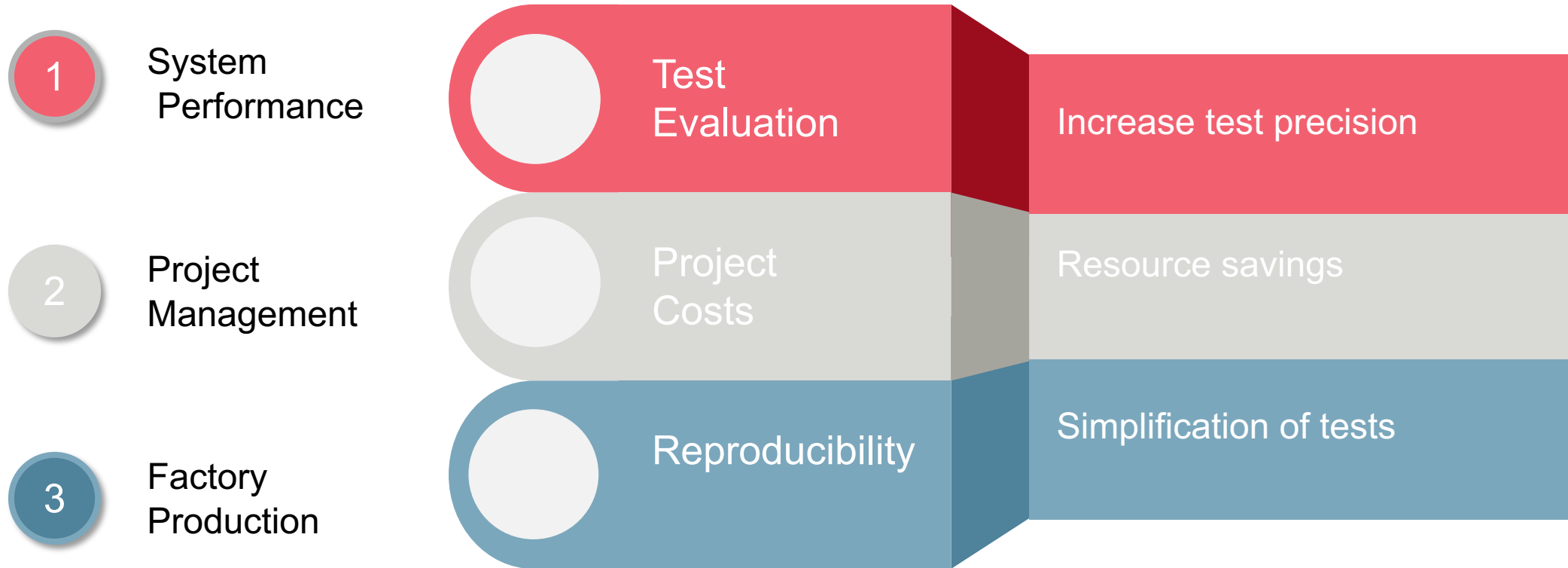
## Increase in Test Robustness

Eliminate Test Uncertainty  
Decrease Allowable Performance Variation

## Statistical Analysis

Using statistical methods as verification techniques for AI-driven results

# Functional Team Benefits



Methodology shows efficacy in RTX's domain:

- Complex systems with SOS interactions
- Expensive test operations
- High-failure rate components/technologies
- High-volume production
- Low-level production

# Questions

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